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| **Guidance on the use of codes for this mark scheme** | |
| M | Method mark |
| A | Accuracy mark |
| B | Working mark |
| C | Communication mark |
| P | Process, proof or justification mark |
| cao | Correct answer only |
| oe | Or equivalent |
| ft | Follow through |

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| **Question** | **Working** | **Answer** | **Mark** | **AO** | **Notes** | **Grade** |
| **1 a**    **b**  **c** |  | False. Experimental probability relies on real life and varies according to the number of trials carried out. You can get a different probability from two different sets of trials.  True. The more trials, the closer you get to the theoretical probability.  False. Relative frequency is  This is different from the theoretical probability, which is  Relative frequency is dependent upon the number of trials. | C1  C1  C1 | 2 | C1 for definition plus explanation oe  C1 for explanation oe  C1 for definition plus explanation oe | M |
| **3** |
| **2** |  | The frequency is approximately the same for each region of the spinner, suggesting that the spinner is likely to be fair. There are no obvious anomalous results to indicate bias, so there is no strong evidence to suggest it is not fair. | C1 | 2 | C1 for explanation | M |
| **1** |
| **3** | Joy wins:  0.65 × 52 = 33.8  which is approximately 34 wins.  Vicky won 10 times.  Joy + Vicky = 44 wins  Max = 52 – 44 = 8 wins | 8 times | M1  A1 | 2  3 | M1 for multiplication to find the number of Vicky’s wins  A1 cao | M |
| **2** |

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| **4 a**  **b i**  **ii**  **iii**  **iv**  **c i**  **ii**  **iii**  **iv**  **d** | P(Anna, Chloe)+ P(Anna, Clara)  + P(Chloe, Clara)  P(Ben, Ciaran) + P(Ben, Daniel)  + P(Ciaran , Daniel)  P(Chloe, Clara) + P(Chloe, Ciaran)  + P(Clara, Ciaran)  1 –= =  P(exhaustive outcomes) = 1  P(same sex) + P (not the same sex) = P(F, F) + P(M, M) + P(M, F) = 1  **OR**  P(two women) = P(A, Ch) + P(A, Cl) +P(Ch, Cl) =  P(two men)= P(B, Ci) + P(C, D) + P(Ci, D) =  P(opposite sex) = P(A, B) + P(A, Ci) + P(A, D) + P(B, Ch)+ P(B, Cl) + P(Ch, Ci) + P(Ch, D) + P(Cl, Ci) + P(Cl, D) =  ++= | Anna, Ben  Anna, Chloe  Anna, Clara  Anna, Ciaran  Anna, Daniel  Ben, Chloe  Ben, Clara  Ben, Ciaran  Ben, Daniel  Chloe, Clara  Chloe, Ciaran  Chloe, Daniel  Clara, Ciaran  Clara, Daniel  Ciaran, Daniel  =  =  =  =  No need to find all the pairs with different initials because it 1 minus the probability that all the pairs have the same initials.  Mutually exclusive as cannot select the same person twice.  Mutually exclusive as ‘two men’ cannot include a man and a women, and vice versa.  Mutually exclusive as no two men have the same initial.  **Not** mutually exclusive as there are possible combinations where two women have the same initial, such as Chloe and Clara.  Picking two people of the same sex and picking two people of opposite sex.  This is mutually exclusive **and** mutually exhaustive because the total probabilities add up to 1. | P1  M1  B1  M1  M1  M1  C1  C1  C1  C1  C1  C1  M1 | 3 | P1 for being methodical  M1 for addition of fractions  B1 for simplification  M1 for addition of fractions  M1 for addition of fractions  M1 for subtraction from 1 oe  C1 for explanation with method  C1 for mutually exclusive with correct explanation oe  C1 for mutually exclusive with correct explanation oe  C1 for mutually exclusive with correct explanation oe  C1 for mutually exclusive with correct explanation oe  C1 for mutually exclusive with correct explanation oe  M1 for full demonstration of exhaustive outcomes to support argument oe | M |
| **13** |

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| **5 a**  **b**  **c**  **d** |  | Probabilities on all the branches at each split must sum to 1 because they are mutually exhaustive and exclusive (an outcome happens or another outcome happens until all possible outcomes are accounted for).  The probabilities at each stage may have the same denominator if they are independent (with replacement) or the denominator may change if they are dependent (without replacement).  Final probabilities must sum to 1 because all possible outcomes have been considered.  The probabilities on all the branches at each split must sum to 1 because they are exhaustive and must describe all possible outcomes for that event.  Denominators for the same event at different stages will be different if the question specifies ‘without replacement’, for example, when choosing counters without replacement, there are fewer counters to choose from after each choice.  Check each set of branches sum to 1.  Check whether choices are made with or without replacement.  Make sure you know when to add P(A) and P(B) and when to multiply.  Check that sum of the final probabilities after multiplication along the branches is 1. | C3  C1  C1  C1 | 2  3 | C1 for explanation that includes mutually exclusive events  C1 for explanation that includes independent events  C1 for clear, complete explanation  C1 for clear explanation of exhaustive events  C1 for clear explanation of dependent events  C1 for at least three checks that include final probabilities sum to 1 oe | M |
| **6** |
| **6** | P(rain, not rain) + P(not rain, rain)  = 0.25 × 0.52 + 0.75 × 0.48  = 0.49 | 0.49 | M1  A1 | 3 | M1 for multiplication of rain and complement  A1 | M |
| **2** |

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| **7 a**  **b**  **c** | 100 ÷ 36 = 2.7 | P(1, 1) = He can expect to win one in 36 times so should expect to have 36 goes to win at least once.If he has 100 goes, then he can expect 3 wins. | M1  C1  C1  P1 | 3 | M1 for correct calculation cao  C1 for good use of diagram such as two-way table to support explanations  C1 for correct interpretation of 36 outcomes, of which only one wins  P1 for division, rounding and correct interpretation in context | M |
| **4** |
| **8 a**    **b**  **c** | P(G) = g  P(Y) = y  We want g2 = gy × gy  If you assume any value where g = 2y  then  g2 = (2y)2 = 4y2  gy × gy = 2y2 × 2y2 = 4y2  So the probabilities will be the same, as required. | P(B, B) = ×=  P(R, B) = 1 – (P(B, B) + P(R, R))  = 1 – (+)  = as required.  No, the probabilities are not the same because:  P(Y, Y) =  ×  =  P(G, G) =  ×  =  P(Y, G) = 1 – (P(Y, Y) + P(G, G))  = 1 – = =  So the probability of scoring green twice is not the same as the probability of scoring yellow and green in this case.  Any spinner with twice as many greens as yellows, such as one divided into six equal sections, with two yellow and four greens in any position.  P(Y) = ; P(Y, Y) =  P(G) = ; P(G, G) =  P(Y, G) = 1 – P(Y, Y) + P(G, G)  = 1 –=  So P(G, G) = P(Y, G) | M1  P1  A1  C1  P1  M1  B1  C1 |  | M1 for multiplication of × and subtraction from 1  P1 for use of technical notation and possible use of tree diagram to aid explanation  A1 for multiplication leading to correct probabilities cao  C1 for use of correct probabilities to compare and justify ‘no’ answer  P1 for use of technical notation and possible use of tree diagram to aid explanation.  M1 for spinner as described. Can be any shape provided sections are equal and it will spin around a central axis (eg, circle, regular hexagon)  B1 for example  C1 for general explanation | M |
| **8** |
| **9 a**  **b** | P(P, P) = 0.4 × 0.5 = 0.2 | 0.2 | M1  C1  A1 | 3 | M1 for correct construction of probability tree diagram  C1 for probabilities and events identified clearly  A1 cao | M |
| **3** |
| **10** | P(6, 7 or 8) = ×  = = 0.049 77… | 0.050 | M1  A1 | 2 | M1 for multiplication showing probabilities for two draws without replacement  A1 cao | M |
| **2** |
| **11** |  | P(land on 1) = P(1, 2, 3 or 4)  = =  P(land on –1) = P(5 or 6)  = =  Since  = 2 × , the counter is twice as likely to land on 1 as –1.  OR  There are twice as many possibilities for the dice to land on 1, 2, 3 or 4 than on 5 or 6 with a fair die. | M1  C1 | 2  3 | M1 for multiplications to calculate P(1) and P(–1)  C1 for explanation that there are twice as many chances oe  OR  C1 for communicating that one probability is twice the other oe | M |
| **2** |
| **12** | P(A and B) = P(A) × P(B) NOT P(A) + P(B)  or  P(A) × P(B) means P(A) and P(B)  P(A) + P(B) means P(A) or P(B) | P(5) =  P(H) =  P(5 and H) = ×  =  P (5 or H) =  +  = +  =  ≠ | M1  C1  C1 |  | M1 for use of probability notation  C1 for explanation that shows an understanding of the difference between ‘and’ and ‘or’  C1 for further explanation, example oe | M |
| **3** |
| **13** | P(pass, pass) = 0.9 × 0.6 = 0.54 | The probability that she passes both parts on the first attempt is 0.54. | M1  C1  A1 | 2 | M1 for correct construction of probability tree diagram  C1 for probabilities and events identified clearly  A1 cao | M |
| **3** |
| **14 a**  **b**  **c** | P(late) = 0.08  P(not late) = 0.92  P(early) = 0.02  P(not early) = 0.98  P(raining) = 0.3  P(not raining) = 0.7  P(on time) = 1 – P(late) – P(early)  = 1 –0.08 – 0.02  = 0.9  P(on time, not raining) = 0.9 × 0.7 = 0.63  P(raining, raining, raining) = 0.33  =0.027  P(not late five days in a row) = 0.925  = 0.6591 | P(on time, not raining) = 0.63  P(raining, raining, raining) = 0.027  P(not late five days in a row) = 0.659 | M1  M1  M1 | 2 | M1 for correct multiplication for three different events oe  M1 for correct multiplication for three same events oe  M1 for correct multiplication for five same complement events oe | M |
| **3** |
| **15** | Let the number of students in the class be x.  Number who solve problem 1 = 0.5x  Number who solve problem 2 = 0.8x  So xis the two added together less 12 as this has been counted twice  x = 0.8x + 0.5x – 12  x= 1.3x – 12  12 = 0.3x  x= 40  or  80% + 50% = 130%  so 12 represents the overcount by 30%.  = 12  x = 40 | The number of students who took the exam is 40. | P1  C1  A1 | 2 | P1 for either solving the linear equation or calculating, using the percentages from the Venn diagram  C1 for explanation as to why 12 is subtracted (or we have 30% too much)  A1 cao | H |
| **3** |

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| **16 a**  **b** | x = 0.7x + 30 – 0.3x  x – 0.7x + 0.3x = 30  0.6x = 30  x = 50 | x = 50  Own problem | P1  A1  C1  C1 | 3 | P1 for equation set up  A1 cao  C1 for clear, organised problem  C1 for relevant mark scheme | H |
| **4** |
| **17** |  | You cannot use a sample space diagram because it is a is a two-way diagram, it is two-dimensional (horizontal and vertical) and it is impossible to draw the third and fourth dimensions.  Also a probability tree diagram would be very complex. | C1  C1 | 3 | C1 for explanation of the fact that a two-way table describes two events only oe  C1 for comment on the complexity or impracticality of a tree diagram | H |
| **1** |

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| **18 a**  **b**  **c** |  | Example of a problem that can be solved by adding probabilities.  Example of a problem that can be solved by multiplying probabilities.  Example of a problem that involves both adding and multiplying probabilities. | P1  P1  B1 | 3 | P1 for clearly structured question, for example:  E.g. A bag contains 3 red, 2 yellow and 4 blue counters. One is drawn and replaced. A second is drawn.  What is the probability of a red first or a blue first?  P(R first) + P (B first) = +  =  P1 for clearly structured question, for example:  What is the probability of drawing two yellows, replacing the counter each time?  P(YY) = P(Y) × P(Y) = × =  B1 for clearly structured question, for example:  What is the probability of drawing two counters the same colour, replacing the counter each time?  P(Y, Y) + P(B, B) + P(R, R)  = (× )+ (× ) + (× )  = | H |
| **3** |
| 1. **a**   **b**  **c** | × ×=  × ×=  The number of ‘plays’ in a year is 45 × 50 = 2250.  The income is 2250 × 20p = £450.  The probability of a win on each play is  .  The expected number of wins is × 2250 = 18.75  = 19 (nearest whole number)  The expected pay-out is 19 × £5 = £95  The expected profit in one year is  £450 – £95 = £355 | P(win) =  He is incorrect; every set of three numbers has the same chance of being chosen.  £355 | M1  C1  M1  M1  M1  M1  A1 | 2  3 | M1 for multiplication of three probabilities without replacement  C1 for explanation that all numbers have the same chance of being drawn  M1 for multiplication 45 × 50 oe  M1 for multiplication 2250 × 20p oe  M1 for × 2250 oe  M1 for 19 × 5 oe  A1 £450 – £95 (ft) | H |
| **7** |
|  |  | It will help to show all nine possible outcomes and which ones give two socks of the same colour. Then the probabilities on the branches can be used to work out the chance of each outcome. | C1  P1 | 2 | P1 for clear explanation that shows awareness of nine possible outcomes (3 possible colours and then a further choice of 3), together with a comment about the diagram finding all possible combinations  P1 for use of technical notation and possible use of a probability tree diagram to aid explanation | H |
| **2** |
| **21** |  | He forgot there were now only 49 cards left in the pack. The probability of being dealt the final ace is . | C1 | 2 | C1 for comment that shows understanding that the cards had not been replaced, leaving the final ace to be chosen from 49 cards, not 52 | H |
| **1** |

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| **22** | P(picture card) =  P(four in a row) = × ××  =  = 0.0067… | 0.0067 | M1  A1 | 3 | M1 for multiplication × ××  A1 cao | H |
| **2** |
| **23** |  | Work out P(Y), P(G) and P(O).  Then P(Y) × P(yellow second), remembering both the numerator and denominator will be 1 less.  Then P(G) × P(green second), remembering both the numerator and denominator will be 1 less. Then P(O) × P(orange second),remembering both the numerator and denominator will be 1 less.  Then add together these three probabilities.  She is most likely to forget to reduce the denominator by one for the second jelly baby. | C1  C1  C1  C1 | 2  3 | C1 for stating the need to find the probabilities of each first oe  C1 for reminding about the change in numerator and denominator oe  C1 for final addition of probabilities oe  C1 for example or relevant diagram | H |
| **4** |
| **24** | Work out the probability that no two friends choose the same random number.  P(no match) =      P(match) = 1 – P(no match)  So P(match) =  = 0.743 941 472 3 | 0.74 | M1  M1  A1 | 3 | M1 for multiplication × × ×  M1 for (1 – probability of no match)  A1 for rounding and ft | H |
| **3** |
| **25 a**  **b**  **c** | Probability that they don’t have their birthday on the same day is:  Probability that they do is:  1 –  Alison is incorrect, a choice of would only give you the probability of choosing 25 days from the year and they would not be the same day. | In reality birthdays are not evenly distributed through the year. For example more babies are born in Spring. | P1  M1  C1  P1 | 2 | P1 for probability that the 25 people have birthdays on different days oe  M1 for probability that they do being 1 – probability that they don’t  C1 for clear explanation of the probability defined by oe  P1 for valid assumption that considers an uneven distribution of birthdays | H |
| **6** |
| **26 a**  **b** | Probability that they don’t is:    = 0.005 25  Probability that they do is:  1 –  = 0.994 75  1 –  – 0.5 | Assumptions made in order to start the question:  All letters are equally likely to be initial letters.  All 10 people are using the same alphabet for naming.  0.994 75 | M1  M1  M1  A1  M1 | 2 | M1 for valid assumption oe  M1 for probability that the 10 people have first names starting with the same letter oe  M1 for probability that they do being 1 – probability that they don’t  A1 ft  M1 for adaptation of calculation | H |
| **5** |