

Guidance on the use of codes for this mark scheme	
M	Method mark
A	Accuracy mark
B	Working mark
cao	Correct answer only
oe	Or equivalent
ft	Follow through

Question	Working	Answer	Mark	AO	Notes	Grade
1 a	$\frac{112}{200} \times 50\,000$	28 000 would vote for Party A.	M1	2	M1 for multiplication of total population by proportion of sample	B
	b	$28\,000 \times 0.9 = 25\,200$	This is over 50% of voters so Party A should be confident of winning.			
2	$\frac{7}{28} \times 1260 = 315$	315 students are in the sample.	M1	2	M1 for multiplication of total population by proportion of sample A1 cao	B
			A1			
3		At four different points in the concert, entrances or bars, each point to conduct the survey on approximately 100 people each, trying to ask as many males as females.	B1	2 3	B1 for explanation of general method of sampling  B1 for specific example related to the concert crowd	B
			B1			



<b>6 a</b>	$1 + 12 + 24 + 15 + 13 + 9 + 5 = 79$	79 patients	M1	3.1	M1 for addition of frequencies	B																		
	<b>b</b>	Total number of minutes = sum of (midpoint × frequency) for each class = 2754 Mean time = $\frac{2754}{79} = 34.86\dots$ minutes	<table border="1"> <tr><td>Time (minutes)</td><td>0–10</td><td>11–20</td><td>21–30</td><td>31–40</td></tr> <tr><td>Midpoint (<i>M</i>)</td><td>5</td><td>15.5</td><td>25.5</td><td>35.5</td></tr> <tr><td>Frequency (<i>f</i>)</td><td>1</td><td>12</td><td>24</td><td>15</td></tr> <tr><td><i>M</i> × <i>f</i></td><td>5</td><td>186</td><td>612</td><td>532.5</td></tr> </table>		Time (minutes)		0–10	11–20	21–30	31–40	Midpoint ( <i>M</i> )	5	15.5	25.5	35.5	Frequency ( <i>f</i> )	1	12	24	15	<i>M</i> × <i>f</i>	5	186	612
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<b>c</b>	Estimated mean = 35 minutes	<table border="1"> <tr><td>Time (minutes)</td><td>41–50</td><td>51–60</td><td>61–70</td></tr> <tr><td>Midpoint (<i>M</i>)</td><td>45.5</td><td>55.5</td><td>65.5</td></tr> <tr><td>Frequency (<i>f</i>)</td><td>13</td><td>9</td><td>5</td></tr> <tr><td><i>M</i> × <i>f</i></td><td>591.5</td><td>499.5</td><td>327.5</td></tr> </table>	Time (minutes)	41–50	51–60	61–70	Midpoint ( <i>M</i> )	45.5	55.5	65.5	Frequency ( <i>f</i> )	13	9	5	<i>M</i> × <i>f</i>	591.5	499.5	327.5	B1		B1 for appropriate rounding to whole minutes			
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<b>d</b>	Modal time = 21–30 minutes $\frac{(79 + 1)}{2} = 40$ The median is the 40th person. The 40th person is in the 31–40 group. Median time is 31–40 minutes  For the group who waited over one hour (61–70), there were 5 patients. So 74 patients were seen in one hour or less. $\frac{74}{79} = 0.9367\dots$ So 93.7% of patients saw a doctor within one hour.	Estimate mean waiting time = 35 minutes  The hospital would use the modal time.  93.7% of patients saw a doctor within one hour.	M1  M1 A1  M1  A1		M1 for mode  M1 for median A1 for correct, shortest, average waiting time  M1 for calculation of $\frac{74}{79}$ or $1 - (\frac{5}{79})$ as a percentage  A1 cao																			
			<b>10</b>																					

7 a	b	Estimate: Often: $90^\circ$ ( $\approx 25\%$ ) Very often: $75^\circ$ ( $\approx 20\%$ ) Rarely: $100^\circ$ ( $\approx 30\%$ ) Never: $75^\circ$ ( $\approx 20\%$ ) Always: $10^\circ$ ( $\approx 5\%$ )	No. It only shows proportions	M1	3	M1 for reference to proportions	B
			Summary and interpretation of available information and data	A1			
				B2			
				4			
8			The 5 minutes spent waiting is halfway between the 4-minute and the 6-minute groups. These people are in that band, but maybe no one had to wait exactly 5 minutes.	M1	3	M1 for awareness that the 5 minutes represents the midpoint of a class of grouped data, so people may have been waiting for any time between 4 and 6 minutes	B
				1			
9			Divide the frequency of the class interval by the width of the class interval to find the frequency density.	M1	3	M1 for correct method for calculation of frequency density	B
				1			
10		Kathy's mean (scores in order): $(8 + 7 + 6 + 5 + 5 + 5 + 4) \div 7 = 5.7$ Connie's mean (scores in order): $(9 + 8 + 7 + 2 + 2) \div 5 = 5.6$ Evie's mean (scores in order): $(8 + 8 + 3 + 2 + 1) \div 5 = 4.4$	Kathy would choose her mean score of 5.7.  Connie would choose her median score of 7.  Evie would choose her modal score of 8.	M1	2	M1 for calculation of all three means M1 for identification of all three modes M1 for identification of all three medians A1 for correct average identified in all three cases	M
				M1			
				M1			
				A1			
				4			

Dancer	Scores	Mean	Median	Mode
Kathy	8, 7, 6, 5, 5, 5, 4	5.7	5	5
Connie	9, 8, 7, 2, 2	5.6	7	2
Evie	8, 8, 3, 2, 1	4.4	3	8

11	<p>Working in thousands of pounds:  <math>\text{Range}_A = 86 - 18 = 70</math>  <math>\text{Range}_B = 45 - 22 = 23</math></p> <p><math>\text{Mean}_A =</math>  <math display="block">\frac{(86 + 62 + 23 + 23 + (5 \times 18))}{9}</math> <math>= 31.555\dots</math></p> <p><math>\text{Mean}_B =</math>  <math display="block">\frac{(45 + 36 + (4 \times 36) + (3 \times 22))}{9}</math> <math>= 27.888\dots</math></p>	<p>Valid advice based on the salary scales provided (see notes), for example:          Jasmin should join firm B if she is prepared to accept that the highest salary is not as high as that offered by firm A. However, the starting salary is higher and Jasmin can progress more quickly to a higher salary with firm B than with firm A. There is a greater range of salaries in firm A than in firm B.          Jasmin should join firm A if she aspires to being the boss!          Alternatively she could start with firm B and move to firm A after 7 salary increments for maximum earnings.</p>	<p>M1          M1          M1          M1          M1          A1</p>	2	<table border="1"> <thead> <tr> <th>Firm</th> <th>Range</th> <th>Mean</th> <th>Median</th> <th>Mode</th> <th>M</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>£70 000</td> <td>£31 556</td> <td>£18 000</td> <td>£18 000</td> <td></td> </tr> <tr> <td>B</td> <td>£23 000</td> <td>£27 889</td> <td>£26 000</td> <td>£26 000</td> <td></td> </tr> </tbody> </table>	Firm	Range	Mean	Median	Mode	M	A	£70 000	£31 556	£18 000	£18 000		B	£23 000	£27 889	£26 000	£26 000		<p>M1 for calculation of ranges          M1 for calculation of means          M1 for identification of medians          M1 for identification of modes          M1 for justification of either firm A or firm B          A1 for use of table or for comparison</p>
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A	£70 000	£31 556	£18 000	£18 000																				
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6																								

<b>12 a</b>		Set of grouped data with an estimated range of 26.	B1	2 3	B1 for correct example (class widths do not need to be equal), e.g. $0 \leq x < 5$ ; $5 \leq x < 25$ ; $25 \leq x < 32$ Estimated range (from midpoints) = $28.5 - 2.5$	M																															
	<b>b</b>	Set of grouped data an estimated median of 46.	B1		B1 for correct example (class widths do not need to be equal), e.g.																																
	<b>c</b>	Set of grouped data an estimated median of 22.5 and an estimated range of 62	B1 B1		<table border="1"> <tr> <th>Class</th> <th><math>0 \leq x &lt; 45</math></th> <th><math>45 \leq x &lt; 47</math></th> <th><math>47 \leq x &lt; 50</math></th> </tr> <tr> <td>Midpoint</td> <td></td> <td>46</td> <td></td> </tr> <tr> <td>Frequency</td> <td>5</td> <td>1</td> <td>5</td> </tr> <tr> <td>cf</td> <td>5</td> <td>6</td> <td>11</td> </tr> </table> <p><math>n = 11</math> hence the sixth data point is the median Estimated median (from midpoint) = 46</p>		Class	$0 \leq x < 45$	$45 \leq x < 47$	$47 \leq x < 50$	Midpoint		46		Frequency	5	1	5	cf	5	6	11															
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<b>d</b>	Set of grouped data an estimated mean of 36 (to one decimal place).	B1 B1	<table border="1"> <tr> <th>Class</th> <th><math>0 \leq x &lt; 20</math></th> <th><math>20 \leq x &lt; 25</math></th> <th><math>25 \leq x &lt; 119</math></th> </tr> <tr> <td>Midpoint</td> <td>10</td> <td>22.5</td> <td>72</td> </tr> <tr> <td>Frequency</td> <td>5</td> <td>1</td> <td>5</td> </tr> <tr> <td>cf</td> <td>5</td> <td>6</td> <td>11</td> </tr> </table> <p><math>n = 11</math> hence the sixth data point is the median Estimated median (from midpoint) = 22.5 Estimated range (from midpoints) = <math>72 - 10 = 62</math></p>	Class	$0 \leq x < 20$	$20 \leq x < 25$	$25 \leq x < 119$	Midpoint	10	22.5	72	Frequency	5	1	5	cf	5	6	11																		
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				6	<p>B1 for correct division: (sum of frequencies <math>\times</math> midpoint) <math>\div</math> (total frequency) B1 for correct example of estimated mean (ft) (class widths do not need to be equal), e.g.</p> <table border="1"> <thead> <tr> <th>Class</th> <th>Frequency (<math>f</math>)</th> <th>Midpoint (<math>m</math>)</th> <th><math>f \times m</math></th> </tr> </thead> <tbody> <tr> <td><math>0 \leq x &lt; 6</math></td> <td>0</td> <td>3</td> <td>0</td> </tr> <tr> <td><math>6 \leq x &lt; 10</math></td> <td>2</td> <td>8</td> <td>16</td> </tr> <tr> <td><math>10 \leq x &lt; 20</math></td> <td>5</td> <td>15</td> <td>75</td> </tr> <tr> <td><math>20 \leq x &lt; 30</math></td> <td>5</td> <td>25</td> <td>125</td> </tr> <tr> <td><math>30 \leq x &lt; 40</math></td> <td>9</td> <td>35</td> <td>315</td> </tr> <tr> <td><math>40 \leq x &lt; 62</math></td> <td>15</td> <td>51</td> <td>765</td> </tr> <tr> <td>Totals</td> <td>36</td> <td></td> <td>1296</td> </tr> </tbody> </table> <p>Estimated mean = <math>1296 \div 36</math></p>	Class	Frequency ( $f$ )	Midpoint ( $m$ )	$f \times m$	$0 \leq x < 6$	0	3	0	$6 \leq x < 10$	2	8	16	$10 \leq x < 20$	5	15	75	$20 \leq x < 30$	5	25	125	$30 \leq x < 40$	9	35	315	$40 \leq x < 62$	15	51	765	Totals	36		1296
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13

Median =  $\frac{n+1}{2}$  th value

Lower quartile =  $\frac{n+1}{4}$  th value

Upper quartile =  $\frac{3(n+1)}{4}$  th value

So if you have a table with 12 values these will be the 6th, 3rd and 9th values.

Order	Value	
1		
2		
3	7	Difference between 14 and 7 equals 7 as required.
4		
5		
6	10	
7		
8		
9	14	
10		
11		

These can be adapted as long as rows are added equally in each section (see example below).

Order	Value	
1		
2		
3		
4	7	Difference between 14 and 7 equals 7 as required.
5		
6		
7		
8	10	
9		
10		

B1

2

B1 for correct formula for median

M

B1

B1 for correct formula for LQ

B1

B1 for correct formula for UQ

M1

M1, for values for UQ and LQ with a difference of 7

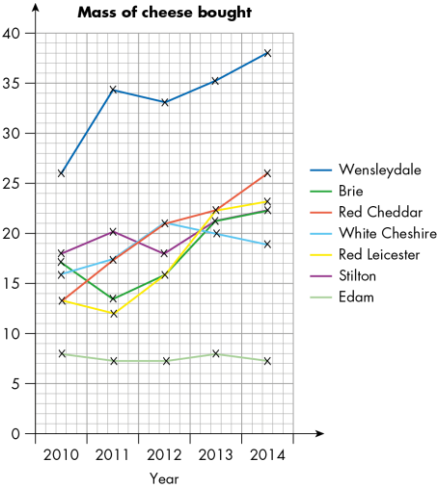
A1

A1 for explanation of difference in relation to range in this context



		<table border="1"> <tr><td>11</td><td></td><td></td></tr> <tr><td>12</td><td>14</td><td></td></tr> <tr><td>13</td><td></td><td></td></tr> <tr><td>14</td><td></td><td></td></tr> <tr><td>15</td><td></td><td></td></tr> </table>	11			12	14		13			14			15							
11																						
12	14																					
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			<b>5</b>																			
<b>14</b>		Either Harold, as he had bigger tomatoes, or Connie, as she had more tomatoes (depending on if you want lots of tomatoes or large tomatoes!).	M1 A1 <b>2</b>	2	M1 for choice of one person with justification A1 for further consideration of second person	M																
<b>15 a</b>		The statement: 'There is strong evidence to support my hypothesis' is more precise. In reality it is usually not possible to prove a hypothesis just to gather evidence to support it.	M1	2	M1 for selection of 'There is strong evidence to support my hypothesis' with explanation about practicalities of proving an hypothesis	M																
<b>bi</b>		Because you may not have gathered enough evidence.	A1		A1 for explanation of having sufficiently large sample / evidence																	
<b>ii</b>		Because you haven't gathered enough evidence or you're using a 'null' hypothesis.	A1		A1 for giving same reason / an awareness of the practical difficulties of getting all other variables equal or unchanged so that they do not affect the success or otherwise of your evidence gathering. oe																	
			<b>3</b>																			
<b>16 a</b>		Valid comparative statement such as: 'The means are very similar but there is evidence that the broadsheets use a broader range of length of words.'	B1		B1 for comparative statement oe	H																
<b>b</b>		No, it provides some evidence, but only assuming length of words is a suitable measure of difficulty. The length of words may not be the thing that readers find makes a paper hard to read.	B1		B1 for explanation that this is insufficient evidence to answer the question oe																	
<b>c</b>		For example: How long did it take to read the sample or a specific question to challenge the readers' understanding of the sample.' Could also look at the modal word length to see if there is evidence to support the	B1		B1 for a suitable further question oe																	

		broadsheet using a greater range of words, for example: Are most of the words in the tabloid four letters long?																																																					
			3																																																				
17	<p>Mean<sub>1</sub> = <math>\frac{455}{40}</math> = 11.375</p> <p>There is a difference of 0.625 so mean<sub>2</sub> is 11.375 ± 0.625. So it is either 12 or 10.75. The new total is either: 40 × 12 = 480 (increase of 25) or 40 × 10.75 = 430 (decrease of 25) By trial and improvement: 15 and 10 are reversed.</p>	The 15 and the 10 are the wrong way round.	M1 M1 M1  A1 A1	3	<table border="1"> <thead> <tr> <th>Mas s</th> <th>0 &lt; m ≤ 5</th> <th>5 &lt; m ≤ 10</th> <th>10 &lt; m ≤ 15</th> <th>15 &lt; m ≤ 20</th> <th>20 &lt; m ≤ 25</th> <th>Total s</th> </tr> </thead> <tbody> <tr> <td>freq</td> <td>4</td> <td>15</td> <td>10</td> <td>8</td> <td>3</td> <td>40</td> </tr> <tr> <td>mp</td> <td>2.5</td> <td>7.5</td> <td>12.5</td> <td>17.5</td> <td>22.5</td> <td></td> </tr> <tr> <td>m × f</td> <td>10</td> <td>112.5</td> <td>125</td> <td>140</td> <td>67.5</td> <td>455</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>freq</td> <td>4</td> <td>10</td> <td>15</td> <td>8</td> <td>3</td> <td>40</td> </tr> <tr> <td>m × f</td> <td>10</td> <td>75</td> <td>187.5</td> <td>140</td> <td>67.5</td> <td>480</td> </tr> </tbody> </table> <p>M1 for calculation of new mean M1 for calculation of new totals M1 for trial and improvement with information gathered oe A1 for correct identification of 15 and 10 A1 for table to show corrected data oe</p>	Mas s	0 < m ≤ 5	5 < m ≤ 10	10 < m ≤ 15	15 < m ≤ 20	20 < m ≤ 25	Total s	freq	4	15	10	8	3	40	mp	2.5	7.5	12.5	17.5	22.5		m × f	10	112.5	125	140	67.5	455								freq	4	10	15	8	3	40	m × f	10	75	187.5	140	67.5	480	H
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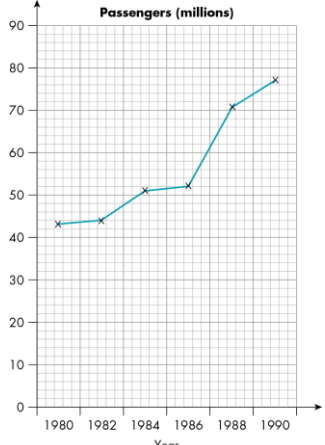
18 a		<p>The diagram chosen needs to show how the mass of each cheese varies from one year to the next. A line graph, as follows, is a good choice when there is variation over time.</p> <table border="1" data-bbox="741 240 1189 518"> <thead> <tr> <th></th> <th>Mean</th> <th>Median</th> <th>Mode</th> <th>Range</th> </tr> </thead> <tbody> <tr> <td>W</td> <td>33.2</td> <td>34</td> <td>-</td> <td>12</td> </tr> <tr> <td>B</td> <td>17.5</td> <td>17</td> <td>-</td> <td>9</td> </tr> <tr> <td>RC</td> <td>19.8</td> <td>21</td> <td>-</td> <td>13</td> </tr> <tr> <td>WC</td> <td>18.6</td> <td>19</td> <td>-</td> <td>5</td> </tr> <tr> <td>RL</td> <td>17.2</td> <td>16</td> <td>-</td> <td>11</td> </tr> <tr> <td>S</td> <td>19.8</td> <td>20</td> <td>18</td> <td>4</td> </tr> <tr> <td>E</td> <td>7.4</td> <td>7</td> <td>7</td> <td>1</td> </tr> </tbody> </table> 		Mean	Median	Mode	Range	W	33.2	34	-	12	B	17.5	17	-	9	RC	19.8	21	-	13	WC	18.6	19	-	5	RL	17.2	16	-	11	S	19.8	20	18	4	E	7.4	7	7	1	<p>M1 A1 M1 M1 A1</p>	<p>3</p>	<p>M1 for report that includes an awareness of change over time, and which cheeses are increasing and which are decreasing in popularity A1 for appropriate diagram or graph oe M1 for calculation of ranges to show which cheeses are most popular oe M1 for calculation of mean or median to show average mass of cheese purchased oe A1 for interpretation of calculations within the report</p>	H
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19		Students' diagrams, measures and reports will vary.	B1	3	B1 for report that includes an awareness of change over time and which wines are increasing and which are decreasing in popularity B1 for appropriate diagram / graph oe M1 for calculation of ranges to show which wines are most popular oe. M1 for calculation of mean, median or mode to show average number of cases of wine purchased purchased oe  A1 for interpretation of calculations within the report	H																																			
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			5																																						
20	Estimated mean = $\frac{2405}{87}$ = 27.6... minutes	From the cumulative frequency (cf) graph (some variance depending on students' reading of unmarked intervals on graph):	M1 M1 A1	2 3	M1 for identification of frequencies from cf graph M1 for identification of mid-points of classes from cf graph A1 for table to show data derived from cf graph oe	H																																			
		<table border="1"> <thead> <tr> <th>mp</th> <th>c.freq</th> <th>freq</th> <th>fxmp</th> </tr> </thead> <tbody> <tr> <td>7.5</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>12.5</td> <td>8</td> <td>8</td> <td>100</td> </tr> <tr> <td>17.5</td> <td>15</td> <td>7</td> <td>105</td> </tr> <tr> <td>22.5</td> <td>25</td> <td>10</td> <td>225</td> </tr> <tr> <td>27.5</td> <td>45</td> <td>20</td> <td>550</td> </tr> <tr> <td>32.5</td> <td>75</td> <td>30</td> <td>975</td> </tr> <tr> <td>37.5</td> <td>87</td> <td>12</td> <td>450</td> </tr> <tr> <td>Totals</td> <td>87</td> <td>86</td> <td>2405</td> </tr> </tbody> </table>	mp				c.freq	freq	fxmp	7.5	0	0	0	12.5	8	8	100	17.5	15	7	105	22.5	25	10	225	27.5	45	20	550	32.5	75	30	975	37.5	87	12	450	Totals	87	86	2405
mp	c.freq	freq	fxmp																																						
7.5	0	0	0																																						
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32.5	75	30	975																																						
37.5	87	12	450																																						
Totals	87	86	2405																																						
Estimate: 28 minutes (to the nearest minute).			A1	A1 for their estimated mean (ft) Allow range of 26–29 minutes																																					
			4																																						
21		Find the top 15% on the cumulative frequency scale, read along to the graph and read down to the marks. The mark seen will be the minimum mark needed for this top grade.	M1 A1	2	M1 for explanation of use of graph A1 for explanation of where to find the minimum grade	H																																			
			2																																						

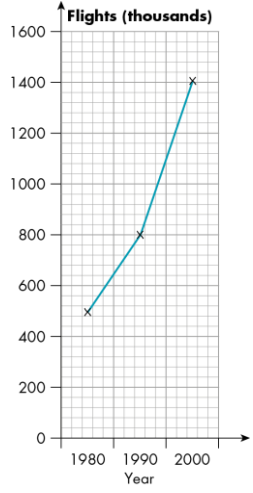
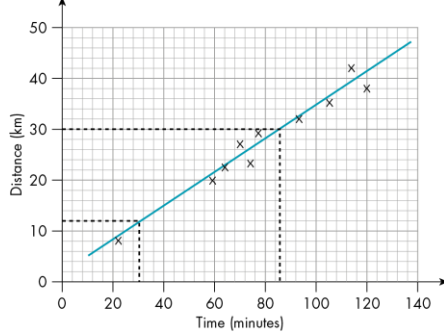
<b>22</b>	<table border="1"> <thead> <tr> <th>Class width</th> <th>fd</th> <th>f</th> </tr> </thead> <tbody> <tr> <td>20</td> <td>0.5</td> <td>10</td> </tr> <tr> <td>20</td> <td>1.5</td> <td>30</td> </tr> <tr> <td>10</td> <td>6</td> <td>60</td> </tr> <tr> <td>10</td> <td>4.5</td> <td>45</td> </tr> <tr> <td>10</td> <td>4</td> <td>40</td> </tr> <tr> <td>20</td> <td>1.5</td> <td>30</td> </tr> <tr> <td></td> <td></td> <td>215</td> </tr> </tbody> </table> <p>Frequency density (fd) = frequency (f) divided by class width  Number of students getting top grade is 10% of 215 = 21.5.  30 students got 80–100</p> $\frac{21.5}{30} = 0.7167$ <p>Class width = 20  <math>20 \times (1 - 0.716) = 5.667</math>  Mark for top grade = <math>80 + 5.667\dots</math></p>	Class width	fd	f	20	0.5	10	20	1.5	30	10	6	60	10	4.5	45	10	4	40	20	1.5	30			215	<p>The mark for the top grade is 85.7 (or 86 to the nearest integer score).</p>	M1	2 3	<p>M1 for identification of class widths and frequency densities  M1 for calculation of frequencies using <math>f = fd \times w</math>  A1 for clear table showing w, fd and f</p>	H
	Class width	fd	f																											
	20	0.5	10																											
	20	1.5	30																											
10	6	60																												
10	4.5	45																												
10	4	40																												
20	1.5	30																												
		215																												
M1	M1 for division to get 0.716 oe																													
M1	M1 for class width $\times 1 - 0.716$ oe																													
A1	A1 cao																													
		<b>6</b>																												
<b>23</b>	<p>Work out frequency density from</p> $\text{frequency} = \frac{\text{frequency}}{\text{class width}}$ <table border="1"> <thead> <tr> <th>Class width</th> <th>fd</th> <th>f</th> </tr> </thead> <tbody> <tr> <td>2</td> <td>22</td> <td>44</td> </tr> <tr> <td>2</td> <td>25</td> <td>50</td> </tr> <tr> <td>2</td> <td>11</td> <td>22</td> </tr> <tr> <td>4</td> <td>5</td> <td>20</td> </tr> <tr> <td></td> <td></td> <td>136</td> </tr> </tbody> </table> <p>20 people travel more than 4 km to church.  <math>\frac{20}{136} = \frac{5}{34} = 0.147 = 0.15</math> to 2 dp</p>	Class width	fd	f	2	22	44	2	25	50	2	11	22	4	5	20			136	<p>The probability is 0.15 (or <math>\frac{5}{34}</math>).</p>	M1	2 3	<p>M1 for calculation of frequency of 20 for class travelling over 4 km to church</p>	H						
	Class width	fd	f																											
	2	22	44																											
	2	25	50																											
2	11	22																												
4	5	20																												
		136																												
M1	M1 for $20 \div 136$ oe																													
M1	M1 for rounding to one dp																													
A1	<p>A1 cao  Notes:  Any one in 4–6 class could travel exactly 4 km to church so only consider the 8–10 class</p>																													
		<b>4</b>																												

24	<table border="1"> <thead> <tr> <th></th> <th>B</th> <th>C</th> </tr> </thead> <tbody> <tr> <td>Max</td> <td>10</td> <td>14</td> </tr> <tr> <td>Min</td> <td>4</td> <td>2</td> </tr> <tr> <td>LQ</td> <td>6</td> <td>4</td> </tr> <tr> <td>M</td> <td>7</td> <td>5</td> </tr> <tr> <td>UQ</td> <td>9</td> <td>8</td> </tr> <tr> <td>R</td> <td>6</td> <td>12</td> </tr> <tr> <td>IQR</td> <td>3</td> <td>4</td> </tr> </tbody> </table>		B	C	Max	10	14	Min	4	2	LQ	6	4	M	7	5	UQ	9	8	R	6	12	IQR	3	4	Gabriel could see either doctor, but students should provide a plausible reason, for example, Dr Ball because patients never have to wait longer than 10 minutes, whereas they may have to wait up to 14 minutes for Dr Charlton; or Dr Charlton because the average waiting time is less than for Dr Ball.	M1 B1  B1	3	M1 for interpretation of data from box plots B1 for choice of doctor with reason, e.g. average waiting time oe B1 for choice of doctor with further reason, e.g. reference to range or inter-quartile range	H
			B	C																										
Max	10	14																												
Min	4	2																												
LQ	6	4																												
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25	<table border="1"> <thead> <tr> <th></th> <th>G</th> <th>B</th> </tr> </thead> <tbody> <tr> <td>Max</td> <td>95</td> <td>95</td> </tr> <tr> <td>Min</td> <td>15</td> <td>25</td> </tr> <tr> <td>LQ</td> <td>40</td> <td>50</td> </tr> <tr> <td>M</td> <td>55</td> <td>65</td> </tr> <tr> <td>UQ</td> <td>65</td> <td>75</td> </tr> <tr> <td>R</td> <td>80</td> <td>70</td> </tr> <tr> <td>IQR</td> <td>25</td> <td>25</td> </tr> </tbody> </table>		G	B	Max	95	95	Min	15	25	LQ	40	50	M	55	65	UQ	65	75	R	80	70	IQR	25	25	There are quite a few possible correct answers, for example, boys' results have higher median and higher quartiles; or girls got lower marks than the boys, interquartile range is same for boys and girls.	M1 B1  B1	2	M1 for interpretation of data from box plots B1 for choice of either boys of girls with one justification, using their data from box plots oe B1 for choice of either boys of girls with one further justification, using their data from box plots oe	H
			G	B																										
Max	95	95																												
Min	15	25																												
LQ	40	50																												
M	55	65																												
UQ	65	75																												
R	80	70																												
IQR	25	25																												
3																														
26		Many different possibilities. Each should contain no specific data – only general data such as: 'Scarborough generally had more sunshine than Blackpool', 'Blackpool tended to have more settled weather than Scarborough' or 'Scarborough had more sunshine on any one day'.	B1  B1	2	B1 for first correct comparison between Scarborough and Blackpool  B1 for a further correct comparison between Scarborough and Blackpool	H																								
			2																											
27	<table border="1"> <thead> <tr> <th></th> <th>Box</th> <th>CF</th> </tr> </thead> <tbody> <tr> <td>Max</td> <td>90</td> <td>100</td> </tr> <tr> <td>Min</td> <td>10</td> <td>20</td> </tr> <tr> <td>LQ</td> <td>30</td> <td>58</td> </tr> <tr> <td>M</td> <td>34</td> <td>61</td> </tr> <tr> <td>UQ</td> <td>45</td> <td>66</td> </tr> <tr> <td>R</td> <td>80</td> <td>80</td> </tr> <tr> <td>IQR</td> <td>15</td> <td>8</td> </tr> </tbody> </table>		Box	CF	Max	90	100	Min	10	20	LQ	30	58	M	34	61	UQ	45	66	R	80	80	IQR	15	8	These are representations from different distributions as no data points match for measures of spread or tendency.	B1 B1	2	B1 for interpretation of data from box plots B1 for comparison of measures of spread or tendency to arrive at a 'no' answer	H
			Box	CF																										
Max	90	100																												
Min	10	20																												
LQ	30	58																												
M	34	61																												
UQ	45	66																												
R	80	80																												
IQR	15	8																												
2																														
28		The measures of central tendency are likely to be different. The range is likely to be bigger for 7 to 13 than for 12 to 13 only. The greatest value (for the tallest student) will be the same and there may be similar differences between boys and girls.	B1 B1	2	B1 for mention of comparisons of range of heights oe B1 for consideration of gender differences in height with comparison of different age ranges, for example, girls are often taller than boys in Y7 and this trend is reversed by the time they reach Y13	H																								
			2																											

29 a		Suitable statements about the distributions with justification for why the representations are from different distributions.	B1	2	B1 for comparison statements such as D1 has data for ages 18–11, which D2 does not; D2 has data for ages 30–32, which D1 does not; D1 has a positive skew so it has a low mode with a long right tail and D2 has a slight negative skew, so it has a higher mode but more consistency across a greater range oe	H	
	b	Distribution 1 is for Africa, distribution 2 is for Europe, plus observations such as: there is a peak at 21; distribution 1 is positively skewed; there is a more constant frequency across the range for distribution 2 with more women marrying older in distribution 2.	B1				B1 for observation of skewness and students' comments on and perception of possible reasons such as: women in Africa tend to marry at a younger age; European women have better health care or careers and so marry later; there is more gender equality and independent women in Europe oe
30 a		Examples such as: positive skew – income distribution	B1	2	B1 for positive skew context where there is a long tail to the right (higher values) and the bulk of the distribution is to the left (lower values) B1 for negative skew context where there is a long tail to the left (lower values) and the bulk of the distribution is to the right (higher values)	H	
	b	The box will be shifted to be in line with the bulk of the distribution. It will veer right for negative skew, left for positive and central for no skew.	B1				B1 for description of negative skew that includes a comment on the distribution being focused to the right (lower values) oe
	c	Suitable box plot for each distribution.	B1				B1 for suitable positive skew box plot
		Positive skew (long right tail, median to the left)	B1				B1 for suitable no skew box plot
	No skew	B1	B1 for suitable negative skew box plot				
	Negative skew (long left tail, median to the right)	B1	Positive skew (long right tail, median to the left)				
			6				

31 a		Examples of diagrams to illustrate changes over a ten-year period could either be number of flights or number of passengers as line graphs oe.	M1 A1	2	M1 for graph or diagram to illustrate either flights or passengers from 1980 to1990 oe B1 for clear diagram and appropriate labels	H
b		Students' research may vary, as will their diagrams. Examples of diagrams to show changes over the period 1980, 1990, 2000 could be either numbers of flights or numbers of passengers as line graphs oe.	M1 A1 A1 A1 A1 A1		M1 for graph or diagram to illustrate either flights or passengers from 1980 to 2000 oe A1 for clear diagram and appropriate labels A1 for appropriate research  A1 for their extrapolation figure for number of passengers in 2010 A1 for their extrapolation figure for number of flights in 2010	
c		 <p>Extrapolating the data in the table for the period between 1980 and 1990 gives: Passengers in 2010 – approximately 145 (million) Flights in 2010 – approximately 1400 (thousand) or 1.4 million.</p> <p>However, looking at current data on the internet, the above 2010 estimates were already being approached in 2000 (cheap flights were introduced).</p> <p>Extrapolating the later data (up to 1999) gives: Passengers in 2010 – approximately 200 (million)</p>				



		<p>Flights in 2010 – approximately 2000 (thousand) or 2.0 million.</p> 				
<p><b>32 a</b></p> <p><b>b</b></p> <p><b>c</b></p>		 <p>12 km 86 minutes</p>	<p>M1</p> <p>A1 A1</p> <p><b>3</b></p>	<p>2</p>	<p>M1 for appropriate distance–time graph</p> <p>A1 for ft answer from their graph A1 for ft answer from their graph</p>	<p>H</p>

33 a		<p>Harry may have misinterpreted the information because owning multiple TVs is more likely to be a measure of wealth rather than of health. In countries of high wealth, where people are likely to own more than one TV, the healthcare system is probably much better than in poorer countries, or nutrition is better than in poorer countries. It may also be a measure of accessibility to electricity.</p>	B1	2	B1 for clear evidence of awareness of other variables that could contribute to the results shown on the scatter graph	H
b		<p>A more likely explanation for the relationship is that people who live in a more affluent country will have more access to high-value goods, such as TVs, a better supply of electricity and better healthcare and nutrition.</p>	B1		B1 for appropriate suggestions as described	
			2			