

AQA GCSE Maths

Foundation Student Book Answers



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Chapter 1 – Number: Basic number

Exercise 1A

1	-	25, 62, 86, 151, 219, 310, 400, 501
	b	97, 357, 368, 740, 888, 2053, 4366
	С	-9,-6, -2, 0, 2, 3, 4, 8
2	2	700 401 174 117 90 65 19 2

- **2** a 700, 401, 174, 117, 80, 65, 18, 2 b 6227, 3928, 2034, 762, 480, 395, 89, 59
- 3 a Number 4 (£128 250)
 b Number 1 (£129 100)
 c £850
- a 368, 386, 638, 683, 836, 863
 b 368
 c 863
- 5 408, 480, 804, 840
- **6** 33, 35, 38, 53, 55, 58, 83, 85, 88
- 7 7045 or 7405

8	-	is < is < is <					is is is	>
9	a	975 - 985 - 983 -	+ 83 + 73 + 75	= 1 = 1 = 1	058 058 058	01	r	
	b	357 -	- 98	= 2	59			
10	a	is <				b	is	>
	С	is <				d	is	<
	-	is >				f	is	<
	g	is <				h		
	ĭ	is >				j	is	<
	k	is <				I	is	>
11	а	5	4	2	2	1	1	0

12 6 °C –2 °C –4 °C 2 °C

13
$$-4\frac{1}{2}$$
 $-\frac{1}{4}$ $+3\frac{3}{4}$ $+\frac{3}{4}$ $+\frac$

14 a 7, 8, 9, 10, 11 **b** 6, 7, 8, 9, 10 **c** 2, 3, 4, 5, 6, 7, 8

Exercise 1B

EX	ercise ID			
1	a 11 e 11 i 12	b 6 f 13 j 4	<pre>c 10 g 11 k 13</pre>	d 12 h 12 l 3
0		,		
2	a 16 e 6	b 2 f 18	c 10 g 6	d 10 h 15
	i 9	j 12	k 3	I 8
3	b 3 + 2	$\times 4 = 11$	$c 9 \div 3$) – 2 = 1
	d 9 – 4 –	-2 = 7	e 5×2) + 3 = 13
	f 5 + 2	$\times 3 = 11$	g 10 ÷ .	5 - 2 = 0
	h 10 – (4	$\div 2 = 8$	i 4×6) - 7 = 17
	j 7 + 4	$\times 6 = 31$	\mathbf{k} $(6 \div 3)$) + 7 = 9
	1 7 + 6	$\div 2 = 10$		
4	a 38	b 48	c 3	d 2
	e 5 i 54	f 14 j 7	g 20 k 2	h 19 I 7
	m 7	n 10	o 2	1 /
5	c (2+1) d No brac e (4+4) f (16-4) g No brac h (5+5) i (4+2) j No brac	kets needeo kets needeo kets needeo kets needeo kets needeo	t t	
6	a 8 e 12	b 6 f 8	c 13 g 15	d 9
	h 16	i 1	g 15	
7	No, correc	t answer is 5	5 + 42 = 47	
8	a $2+3\times4$	= 14		
		= 7 (correct		
	c $6+3\times 2$ d $7-1\times 5$	= 12 (correc	ct)	
		= 16 (correc	ct)	
	f $9-3\times 3$,	
9	a $2 \times 3 + 5$		b $2 \times (3+5)$	
	$\mathbf{c} 2+3\times 5$	= 17	d $5 - (3 - 2)$ (5 - 3) + 2	,
			(5-3) + 2 $(5+3) \div 2$	
	e $5 \times 3 - 2$	= 13 1	f $5 \times 3 \times 2$	
10	$4 + 5 \times 3 = 100$	19 2 7 2 5 5 -		

 $(4+5) \times 3 = 27$. So $4+5 \times 3$ is smaller

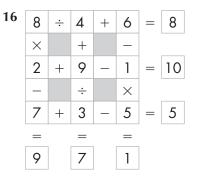
11 $(5-2) \times 6 = 18$ **12** $8 \div (5-3) = 4$

13 $10 - 3 \times 1.5$ and 10 - 1.5 - 1.5 - 1.5

15 a i
$$(4+4) \div (4+4) = 1$$

ii $(4 \div 4) + (4 \div 4) = 2$
iii $(4 + 4 + 4) \div 4 = 3$
iv $(4-4) \times 4 + 4 = 4$
v $(4 \times 4 + 4) \div 4 = 5$
b There are other ways to a

- **b** There are other ways to do these: $4 + (4 + 4) \div 4 = 6, 4 + 4 - (4 \div 4) = 7$ $(4 + 4) \times (4 \div 4) = 8, (4 + 4) + (4 \div 4) = 9$
- **c** There are other ways to do this $4 + \sqrt{4} + \sqrt{4} + \sqrt{4} = 10$



Exercise 1C

1		713 968			151 622	С	6381
2		646 75.5			826 92.92	-	3818 85.33
3	d g	450 414 4417 1828		e	563 285 3767	f	482 2892 4087
4		128 17.8			29 61.63		334 6.882
-		FFO	• 1		054		

- **5 a** 558 miles **b** 254 miles
- **6** 252
- 7 Units digit should be 6 (from 14 8)
- **8** For example: 181 27 = 154

9	а	115	b	204	C	2	294
	d	212	e	425	f		150
	g	800	h	960	i		1360
	j	1518					

10	a	294	b	370	С	288
	d	83.2	e	21.63	f	25.2
	g	16.44	h	321.5	i	30
11	a	219	b	317	С	315
	d	10.6	e	0.99	f	12.1
		25.2		1.41	•	1.44

- **12 a** 705 miles **b** £3525
- 13 a 47 miles
 - **b** Three numbers with a total of 125. First number must be less than 50, second number less than first number, third number less than second number, for example 48, 42 and 35.

14 a 119	b 96	c 144
d 210	e 210	

- **15 a** 13 **b** 37 weeks **c** 4.3 m **d** 36 **e** 45
- **16 a** 152 + 190 = 342 **b** (10 × 190) + 76 = 1976 **c** (100 × 38) + 190 = 3990

Exercise 1D

1	a –1	b -1	c 2	d −3
	e –4	f -6	g -6	h −1
	i –5	j -4	k 4	I −1
2	a −4 e −32 i −36	b -4 f -30 j -14	 c −10 g −8 k 12 	d 2 h 10 Ⅰ −101
3	a 6	b –5	c 6	d −1
	e −2	f –6	g −9	h −5
	i −80	j –7	k −1	I −47
4	a $-5 + 7 =$ b $+5 - 6 =$ c $-3 - 8 =$	- 1		

- **5 a** 7 degrees **b** -6 °C
- 6 a 2-8b 2+5-8 or 2+4-7 or 8-4-5 or 8-2-7 or 5-4-2c 2-5-7-8 d 2+5-4-7-8
- 7 500 feet

Exercise 1E

1	a 6	b 7	c 8	d 6
	e 8	f 10	g 2	h –3
	i 2	j –3	k 1	I –5
	m 3	n –4	o –3	р — 8

2	a 7	b –8	c –5	d
	e 11	f 6	g 8	h
	i -2	j —1	k –9	I
	m 5	n –9	o 8	р
3	a 3°C	b 0 °C	c −3 °C	
	d −5 °C	e −11 °C		
4	a 10 degre			
	b 7 degree			
	c 9 degree	es Celsius		
5	-9, -6, -5, -	-1, 1, 2, 3, 8		
6	a 2	b –3	c -5	
	d -7	e -10	f -20	
7	a 2	b 4	c –1	
	d -5	e -11	f 8	
8	a 13	b 2	c 5	
	d 4	e 11	f −2	
9	a -10	b –5	c -2	
	d 4	e 7	f -4	
10	a –5	b 6	c 0	
	d –6	e -2	f 212	
	g -67	h 7	i 25	

-11

8

-5

0

11 Yes. The worst case is when the temperature is just below 0 °C and the thermometer error causes a measurement of 0 + 2 = 2 °C which is below 3 °C so the alert will come on.

12 a -1, 0, 1, 2, 3
b -9, -8, -7, -6, -5
c -2, -1, 0, 1, 2, 3; -4, -3, -2, -1, 0, 1
d -12, -11, -10, -9, -8, -7;
-14, -13, -12, -11, -10, -9
e -8, -7, -6, -5, -4, -3, -2;
-5, -4, -3, -2, -1, 0, 1
f -10, -9, -8, -7, -6, -5, -4; -1, 0, 1, 2, 3, 4, 5
13 a -4 b 3 c 4 d -6
e 7 f 2 g 0 h 0
i -6 j -7 k -9 l 4
m -3 n -9 o 0
14 a +6 + +5 = 11 b +6 + -9 = -3
c +6 - -9 = 15 d +6 - +5 = 1
15 a +5 + 7 - 9 = +21
b +5 + -9 - +7 = -11
c +7 + -7 or +4 + -4
16 -3 and 8
17 -7
$$\frac{1}{2}$$
 and $-4\frac{1}{2}$

Exercise 1F 1 **a** –15 **b** -14 **c** -24 **d** 6 **e** 14 f 2 **g** -2 **h** -8 i -4 **j** 3 **k** -24 **I** -10 **m**–18 **o** 36 **p** -4 **n** 16 **s** 7 t 25 **q** -12 **r** -4 **u** 18 **v** -8 **w** -45 **y** -40 **x** 3 2 **a** -9 **b** 16 **c** -3 **d** -32 **e** 18 18 **g** 6 **h** –4 f i 20 **i** 16 **k** 8 -48 **p** 0 **m** 13 **n** -13 **o** -8 **q** 16 **r** -42 **s** 6 t 1 **u** -14 **v** 6 **w** -4 **x** 7 **y** 0 **a** -2 3 **b** 30 **c** 15 **d** -27 **e** -7 4 **a** 4 **b** -9 **c** -3 **d** 6 **e** -4 **b** 3 5 **a** -9 **c** 1 6 **a** 16 **b** -2 **c** -12 **a** 24 7 **b** 6 **c** -4 **d** -2 8 For example: $1 \times (-12)$, -1×12 , $2 \times (-6)$, $6 \times (-2), 3 \times (-4), 4 \times (-3)$ 9 For example: $4 \div (-1)$, $8 \div (-2)$, $12 \div (-3)$, $16 \div (-4), 20 \div (-5), 24 \div (-6)$ **10** a 21 **b** -4 **c** 2 **d** -16 **e** 2 f -5 **g** –35 **h** -17 **i** -12 **k** 45 **I** -2 **j** 6 **p** -36 **o** -7 **m** 0 **n** -1 **q** 9 **r** 32 **s** 0 t -65 **11 a** -12 **b** 12 degrees $\mathbf{c} \quad 3 \times -6$ **12** -5×4 , 3×-6 , $-20 \div 2$, $-16 \div -4$ **c** 21 13 a 16 **b** 41 **d** 64 **Exercise 1G a** 12 138 **b** 45 612 c 29 988 1 **d** 20 654 **e** 51 732 f 25 012 **g** 19 359 **h** 12 673 i 140 224 **j** 92 851 **k** 520 585 **I** 78 660 3500 2 3 No, 62 pupils cannot get in 4 Yes, he walks 57.6 km

- 5 Yes, 1 204 000 letters
- 6 5819 litres
- 7 No, she raised £302.40

Exercise 1H

- 1 a 25 **b** 15 **c** 37 e 27 f 48 **d** 43 **g** 53 **h** 52 i 32 **k** 37 rem 15 25 rem 5 i 57 **m** 34 rem 11 **n** 54 rem 9 o 36 rem 11 p 17 rem 4 **q** 23 **r** 61 rem 14 t 27 rem 2 s 42
- **2** 68
- **3** 38
- 4 4 months
- 5 34 hours
- 6 45p
- 7 a £46.75
 - **b** 13 weeks
- 8 An odd number divided by an even number cannot give a whole number
- **9 a** 64 **b** 22 **c** 22

Exercise 11

1	a 89.28	b 298.39	c 66.04
	d 167.98	e 2352.0	f 322.4
	g 1117.8	h 4471.5	i 464.94
	j 25.55	k 1047.2	I 1890.5
2	a £224.10	b £223.75	c £29.90
3	$5 \times 7 = 35$		
4	£54.20		

5 a £120.75 b £17 – £3.45 = £13.55

Review questions

- 1 a £1505
 - **b** 19 people
- 2 Murray did the addition first, Harry did the multiplication first.

- a Adam has calculated 5 × 2 instead of 5², Bekki has added 3 to 5 first, instead of doing the power first.
 b 26
- **4 a** -2 °C, -1 °C, 0 °C, 1 °C
 - **b** 3 degrees
- 5 i Any number between -196 °C and -210 °C, e.g. -200 °C
 - ii Any number over -196 °C, e.g. -10 °C or any positive number
 iii Any number below -210 °C, e.g. -250 °C
- 6 answer in the region of £7.67 to £8
- 7 DVD, jeans and pen
- 8 Pack of 8 at £0.625 each
- 9 a £49.90b Small, so that all four children can have an ice cream (cost £4.80)
- **10** Yes. She only needed 8 paving stones.
- **11** $2.5 \times 8.4, 5 \times 4.2, 10 \times 2.1 = 21$
- 12 £133.05
- **13 a** £141.75 **b** £119.25
- **14 a** 7542 **b** 2457 **c** 27 × 2 = 54

Chapter 2 – Geometry and measures: Measures and scale drawings

Exercise 2A

- a 26 cm, 1.5 kg. Check individual answers.
 b-j Check individual answers
- 2 The 5 metre ladder, since his height is about 175 cm and the lamp post will be about 525 cm.
- 3 Metres and centimetres are too small as units; needs to be a large unit as this is a large distance.

4	а	3400 mm	b	135 mm	С	67 cm
	d	7030 m	e	2400 ml	f	590 cl
	g	84 ml	h	5200 l	i	3750 kg
	Ĵ	0.000 94 l	k	15 200 g	I	0.19 ml

5	а	1.25 m	b	8.2 cm	С	0.55 m
	d	2.1 km	e	4.2 kg	f	5.75 t
	g	2.58 l		3.4 I		0.6 t
	j	63 cl	k	35 cm^3	I	1.035 m ³

- 6 He should choose the 2000 mm \times 15 mm \times 20 mm.
- 7 1 000 000
- **8 a** 1 000 000 **b** 1 000 000 000 000

Exercise 2B

d g j	24 in 80 oz 40 pt 30 ft 70 lb	e h k	12 ft 56 lb 48 in 64 oz 12 yd	f i I	3520 yd 6720 lb 36 in 5 ft 224 oz
d g j	5 miles 8 ft 2 lb 63 360 in 10 st	e h k	120 pt 7 st 5 yd 8 lb 3 miles	f i I	5280 ft 7 gal 5 tons 9 gal 35 840 oz

- 3 The 32-ounce bag
- 4 4 014 489 600 in²
- a miles, feet, ounces, gallonsb 108 inches
 - **c** 3 gallons

Exercise 2C

1	a 20 cm	b 13.2 lb	c 48 km
	d 67.5 l	e 2850 ml	f 10 gal
	g 12 in	h 50 miles	i 5 kg
	j 3 pints	k 160 km	l 123.2 lb
	m 180 l	n 90.9 kg	o 1100 yd
	p 30 cm	q 6.4 kg	r 90 cm

- 2 ton
- 3 metre
- **4 a i** 1000 g **ii** 1 kg **b i** 4500 g **ii** 4.5 kg
- **5 a** 135 miles **b** 50 mph **c** 2 h 42 min
- 6 4 hours 10 minutes
- 7 2770 in³

Exercise 2D

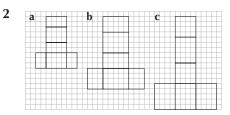
- 1 a Onions: 40 m \times 10 m; Soft fruits: 50 m \times 10 m; Apple trees: 20 m \times 20 m; Lawn: 30 m \times 20 m; Potatoes: 50 m \times 20 m
 - b Onions: 400 m²; Soft fruit: 500 m²; Apple trees: 400 m²; Lawn: 600 m²; Potatoes: 1000 m²
- **2 a** 33 cm **b** 9 cm
- 3 $\mathbf{a} \ 6\mathbf{m} \times 6\mathbf{m}$ $\mathbf{b} \ 8\mathbf{m} \times 2\mathbf{m}$ $\mathbf{c} \ 4\mathbf{m} \times 3\mathbf{m}$ $\mathbf{d} \ 4\mathbf{m} \times 6\mathbf{m}$ $\mathbf{e} \ 6\mathbf{m} \times 4\mathbf{m}$ $\mathbf{f} \ 3\mathbf{m} \times 2\mathbf{m}$
- 4 a Student's scale drawingb 39 plants (the edge is about 19 m)
- 5 a 15 km b 9 km c 12 km d 13.5 km e 7.8 km f 5.4 km
- 6 a On the map, Carlisle to Scarborough is 5.8 cm, so 1 cm represents 232 × 100000 / 5.8 = 4000000
 - **b i** 176 km **ii** 66 km
- 7 a 80 km b 70 km c 122 km
- **8 d** 1:600
- 9 a i 160 miles ii 310 miles

Exercise 2E

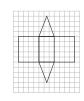
- 1 Bicycle about 2 m, bus about 10 m, train about 17 m
- 2 Height about 4 m, length about 18 or 19 m
- 3 a About 4 m
 b About 5 m
 c About 5.5 m
- 4 About 9 m; the ratio of Joel's height in the photograph to his real height must be the same as the ratio of the height on the statue in the photograph to its actual height
- 5 Assuming the man's height is about 1.8 metres, the T. Rex height is about 4 times the height of the man and 4×1.8 is 7.2 m. So yes, Ben's estimate of the height is correct. The length of T. Rex looks about 5 times the height of the man. $5 \times 1.8 = 9$ m, so Ben has overestimated the length of the T. Rex, but not by much.

Exercise 2F

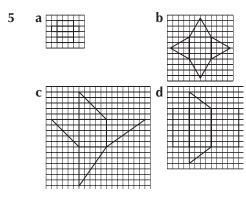
1 A, C, D



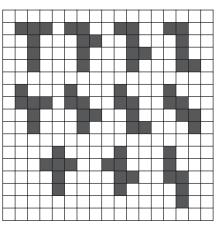
3 Yes. For example, Jenny could make it from a card 10 cm × 15 cm



4

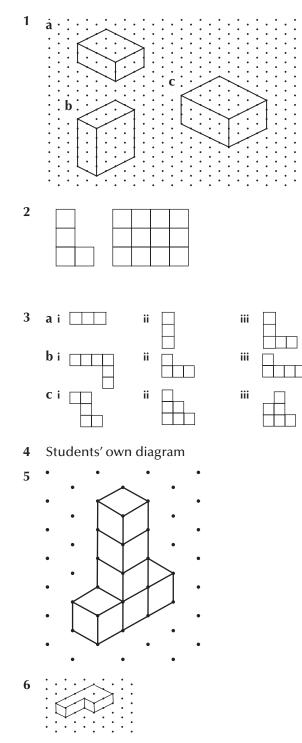


6

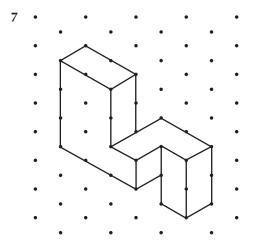


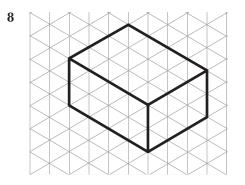
- $7 \quad a and b$
- 8 The length and height of the net needs to be at least 6.5 cm + 5 cm + 6.5 cm = 18 cm, so a card 15 cm by 15 cm is too small.

Exercise 2G



b She could be correct as 4 bricks could be put together to form a 2 cm by 12 cm block, 4 such blocks creates the bottom layer of bricks almost filling the base of 12 cm \times 9 cm, making 4 \times 4 =16 bricks in a layer. There will be 5 such layers, making 5 \times 16 = 80 bricks, leaving a 1 cm \times 12 cm \times 5 cm gap at the end of the box. You can put two of the blocks sideways into this space, giving 8 extra bricks and a total of 88 bricks.



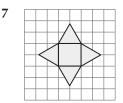


Review questions

1

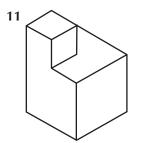
The length of a garden	metres
The mass of a puppy	kilograms
The length of a brick	centimetres

- **2 a** 40 000 metres **b** 25 miles
- **3 a i** Kilometres **ii** Litres **b i** 90 mm **ii** 3 kg
- 4 And rew is correct as $130 \times \frac{5}{8} = 81.25$
- **5 a** 1 m **b** 2.82 m
- **6 a** 160 mm **b** 150 m



- 8 Centimetres are too small and this distance is an approximation of a large distance and so needs to be a large unit such as kilometres.
- 9 a Seven and a half milesb 2.3 kg potatoes, 225 grams of butter, 2.3 litres of milk

10												
	-			-								
			_	_								
		Fro	nt e	evo	itio	h	Si	de	elev	rati	on_	
			\vdash	-								
			Plar									



Chapter 3 – Statistics: Charts, tables and averages

Exercise 3A

a			
Goals	0	1	2
Frequency	6	8	4

- **b** 1 goal c 22
- 2

1

l i						
Score	1	2	3	4	5	6
Frequency	5	6	6	6	3	4

3

2

b 30 c Yes, frequencies are similar.

3 a/b

Temperature (°C)	Frequency
14–16	5
17–19	10
20–22	8
23–25	5
26–28	2

c 17–19 °C

d Getting warmer in the first half of the month and then getting cooler towards the end.

a/b 4

Height(cm)	Frequency
151–155	2
156–160	5
161–165	5
166–170	7
171–175	5
176–180	4
181–185	3
186–190	1

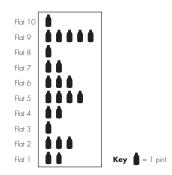
- c 166–170 cm
- a Observation 5
- **b** Sampling d Sampling
- c Observation e Experiment
- g Experiment
- f Observation

- 6 Draw a tally chart with class intervals 1–10, 11-20, 21-30, 31-40, 41-50 and 51-60. Then complete a grouped frequency table from the tally chart.

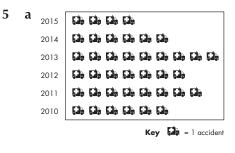
The class intervals overlap as the ages 7 20, 30, 40 and 50 are in two different class intervals

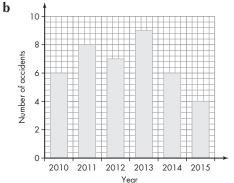
Exercise 3B

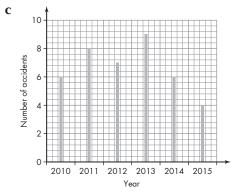
1



- 2 a May 9 h, Jun 11 h, Jul 12 h, Aug 11 h, Sep 10 h
 - **b** July **c** Visual impact, easy to understand.
- 3 a Simon **b** £330
 - **c** Difficult to show fractions of a £ symbol.
- 4 a Swimming **b** 74
 - c a better visual impact and easier to read the frequencies
 - d No. It may not include people who are not fit or not interested in sport.





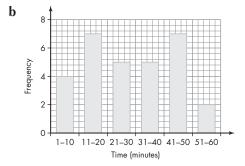


d Use the pictogram because an appropriate symbol makes more impact.

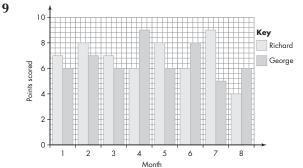
6

а

Time (min)	Frequency
1–10	4
11–20	7
21–30	5
31–40	5
41–50	7
51–60	2



- c Some students live close to the school and some live a good distance away and probably travel to school by bus.
- 7 Yes, in most cities. If you double the minimum temperature each time, it is very close to the maximum temperature.
- 8 The bar chart is misleading because the temperature axis does not start at zero.



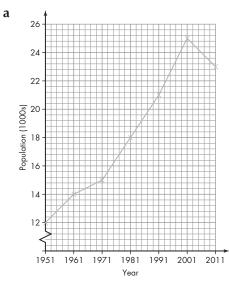
- **10 a** 102 **b** 16 **c** 42
- **11** £88.80

Exercise 3C

2

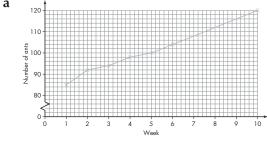
 1
 a
 Tuesday, 52p
 b
 2p

 c
 Friday
 d
 £90

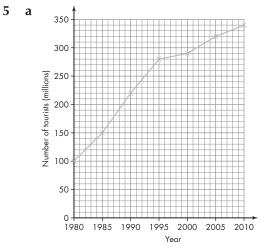


- **b** about 16 500
- c 1991 and 2001
- **d** No; do not know the reason why the population started to decrease after 2001
- 3 All the temperatures were higher than 20 degrees.

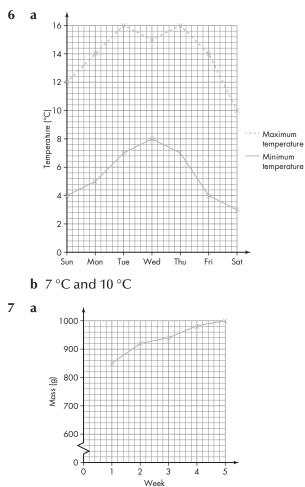








- **b** About 60 million
- **c** 1985 and 1990
- d e.g. the trend in tourism is rising over the 30 year period. This is probably because holidays have become cheaper and the rise in popularity of package holidays



b It is not possible to predict the trend as the puppy's mass is likely to level out.

Exercise 3D

1	a 4	b	48		c –1		
	d $\frac{1}{4}$	e	no mode	•	f 3.21		
2	a red	b	sun	С	β	d	М

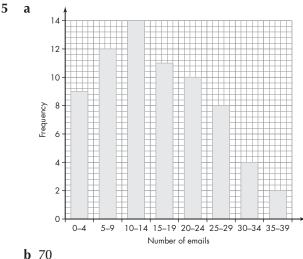
a 32 **b** 6 **c** no

d no; boys generally take larger shoe sizes

4 a 5

3

b no; more than half the class got a higher mark



- **b** 70
- **c** 24
- d cannot tell; know only that 9 households had between 0 and 4 emails
- **e** 10–14
- 6 a 28
 - **b** i brown ii blue iii brown
 - c Both students had blue eyes.
- 7 a May lose count.
 b Put in a table, or arrange in order
 c 4
- 8 The mode will be the most popular item or brand sold in a shop.

Exercise 3E

1 a 5 **b** 33 **c** $7\frac{1}{2}$ **d** 24 **e** $8\frac{1}{2}$ **f** 0 **g** 5.25

2 a £2.20 **b** £2.25

c median, because it is the central value

- **3 a** 5 **b i** 15 **ii** 215 **iii** 10 **iv** 10
- 4 a 13 years, Amina
 - **b** 162 cm, Dolly
 - c 46 kg, Grace
 - **d** Amina, because she is closest to the 3 medians
- 5 A median of £15 does not take into account the large payment of the £200 so is in no way representative.
- 6 a Possible answer: 11, 15, 21, 21 (one below or equal to 12 and three above or equal)
 - b Any four numbers higher than or equal to 12, and any two lower or equal to 12c Eight, all 4 or under
- 7 12, 14, 14, 16, 20, 22, 24, or 12, 14, 14, 16, 18, 20, 24 or 12, 14, 14, 16, 18, 22, 24

21 b	16
Mark	Frequency
12	1
13	3
14	4
15	3
16	6
17	3
18	1
	Mark 12 13 14 15 16 17

d There are 21 students altogether, so the median is the 11th mark when the marks are put in order.
 There are 11 values up to a mark of 15,

so the median is 15.

Exercise 3F

8

1	a 6 d 1.57	b 24 e 2	c 45
2	a 55.1 d 44.9	b 324.7 e 2.3	c 58.5
3	a 61 d Blake	b 60 e 2	c 59

- **4** 42 min
- **5 a** £200 **b** £260 **c** £278
 - d Median, because the extreme value of £480 is taken into account when calculating the mean and the mode would be too small to represent the data.

- **6 a** 35 **b** 36
- **7** a 6
 - **b** 16; all the numbers and the mean are 10 more than those in part **a**
 - **c i** 56 **ii** 106 **iii** 7
- 8 Possible answers: Speed Kath, James, John, Joseph; Roberts – Frank, Jim, Helen, Evie.
- **9** 36
- **10** 24

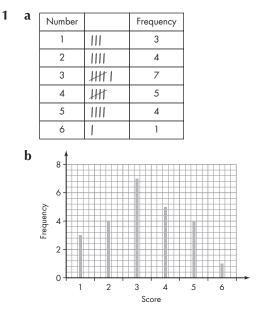
Exercise 3G

- **1 a i** Mode 3, median 4, mean 5 **ii** 6, 7, 7¹/₂ **iii** 4, 6, 8
 - b i Mean: balanced data
 ii Mode: 6 appears five times
 iii Median: 28 is an extreme value
- 2 a i 29 ii 28 iii 27.1 b The mean as it is balanced data
- 3 a Mode 73, median 76, mean 80b The mean, because it is the highest average
- 4 a Mean takes all marks into accountb Median avoids any extreme amounts
 - **c** Mode easy to find
 - **d** Median avoids any extreme heights
 - e Mode non numerical data
 - f Mean takes all masses into account
- 5 Yes, mode is 31, median is 31, and mean is $31\frac{1}{2}$; all are close to the stated average.
- 6 a i £20 000 ii £28 000 iii £34 000
 - **b** i The 6% rise, because it gives a greater increase in salary for the higher paid employees.
 - ii 6% increase: £21 200, £29 680, £36 040;
 £1500 pay rise: £21 500, £29 500,
 £35 500
- 7 a Median b Mode c Mean
- Tom mean, takes all scores into account; David – median, avoids the extreme scores; Mohammed – mode, the two highest scores
- **9** The boss chose the mean while the worker chose the mode.

Exercise 3H

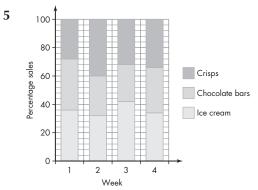
- 1 a 7 b 26 c 5 d 2.4 e 7
- a 5°, 3°, 2°, 7°, 3°
 b Variable or inconsistent weather over England
- 3 a £31, £28, £33 b £8, £14, £4 c Not particularly consistent
- 4 a 82 and 83 b 20 and 12
 c Shona, because the ranges show that her scores are more consistent
- 5 **a i** 5 min and 4 min **ii** 9 min and 13 min
 - **b** Number 50, because the times are more consistent
- 6 a Isaac, Oliver, Andrew, Niamh, Zoe, Jake and Zac
 - **b** For example: 70 cm to 90 cm
- 7 **a** The teachers because they have a high mean and students could not have a range of 20.
 - **b** Year 11 students as the mean is between 15 and 16 and the range is 1.
- 8 For example: a 1, 6, 6, 6, 6 b 2, 5, 5, 6, 7

Review questions



2 a i 75 minutes b i 110 minutes ii 80 minutes ii 140 minutes

- c on average Josh spent more time on his computer, but Hannah's times were more consistent.
- 3 a 84 cm b 73 cm c 70 cm
 d the median, avoids the extreme height of 43 cm
- 4 The modal age of 16, as most of the team are this age



6 The vertical scale does not start at zero, the horizontal scale is not linear, no £ sign for sales, no information to explain what it is about

7 a 12 **b** 11 **c** 11

8 11.6

Chapter 4 – Geometry and measures: Angles

Exercise 4A

1	a 48°	b 307°	c 108°
	d 52°	e 59°	f 81°

- **2** a 82° b 105° c 75°
- 3 No, as $45^{\circ} + 125^{\circ} = 170^{\circ}$ and for a straight line it should be 180°
- **4 a** $x = 100^{\circ}$ **b** $x = 110^{\circ}$ **c** $x = 30^{\circ}$
- **5 a** $x = 55^{\circ}$ **b** $x = 45^{\circ}$ **c** $x = 12.5^{\circ}$
- **6 a** $x = 34^{\circ}, y = 98^{\circ}$ **b** $x = 70^{\circ}, y = 120^{\circ}$ **c** $x = 20^{\circ}, y = 80^{\circ}$
- 7 $6 \times 60^\circ = 360^\circ$; imagine six of the triangles meeting at a point
- 8 $x = 35^{\circ}$, $y = 75^{\circ}$; $2x = 70^{\circ}$ (opposite angles), so $x = 35^{\circ}$ and $x + y = 110^{\circ}$ (angles on a line), so $y = 75^{\circ}$

Exercise 4B

1		70° 75°	b 50° f 109°	c80°d60°g38°h63°
2	С	No, total No, total Yes, tota	l is 170°	 b Yes, total is 180° d Yes, total is 180° f No, total is 170°
3		80° 43°	b 67° e 10°	c 20° f 1°

- 4 a-c Students' own drawings d 180°
- 5 a 60° b Equilateral triangle c Same length
- 6 a 70° each b Isosceles triangle c Same length
- **7 a** 109° **b** 130° **c** 135°
- **8** 65°
- 9 Joe is not correct as DFE = 30° , DEF = 75° hence angle D = $180^\circ - 105^\circ = 75^\circ$ but Hannah is correct as FED = FDE = 75°
- **10** $a = 35^{\circ}$ (angles in a triangle) because the other angles in the triangle are 65° (angles on a line) and 80° (opposite angles) giving a total of 145, this subtracted from the 180 degrees in a triangle leaves the answer of 35. As *a* is less than 90°, it is acute.
- 11 Missing angle = y, $x + y = 180^{\circ}$ and $a + b + y = 180^{\circ}$ so x = a + b
- **12** 32°
- **13** 72°

Exercise 4C

- **1c** $2, 2 \times 180^{\circ} = 360^{\circ}$
- **2c** 3, $3 \times 180^{\circ} = 540^{\circ}$
- 3c 4, $4 \times 180^{\circ} = 720^{\circ}$

4	Shape	Number of sides	Triangles	Angle sum
	triangle	3	1	180°
	quadrilateral	4	2	360°
	pentagon	5	3	540°
	hexagon	6	4	720°
	heptagon	7	5	900°
	octagon	8	6	1080°
	nonagon	9	7	1260°
	decagon	10	8	1440°

Exercise 4D

1		90° 80°		150° 77°			80° 131°
2	С	No, tot No, tot Yes, tot	al is 3	50°	d	No,	total is 360° total is 370° total is 360°
3		100° 40°		67° 40°		-	120° 1°
4	a	90°	b Re	ctang	le	С	Yes, square
5		120° 136°		170° 149°		-	125° 126°
6	60	$0^{\circ} + 60^{\circ}$	+ 120°	+ 120)° +	120	$^{\circ} + 240^{\circ} = 720^{\circ}$
-		2000	4		h	20	00 4

- 7 $y = 360^{\circ} 4x$; $2x + y + 2x = 360^{\circ}$, $4x + y = 360^{\circ}$, so $y = 360^{\circ} - 4x$
- 8 $x = 40^{\circ}$, smallest angle = 60°

Exercise 4E

1	Regular polygon	Number of sides	Interior angle sum	Each interior angle
	octagon	8	1080°	135°
	nonagon	9	1260°	140°
	decagon	10	1440°	144°

2	Regular polygon	Number of sides	Interior angle	Exterior angle
	square	4	90°	90°
	pentagon	5	108°	72°
	hexagon	6	120°	60°
	octagon	8	135°	45°
	nonagon	9	140°	40°
	decagon	10	144°	36°
~		•• •	*** 1000	

3	а	i	45°	ii	8	iii	1080°
	b	i	20°	ii	18	iii	2880°
	С	i	15°	ii	24	iii	3960°
	d	i	36°	ii	10	iii	1440°
4	а	i	172°	ii	45	iii	7740°
4		-	172° 174°		45 60		7740° 10 440°
4	b	i		ii		iii	

- 5 a Exterior angle is 7°, which does not divide exactly into 360°
 - b Exterior angle is 19°, which does not divide exactly into 360°

- c Exterior angle is 11°, which does not divide exactly into 360°
- d Exterior angle is 70°, which does not divide exactly into 360°
- 6 a 7° does not divide exactly into 360°
 - **b** 26° does not divide exactly into 360°
 - c 44° does not divide exactly into 360°
 - d 13° does not divide exactly into 360°
- 7 $x = 45^{\circ}$, they are the same, true for all regular polygons
- 8 Three are 135° and two are 67.5°
- 9 48°; $\frac{1440^\circ 5 \times 240^\circ}{-5}$
- **10** 10
- **11** 72°, 72°, 108°, 144°, 144°
- **12** 93°

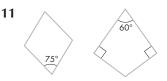
Exercise 4F

1	a d		b <i>f</i> e <i>f</i>	c f	d e
2	a	40°			
	b	$b=c=70^\circ$			
	С	$d = 75^{\circ}, e =$	$f = 105^{\circ}$		
	d	$g = 50^{\circ}, h =$	<i>i</i> = 130°		
	e	j = k = l = 7	0°		
	f	$n = m = 80^{\circ}$))		
	g	$a = 50^{\circ}, b =$	= 130°		
	h	$c = d = 65^{\circ}$	$e = f = 115^{\circ}$		
	i	$g = i = 65^{\circ}$,	$h = 115^{\circ}$		
	j	$j = k = 72^{\circ}$,	$l = 108^{\circ}$		
		m = n = o =	*		
	I	q = r = s = r	125°		

- **3 a** $a = 95^{\circ}$ **b** $b = 66^{\circ}, c = 114^{\circ}$
- 4 **a** $x = 30^{\circ}, y = 120^{\circ}$ **b** $x = 25^{\circ}, y = 105^{\circ}$ **c** $x = 30^{\circ}, y = 100^{\circ}$ **d** $x = 50^{\circ}, y = 110^{\circ}$ **e** $x = 25^{\circ}, y = 55^{\circ}$ **f** $x = 20^{\circ}, y = 140^{\circ}$
- 5 290°; *x* is double the angle allied to 35°, so is $2 \times 145^{\circ}$
- 6 $a = 66^{\circ}$; angle BDC = 66° (angles in a triangle = 180°) and *a* is the corresponding angle
- 7 Angle PQD = 64° (alternate angles), so angle DQY = 116° (angles on a line = 180°)
- 8 Use alternate angles to see *b*, *a* and *c* are all angles on a straight line, and so total 180°
- **9** Third angle in triangle equals *q* (alternate angle), angle sum of triangle is 180°

Exercise 4G

- **1 a** *a* = 110°, *b* = 55° **b** *c* = 75°, *d* = 115° **c** *e* = 87°, *f* = 48°
- a a = c = 105°, b = 75° b d = f = 70°, e = 110°
 c g = i = 63°, h = 117°
- 3 **a** $a = c = 105^{\circ}, b = 75^{\circ}$ **b** $d = f = 93^{\circ}, e = 87^{\circ}$ **c** $g = i = 49^{\circ}, h = 131^{\circ}$
- **4 a** *a* = 135°, *b* = 25° **b** *c* = *d* = 145° **c** *e* = f = 94°
- **5 a** $a = 58^{\circ}, b = 47^{\circ}$ **b** $c = 141^{\circ}, d = 37^{\circ}$ **c** $e = g = 65^{\circ}, f = 115^{\circ}$
- **6 a** 65° **b** 60° **c** 68°
- 7 both 129°
- 8 Marie is correct as a rectangle is a special form of parallelogram with all angles = 90°
- **9** a 65°
 - **b** Trapezium, angle BAD + angle ADC = 180° and angle ABC + angle BCD = 180°
- **10** 135°



12 A trapezium; angles add up to 10x, two angles x and 4x = 2x + 3x, the other pair of angles. Hence each pair adds up to 180 (since $2 \times 180 = 360$). Hence two pairs of allied angles, hence a trapezium. Alternatively you could have found that x = 36 which will give the same result.

Exercise 4H

- **1 a** 110°, 12.6 km **b** 250°, 4.5 km
 - c 091°, 11.8 km d 270°, 8.4 km
 - e 130°, 7.2 km f 180°, 4.2 km
- 2 Students' sketches
- 3 a Sketch
 - **b** D is due south of B and B is east of A, so A must be west of D. A bearing to the west will be greater than 180°
- **4 a** 090°, 180°, 270° **b** 000°, 270°, 180°
- **5 a** 250° **b** 325° **c** 144°

- **6 a** 045° **b** 286°
 - c Measure the distance from X to Y and divide 15 by this to find the scale of the map. Then measure the distance from Y to P and multiply by the scale factor.
- **7 a** 900 m **b** 280°
 - **c** angle NHS = 150° and HS = 3 cm
- **8** 108°
- **9** 255°
- 10 9.2 km

Review questions

1 16°

2

- **a** i 115° ii opposite angles are equal and the angle opposite to *x* is 180 - 65
- **b** the angles do not add up to 360°
- **3 a** 50° **b** 32.5°
- 4 $3 \times 180 = 540^{\circ}$ A five-sided shape can be split into three triangles hence 3×180
- **5** 150°
- 6 angle TQP = 37° , alternate angles, PTQ = 180 (29 + 37) = 114 angles in a triangle, QTS = 180 114, angles on a line, = 66.
- **7** 333°
- 8 $360 \div 8 = 45^\circ$, exterior angle formula is <u>360</u> number of sides
- **9** $180 (360 \div 6) = 120^{\circ}$
- **10** Selvi might be correct. You will need to draw one example showing this is not a kite, and one example showing that this could be a kite
- **11 b** 12.4 km

Chapter 5 – Number: Number properties

Exercise 5A

- 1
 a
 3, 6, 9, 12, 15
 b
 7, 14, 21, 28, 35

 c
 9, 18, 27, 36, 45
 d
 11, 22, 33, 44, 55

 e
 16, 32, 48, 64, 80
- a 254, 108, 68, 162, 98, 812, 102, 270
 b 111, 255, 108, 162, 711, 615, 102, 75, 270
 c 255, 615, 75, 270
 d 108, 162, 711, 270

- a 72, 132, 216, 312, 168, 144
 b 161, 91, 168, 294
 c 72, 102, 132, 78, 216, 312, 168, 144, 294
- 4 a 98 b 99 c 96 d 95 e 98 f 96
- **5 a** 1002 **b** 1008 **c** 1008
- 6 No, 50 is not a multiple of 6.
- 7 4 or 5 (as 2, 10 and 20 are not realistic answers)
- **8 a** 18 **b** 28 **c** 15
- **9** 66
- 10 5 numbers: 18, 36, 54, 72, 90
- **11 a** 1, 2, 5, 10 **b** 1, 2, 3, 5, 6, 10, 15, 30 **c** 1, 2, 4, 5, 10, 20, 25, 50, 100 **d** Any one of 60, 72, 84, 90, 96

Exercise 5B

3

- 1
 a
 1, 2, 5, 10
 b
 1, 2, 4, 7, 14, 28

 c
 1, 2, 3, 6, 9, 18
 d
 1, 17

 e
 1, 5, 25
 f
 1, 2, 4, 5, 8, 10, 20, 40

 g
 1, 2, 3, 5, 6, 10, 15, 30
 h
 1, 3, 5, 9, 15, 45
 i
 1, 2, 3, 4, 6, 8, 12, 24

 j
 1, 2, 4, 8, 16
- **2** 8 ways (1, 2, 3, 4, 6, 8, 12, 24 per box)
 - **a** 1, 2, 3, 4, 5, 6, 8, 10, 12, 15, 20, 24, 30, 40, 60, 120 **b** 1, 2, 3, 5, 6, 10, 15, 25, 30, 50, 75, 150 c 1, 2, 3, 4, 6, 8, 9, 12, 16, 18, 24, 36, 48, 72, 144 **d** 1, 2, 3, 4, 5, 6, 9, 10, 12, 15, 18, 20, 30, 36, 45, 60, 90, 180 e 1, 13, 169 **f** 1, 2, 3, 4, 6, 9, 12, 18, 27, 36, 54, 108 **g** 1, 2, 4, 7, 14, 28, 49, 98, 196 **h** 1, 3, 9, 17, 51, 153 i 1, 2, 3, 6, 9, 11, 18, 22, 33, 66, 99, 198 j 1, 199 a 55 **b** 67 c 29 **d** 39 e 65 f 80 g 80 **h** 70 i 81 i 50 **a** 2 **b** 2 **c** 3 **d** 5 **f** 3 **e** 3 **h** 5 **g** 7 i 10 i 11
- 6 4 in each layer, which is a 2 × 2 square
- 7 It does not have a factor of 3.
- **8** 5

4

5

Exercise 5C

- 1 23 and 29
- **2** 97
- 3 All these numbers are not prime.
- **4** 3, 5, 7
- 5 only if all 31 bars are in a single row, as 31 is a prime number and its only factors are 1 and 31
- 6 a E b C c C
- 7 **a** as this would leave 27 and taking off any other prime, which must be odd, would leave an even number
 - **b** 3, 7 and 19 or 5, 7 and 17 or 5, 11 and 13
- 8 All prime numbers greater than 2 are odd and Odd Odd = Even.

Exercise 5D

- $\mathbf{1} \quad \mathbf{a} \quad 84 = 2 \times 2 \times 3 \times 7$
 - **b** $100 = 2 \times 2 \times 5 \times 5$
 - $\mathbf{c} \quad 180 = 2 \times 2 \times 3 \times 3 \times 5$
 - **d** $220 = 2 \times 2 \times 5 \times 11$
 - $e \quad 280 = 2 \times 2 \times 2 \times 5 \times 7$
 - $\mathbf{f} \quad 128 = 2 \times 2$
 - **g** $50 = 2 \times 5 \times 5$
 - **h** $1000 = 2 \times 2 \times 2 \times 5 \times 5 \times 5$
 - i $576 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3$ j $650 = 2 \times 5 \times 5 \times 13$

2	a	$2^2 \times 3 \times 7$	b	$2^{2} \times 5^{2}$
	С	$2^2 \times 3^2 \times 5$	d	$2^2 \times 5 \times 11$
	e	$2^3 \times 5 \times 7$	f	27
	g	2×5^{2}	h	$2^{3} \times 5^{3}$
	ĭ	$2^{6} \times 3^{2}$	j	$2 \times 5^2 \times 13$

- 4 a Each is double the previous numberb 64, 128
 - **c** 81, 243, 729
 - d 256, 1024, 4096
 - **e** 3, 3², 3³, 3⁴, 3⁵, 3⁶, ...; 4, 4², 4³, 4⁴, 4⁵, ...

- 5 a $2 \times 2 \times 3 \times 5$
- **b** $2^2 \times 3 \times 5$
 - **c** $120 = 2^3 \times 3 \times 5$, $240 = 2^4 \times 3 \times 5$, $480 = 2^5 \times 3 \times 5$
- $\begin{array}{cccc} \mathbf{6} & \mathbf{a} & 7^2 \times 11^2 \times 13^2 \\ & \mathbf{b} & 7^3 \times 11^3 \times 13^3 \end{array}$
 - **c** $7^{10} \times 11^{10} \times 13^{10}$
- 7 because 3 is not a factor of 40 so it does not divide exactly
- **8 a** $5 \times 7 \times 11$ **b** 3×7^2 , x = 3, y = 7

Exercise 5E

1	a20b56c6d28e10f15g24h30
2	It is their product.
3	a 8 b 18 c 12 d 30
4	No. Because the numbers in each part have common factors
5	a 168 b 105 c 84 d 84 e 96 f 54 g 75 h 144
6	3 packs of cheese slices and 4 packs of bread rolls
7	a 8 b 7 c 4 d 14 e 4 f 9 g 5 h 4 i 3 j 16 k 5 I 18
8	a i noii yesiii yesiv nob i noii noiii yesiv no
9	18 and 24, or 6 and 72
Ex	ercise 5F
1	36, 49, 64, 81, 100, 121, 144, 169, 196, 225, 256, 289, 324, 361, 400
2	4, 9, 16 1 + 3 + 5 + 7 + 9 = 25 1 + 3 + 5 + 7 + 9 + 11 = 36 1 + 3 + 5 + 7 + 9 + 11 + 13 = 49
3	a 3 b 5 c 7 d odd numbers
4	a529b3249c5929d15129e23104f10.24g90.25h566.44i16j144
5	a 169 b 196 c Answer between 169 and 196 (exact

answer is 174.24)

- 6 a 50, 65, 82 b 98, 128, 162 c 51, 66, 83 d 48, 63, 80 e 149, 164, 181
- 7 a 25, 169, 625, 1681, 3721b Answers in each row are the same
- 8 £144
- **9** 29
- 10 36 and 49

Exercise 5G

- **2** 1, 4, 9, 16, 25, 36, 49, 64, 81, 100
- 3
 a
 1, 2, 3, 4, 6, 12
 b
 1, 2, 4, 5, 10, 20

 c
 1, 3, 9
 d
 1, 2, 4, 8, 16, 32

 e
 1, 2, 3, 4, 6, 8, 12, 24
 f
 1, 2, 19, 38

 g
 1, 13
 h
 1, 2, 3, 6, 7, 14, 21, 42

 i
 1, 3, 5, 9, 15, 45
 j
 1, 2, 3, 4, 6, 9, 12, 18, 36
- 4
 a
 12, 24, 36
 b
 20, 40, 60

 c
 15, 30, 45
 d
 18, 36, 54

 e
 35, 70, 105
 d
 18, 36, 54
- 5 square numbers
- 6 13 is a prime number
- 7 2, 3, 5, 7, 11, 13, 17, 19
- 8 1+3+5+7+9=25 1+3+5+7+9+11=36 1+3+5+7+9+11+13=491+3+5+7+9+11+13+15=64

9		Square number	Factor of 70
	Even number	16	10
	Multiple of 7	49	35

- **10** 4761 (69²)
- 11 4 packs of sausages, 5 packs of buns
- 12 24 seconds
- 13 30 seconds
- 14 12 minutes; Debbie: 4 and Fred: 3

15 a 1	2 b	9	С	6	d	13
e 1	-		g	16	h	10
i 1	8 j	17	k	8	I	21

16 b 21, 28, 36, 45, 55

Ex	ercise 5H			
1	e 9 t	f 10 j 4	 c 7 g 8 k 11 o 13 	h 3
2	a +5, -5 d +7, -7 g +3, -3 j +12, -12	e +8, −8	f +4, -4	0
3	a 81 e 36 i 25 m 64	f 15 j 21		
4	a 24 e 67 i 13.9	f 101		
5	$\sqrt{50}, 3^2, \sqrt{9}$	0, 4 ²		
6	4 and 5			
7	$\sqrt{324} = 18$			
8	15 tiles		2	
9	a 0.36			
	d i $\frac{2}{3}$ i	ii $\frac{5}{7}$	iii $\frac{8}{9}$	
10	Because $8^2 = \sqrt{81} = 9.8.7$			= 8 and
11	a False c False	b True d True		
12	a $2^2 \times 3^4$	b $2 \times 3^2 =$	18 c 22	
13	a 16 900	b 3600		
Ex	ercise 51			
1	a 45	b 52	c 66	
2	a 200	b 115	c 236	
3	a 56	b 157	c 76	d 193
4	a 144	b 108		
5	a 12.54	b 27.45		
6	a 26.7	b 24.5	c 145.3	d 1.5
7	Sovereign is 102.73p per			
8	Abby 1.247, 6.538 Col is correc		2, Col 5.333,	Donna

9 $31 \times 3600 \div 1610 = 69.31677 \approx 70$

10 a 167.552b 196.4811 a 2.77b 6.0012 a 497.952b 110.978 62513 a Trueb False	2 a 200 b 600 c 800 d 500 e 1000 f 100 g 600 h 400 i 1000 j 1100 k 400 l 700 m 800 n 1000 o 1100 l
Review questions	e 3 f 2 g 3 h 2 i 1 j 1 k 3 l 2 m 74 n 126 o 184
 a 90 b 105 a Last digits: 4, 6, 4. 4×4×4×4×4=1024 b 4 a 6, 12, 18, 24, 30 b 1, 2, 3, 4, 6, 12 	4 a 2000 b 6000 c 8000 d 5000 e 10 000 f 1000 g 6000 h 3000 i 9000 j 2000 k 3000 l 5000 m 8000 n 5000 o 9000 p 4000 7000 0000 i 2000 i 2000
c 25 d 23, 29 4 13.69 5 53, 59 6 a 8 b 8 c 125	 q 7000 r 8000 s 1000 t 2000 5 a 230 b 570 c 720 d 520 e 910 f 230 g 880 h 630 i 110 j 300 k 380 l 630 m 350 n 1010 o 1070
7 9 th February	6 a True b False c True d True e True f False
8 5 packets of pies and 2 packets of breadsticks	7 Welcome to Drayton. Population 1400 (to the nearest 100)
 9 a 2×3×3×5 b 5 10 630 11 a 15 b 3150 12 a 196 b 35×35 must end in 5 13 a Clock A 3 am, clock B 3.15 am b Clock A 12 midday, clock B 1.00 pm 14 a 30 seconds c 75 seconds d 150 seconds 	 8 a Man Utd v Chelsea b QPR V Aston Villa c 20 000, 45 000, 75 000, 18 000, 30 000, 44 000, 20 000, 36 000, 25 000, 35 000 d 19 900, 44 600, 75 300, 18 000, 30 000, 44 400, 20 300, 35 700, 24 700, 35 000 9 a 35 min b 55 min c 15 min d 50 min e 10 min f 15 min g 45 min h 35 min i 5 min
15 a Newton's method = 7.746103896, $\sqrt{60}$ from calculator = 7.745966692 so the root is correct to 2 dp or 3dp if rounded. b Newton's method = 6.245 1612 9, $\sqrt{39}$ from calculator = 6.244 997 998 so the root is correct to 2 dp or 3 dp if rounded.	 j 0 min 10 a 375 b 350 to 374 inclusive 11 A number between 75 and 84 inclusive added to a number between 45 and 54 inclusive with a total not equal to 130, for example 79 + 49 = 128
16 $x = y$	Exercise 6B
Chapter 6 – Number: Approximations	1 a 4.8 b 3.8 c 2.2 d 8.3 e 3.7 f 46.9 g 23.9 h 9.5 i 0.1 j 0.6 k 65.0 l 51.0 2 a 5.78 b 2.36 c 0.98 d 33.09
Exercise 6A	e 23.57 f 91.79 g 8.00 h 2.31
1 a 20 b 60 c 80 d 50 e 100 f 20 g 90 h 70 i 10 j 30 k 30 l 50 m 80 n 50 o 90	i 6.00 j 3.51 k 96.51 l 0.01 3 a 4.6 b 0.08 c 45.716 d 94.85 e 602.1 f 671.76 g 7.1 h 6.904 i 13.78 j 0.1 k 4.002 l 60.0

4	a	9	b	9	с	7	d	3	
	-	8 2	f i			6 154	h I	4 343	
5	-	- I + £7 + £4	,			101	•	5 15	
6	3, 3.46, 3.5								
7	4.7275 or 4.7282								
8	6.445 or 6.446 or 6.447 or 6.448 or 6.449								
9	$8.75 \leq \text{value} < 8.85$								
10	£8.45 to £8.49 inclusive								
11	a $6.45 \text{ cm} \leq \text{value} < 6.55 \text{ cm}$ b Smallest value of perimeter = $2 \times (6.45 + 3.25) = 19.4 \text{ cm}$ Largest value of perimeter = $2 \times (6.55 + 3.35) = 19.8 \text{ cm}$ Therefore $19.4 \leq \text{perimeter} < 19.8$ c Smallest area = $6.45 \times 3.25 = 20.96 \text{ cm}^2$								
12	a	29.83 cm		b	32	.991 cm			
13	3.	645							
Exe	ero	cise 6C							
1		50 000 90 000		60 000 90 000		c 30 000 f 50)		

	a 30.000	00000	C 30 000
	d 90 000	e 90 000	f 50
	g 90	h 30	i 100
	g 90 j 200	k 0.5	0.3
	m 0.006	n 0.05	o 0.0009
	p 10	q 90	r 90
	s 200	t 1000	
2	a 56 000	b 27 000	c 80 000
	d 31 000	e 14 000	f 5900
	g 1100	h 850	i 110
	j 640	k 1.7	4 .1
	m 2.7	n 8.0	o 42
	p 0.80	q 0.46	r 0.066
	s 1.0	t 0.0098	
3	a 64 500	b 19 300	c 4.55
	d 4.08	e 14.4	f 6.69
	g 1.07	h 9430	i 10.4
	g 1.07 j 9.68		
4	a 65, 74	b 95, 149	c 950, 1499
5	Ayton: 750, 8	349; Beeville	e: 950, 1499;
	Charlestow		
6	a 64.4	b 63.5	
7	15, 16 or 17		
-			

- 8 1, because there could be 450 then 449
- 9 Between 1950 and 1954

Evercise hill	in (D	F
	CISE 6D	Exercise

LA								
1		b 15 000e 1050h 20						
2	a £4000	b £3000	c £2000 d £800					
3	a £15 000	b £20 000	c £15 000					
4	£21 000							
5	a 14		c 1.1 d $\frac{3}{4}$					
	e 5	f $\frac{2}{3}$	g 3 h 0.3					
	i 6	j 400	k 2 l 24					
6	a 500 d 50	b 200e 50	c 90f 500					
7	8							
8	a 200	b 2800	c 10 d 1000					
9	a 40	b 10	c £70					
10	1000 or 120	00						
11 Yes, the approximation for both distances is 120 km								
12	2 400							
13	3 a 3 kg b 200							
14	a \$210 000	000 b	\$42 000 000					
15	$7.5 \leq N < 8$	8.5						
16	a $9.5 \le L \le$ c $28.0 \le P$		$4.5 \le W < 5.5$ $42.75 \le A < 57.75$					
Review questions								
1	a 6000	b 790						
2	a 3200	b 5000						
3	3 a i 36 000 000 ii 3600 b i 1000 ii 100							
4			1340 – 1090 = 250 m s up, the other down					
5	a 7650	b 7749						
6	a 2450	b 2549	c i 2475 ii 2524					
7	a 2	b 3	c 3 d 4					
8	a 2 e 3	b 1 f 4	c 2 d 3 g 3 h 1					

9 a 67.5

e 20

b 31

f 12.4

c 3000

g 13.57

d 4.0

h 29.4

- 10 No, as there could be 44 people on the bus and 24 at the bus stop. That makes 68 people altogether and the bus can only have 52 + 10 = 62 passengers maximum.
- 11 Width wise: Yes, as error interval of the envelope is $8.5 \le$ width < 9.5 and for the postcard the error interval is $7.75 \le$ width < 8.25

Length wise: No, as error interval of the envelope is $12.5 \le \text{length} < 13.5$ and for the postcard the error interval is $12.25 \le \text{length} < 12.75$, so largest postcard is larger than the smallest envelope.

- **12** 1.850 or 1.851 or 1.852 or 1.853 or 1.854
- **13** $235 \leq \text{number} < 245$
- 14 a $49.5 \le \text{side} < 50.5$ b No, as the error interval for the peg is $48 \le \text{diameter} < 50$
- **15 a** 10.5 ≤ perimeter < 13.5 **b** 4.375 ≤ area < 7.875

Chapter 7 – Number: Decimals and fractions

Exercise 7A

1	0.48 0.028		2.92 0.09	-	1.12 0.192	-	
2	 8 7.8	~	9 9.7		4 12.1		8.7 9.7

- 3 Yes, with 25p left over
- 4 Alistair 0.90 Shane 70 Charlotte 66
- 5 27 (three 0.7 m lengths from each 2.4 m length)

6	a i $5 \times 1 = 5$	ii 3.36, 1.64
	b i $2 \times 1 = 2$	ii 1.44, 0.56
	c i $15 \times 1 = 15$	ii 13.77, 1.23
	d i $20 \times 1 = 20$	ii 16.08, 3.92

- **7 a** 572 **b i** 5.72 **ii** 1.43 **iii** 22.88
- **8 a** 29 **b** 24 **c** 0.12 **d** 0.08
- **9 a** $33.25 \le ab < 47.25$
 - **b** Because it is the highest value of a divided by the lowest value of b**c** 2.11

Exercise 7B

1	а	0.5	b	0.3	С	0.25	d	0.2
	e	0.16	f	0.142857	g	0.125	h	0.1

- **i** 0.1 **j** 0.076 923
- a i 0.571428571428571428571428571428
 ii 0.714285714285714285714285714285
 iii 0.857142857142857142857142857142
 - **b** The recurring digits are all in the same sequence but they start in a different place each time.
- a i 0.4 ii 0.2 iii 0.1
 b Halve the answers to get 1 ÷ 20 = 0.05 and 1 ÷ 40 = 0.025
- **4** 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8

The recurring digit is the numerator of the fraction.

5 0.09, 0.18, 0.27, 0.36, 0.45, 0.54, 0.63,

0.72, 0.81, 0.90 The recurring digits follow the nine times table.

$$6 \quad \frac{9}{22} = 0.409, \frac{3}{7} = 0.428\ 571,$$
$$\frac{16}{37} = 0.432, \frac{4}{9} = 0.4,$$
$$\frac{5}{11} = 0.45, \frac{6}{13} = 0.461538,$$

7
$$\frac{7}{24} = \frac{35}{120}, \ \frac{3}{10} = \frac{36}{120}, \ \frac{19}{60} = \frac{38}{120}$$

 $\frac{2}{5} = \frac{48}{120}, \ \frac{5}{12} = \frac{50}{120}$

10 a
$$\frac{4}{3} = 1\frac{1}{3}$$
 b $\frac{6}{5} = 1\frac{1}{5}$ c $\frac{5}{2} = 2\frac{1}{2}$
d $\frac{10}{7} = 1\frac{3}{7}$ e $\frac{20}{11} = 1\frac{9}{11}$ f $\frac{15}{4} = 3\frac{3}{4}$

- **11 a i** 0.75, 1.3 **ii** 0.83, 1.2 **iii** 0.4, 2.5 **iv** 0.7, 1.428 571 **v** 0.55, 1.81 **vi** 0.26, 3.75
 - **b** No, look at c above for example

12 The answer is always 1.

- **13** $1 \div 0$ is infinite so there is no finite answer.
- **14 a** 10 **b** 2
 - **c** The reciprocal of a reciprocal is always the original number.
- **15** The reciprocal of *x* is greater than the reciprocal of y. For example, reciprocal of 2 is 0.5, reciprocal of 10 is 0.1.

Exercise 7C

- **1 a** $\frac{1}{3}$ **b** $\frac{1}{5}$ **c** $\frac{2}{5}$ **d** $\frac{5}{24}$ **e** $\frac{2}{5}$ **f** $\frac{1}{6}$ **g** $\frac{2}{7}$ **h** $\frac{1}{3}$ $\frac{3}{5}$ 2 $\frac{2}{5}$ 3 $\frac{2}{3}$ 4 $\frac{1}{5}$ 5 $\frac{1}{2}$ 6 7 Jon saves $\frac{30}{90} = \frac{1}{3}$ Matt saves, $\frac{35}{100} = \frac{7}{20}$, which is greater than $\frac{1}{3}$, so Matt saves the greater proportion of
 - his earnings.
- 8 $\frac{13}{20} = \frac{65}{100}$ and $\frac{16}{25} = \frac{64}{100}$ so 13 out of 20 is the better mark.
- 9
- **10** $\frac{11}{24}$
- 11 26 out of 63 because 13 out of 32 is the same as 26 out of 64.
- **12** The price is the same at both shops: £432

Exercise 7D

- **1** a $\frac{8}{15}$ b $\frac{7}{12}$ c $\frac{11}{12}$ **d** $\frac{1}{10}$ **e** $\frac{1}{8}$ **f** $\frac{1}{12}$
- 2 Three-quarters of 68

- **3 a** $4\frac{47}{60}$ **b** $\frac{41}{72}$ **c** $1\frac{109}{120}$ **d** $1\frac{23}{30}$ 4 a $\frac{1}{6}$ **b** 30
- No, one eighth is left, which is 12.5 cl, so enough for one cup but not two cups.
- He has added the numerators and added 6 the denominators instead of using a common denominator. Correct answer is $3\frac{7}{12}$.
- 7 Possible answer: The denominators are 4 and 5. I first find a common denominator. The lowest common denominator is 20 because 4 and 5 are both factors of 20. So I am changing the fractions to twentieths. One-quarter is the same as five-twentieths (multiplying numerator and denominator by 5). Two-fifths is the same as eighttwentieths (multiplying numerator and denominator by 4). Five-twentieths plus eight-twentieths = thirteen-twentieths.
- 8 $\frac{11}{20}$ of 900 = 495, $\frac{2}{11}$ of 495 = 90 left-handed boys. 900 495 = 405 girls. $\frac{2}{9}$ of 405 = 90 left-handed girls. 180 left-handed students altogether so 180 out of 900 = $\frac{1}{5}$.
- 9 $\frac{1}{5} + \frac{3}{8} = \frac{23}{40}$, so $\frac{17}{40}$ of the counters are yellow. $\frac{17}{40}$ of 600 = 255
- **10 a** because $\frac{27}{40} + \frac{2}{5} = 1\frac{3}{40}$, which is greater than 1.
 - **b** $\frac{2}{5}$ of 200 = 80. $\frac{5}{8}$ of 80 = 50 women at least 40. $\frac{27}{40}$ of 200 = 135 members at least 40. 135 - 50 = 85 men at least 40. $\frac{3}{5}$ of 200 = 120, so 120 - 85 = 35 men under 40.

Exercise 7E

 $\frac{3}{8}$ 3

 $\frac{1}{8}$ 4 5 40 $\frac{2}{5}$ of $6\frac{1}{2}$ 6 £10.40 7 **Exercise 7F 1** a $1\frac{11}{20}$ b $1\frac{1}{4}$ c $1\frac{63}{80}$ **d** $\frac{11}{30}$ **e** $\frac{61}{80}$ **f** $\frac{167}{240}$ **2 a** $12\frac{1}{4}$ miles **b** $3\frac{1}{4}$ miles **3 a** $6\frac{11}{20}$ **b** $8\frac{8}{15}$ **c** $11\frac{63}{80}$ **d** $3\frac{11}{30}$ **e** $7\frac{61}{80}$ **f** $4\frac{277}{396}$ 4 **a** $-\frac{77}{1591}$ **b** The answer is negative 5 $\frac{5}{12}$ (anticlockwise) or $\frac{7}{12}$ (clockwise) **6 a** $\frac{3}{5}$ **b** $\frac{27}{128}$ **c** $5\frac{2}{5}$ **d** $5\frac{1}{7}$ **e** $3\frac{9}{32}$ **f** $\frac{11}{18}$ 7 **a** $8\frac{11}{20}$ **b** $65\frac{91}{100}$ **c** $52\frac{59}{160}$ **d** $2\frac{17}{185}$ **e** $2\frac{22}{103}$ **f** $7\frac{881}{4512}$ 8 3 rolls **9** $22 \div (2 \times \frac{22}{7}) = \frac{7}{2}, \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} = 38\frac{1}{2} \text{ cm}^2$

Review questions

- 0.3 < decimal < 0.33... for example 0.32 1
- 2 17
- **b** $\frac{9}{20}$ 3 **a** 0.4 $\frac{22}{75}$
- 4
- **a** 0.5 **b** 0.3 5
- $28 \div 40 = 0.7$; $33 \div 50 = 0.66$. Zac did better 6 in English
- $\frac{4}{5}$ 7
- 900 × 12 = 10 800 miles per year. 10 800 ÷ 45 8 = 240 gallons. $240 \times 4.55 = 1092$ litres. $1092 \times$ $1.4 = \pm 1528.80$ per year.

9 a 5 b $\frac{3}{2}$ c $\frac{7}{1}$
--

d $\frac{1}{8}$

10 Starbuys $10 \times 0.8 = \pm 8$. Shoprite $12 \times 0.8 =$ $\pm 9.60.20\%$ off = ± 7.68 , so Shoprite is best value.

11	a	1672	b	i	167.2	ii	83.6	iii	16.72
----	---	------	---	---	-------	----	------	-----	-------

- **12 a** 3.2 **b** 360 **c** 0.32
- **13 a** $\frac{7}{20}$ **b** $\frac{2}{5}$ **c** $1\frac{1}{2}$
- 14 40.96
- 15 $2\frac{1}{24}$
- **16** $18\frac{11}{12}$ cm
- 17 $18\frac{5}{12}$ m²
- **18** a 0.5 (T), 0.6 (R), 0.75 (T), 0.8 (T), 0.83 (R), 0.857142 (R), 0.875 (T), 0.8 (R), 0.9 (T)
 - **b** 2, 2 \times 2, 5, 2 \times 2 \times 2, 2 \times 5
 - c If the prime factors of the denominator of a fraction in its simplest form are only 2 and/or 5 its decimal will terminate.

19		Blue	Red	Total
	Squares	136	74	210
	Triangles	95	95	190
	Total	231	169	400

Chapter 8 – Algebra: Linear graphs

Exercise 8A

- a A(1, 2), B(3, 0), C(0, 1), D(-2, 4), 1 E(-3, 2), F(-2, 0), G(-4, -1), H(-3, -3), I(1, -3), J(4, -2)
 - **b** i (2, 1) ii (-1, -3) iii (1, 1)
- **2 a** x = -3, x = 2, y = 3, y = -4L: 1 ;. <u>1</u>

b i
$$x = -\frac{1}{4}$$
 ii $y = -\frac{1}{2}$

- 3 Values of *y*: 2, 3, 4, 5, 6
- Values of *y*: –2, 0, 2, 4, 6 4
- Values of *y*: 1, 2, 3, 4, 5 5
- 6 Values of *y*: -4, -3, -2, -1, 0
- a Check student's graph 7 **b** (6, 12)
- Points could be (0, -1), (1, 4), (2, 9), (3, 14), 8 (4, 19), (5, 24), etc

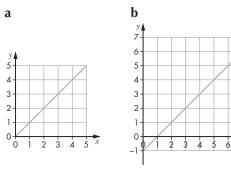
- **9** a £20.50
 - b £25.00, £28.50, £32.00, £35.50, £39.00, £42.50;
 (£20.00), £23.50, £27.00, £30.50, £34.00, £37.50;
 (£15.00), £18.50, £22.00, £25.50, £29.00, £32.50;
 (£10.00), (£13.50), £17.00, £20.50, £24.00, £27.50;
 (£5.00), (£8.50), (£12.00), £15.50, £19.00, £22.50;
 (£0.00), (£3.50), (£7.00), (£10.50), (£14.00), £17.50
 c Yes, they had 3 rolls and 4 baguettes.

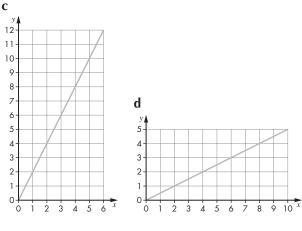
10 Number
$$\times 3$$
 $+1$ Answer

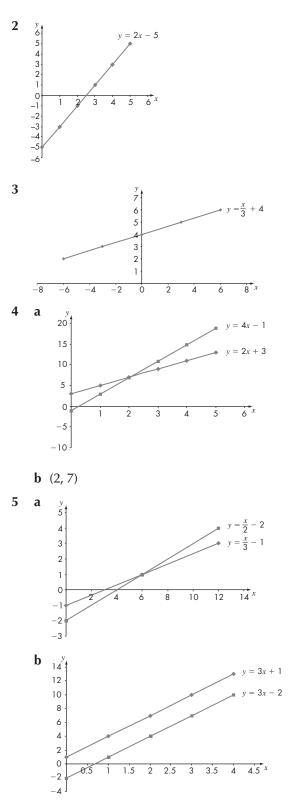
- **b** y = 3x + 1
- **c** Graph from (0, 1) to (5, 16)
- **d** Read from 13 on the *y*-axis across to the graph and down to the *x*-axis. This should give a value of 4.
- **11** 0, 8, 16, 24, 32, 40, 48

Exercise 8B



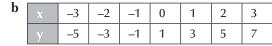




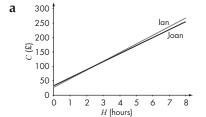


c Lines in part a intersect at (6, 1). Lines in part b don't intersect because they are parallel.

6 a Line isn't straight

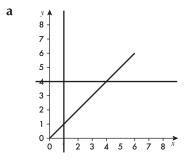




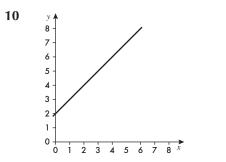


- **b** Ian, as Ian only charges £85, whilst Joan charges £90 for a 2-hour job
- 8 Jada's

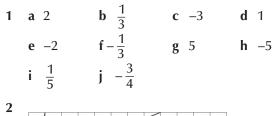
9

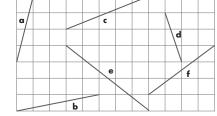


b 4.5 units squared



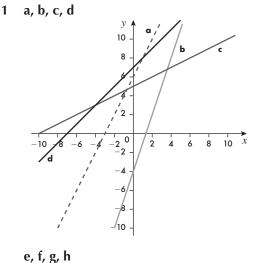
Exercise 8C

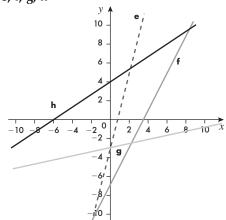




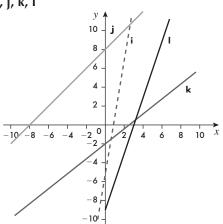
- 3 a Both answers are correct
 - **b** generally the bigger the triangle the more accurate the answer, so Brianna
- 4 a Slide won't be steep enough for children to slide down.
 - **b** If it is too steep children might slide down too quickly.
 - c A, B, E and F satisfy the safety regulations; C and D do not
- **5 a** 0.5 **b** 0.4 **c** 0.2 **d** 0.1 **e** 0
- **6 a** 1.4 **b** 2 **c** 3.3 **d** 10 **e** ∞
- 7 Raisa has misread the scales. The second line has four times the gradient (2.4) of the first (0.6).
- 8 4 horizontal 6 vertical; 5 horizontal 8 vertical; 3 horizontal 5 vertical; 6 horizontal 11 vertical; 1 horizontal 2 vertical; 2 horizontal 5 vertical
- **9** 0, 2, -1, $\frac{1}{2}$, $-\frac{3}{2}$

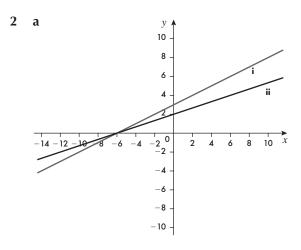
Exercise 8D







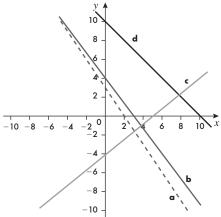


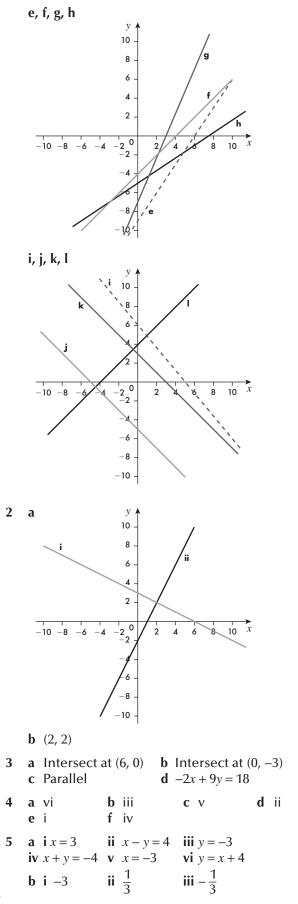


- 3 **a** y = 3x 2**b** They intercept the *y*-axis at the same point (0, -2).
 - **c** (−1, −4)
- **4 a** -2 **b** $\frac{1}{2}$

Exercise 8E

1 a, b, c, d





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6 Cover-up method for 2x + y = 10 and gradient-intercept method for y = 10 - 2x, but actually the lines are the same

Exercise 8F

- 1 **a** $y = \frac{4}{3}x 2$ or 3y = 4x 6**b** y = 2x **c** 2y = x + 6
- 2 a i y=2x+1, y=-2x+1ii Reflection in y-axis (and y=1) iii Different sign
 - **b** i 5y = 2x 5, 5y = -2x 5ii Reflection in *y*-axis (and y = -1) iii Different sign
 - **c** i y=x+1, y=-x+1ii Reflection in *y*-axis (and y=1) iii Different sign
- 3 **a** *x*-coordinates go from $2 \rightarrow 1 \rightarrow 0$ and *y*-coordinates go from $5 \rightarrow 3 \rightarrow 1$.
 - **b** *x*-step between the points is 1 and *y*-step is 2.
 - $\mathbf{c} \quad y = 3x + 2$
- 4 **a** y = -x + 1 **b** 5y = -2x - 5**c** $y = -\frac{3}{2}x - 3$ or 2y = -3x - 6
- 5 **a** i $y = \frac{1}{2}x, y = 2x$
 - **ii** Reflection in x = y

iii Reciprocal of each other

b i y = 2, x = 2 ii Reflection in x = y

iii Reciprocal of each other (reciprocal of zero is infinity)

- 6 All of the lines except $y = \frac{1}{4}x + 9$
- 7 **a** y = -3x + 5 **b** y = 2x - 4 **c** y = 8x - 3**e** $y = \frac{2}{3}x - 1$
- **8** 5x + 6y = 30
- 9 Chris is correct. The equation of the line is $y = \frac{1}{2}x + 2$ and (12, 8) satisfies the rule

10 a i x + y = 100 ii k = 1b i x = 46 ii k = 46c i y = 2x + 1 ii k = 60d i y = x + 19 ii k = -17

Exercise 8G

1 A and B are parallel because they have the same gradient (m = 3)

2 x = 8 and x = -2 y = 3 - x and y = 10 - x y = 3x - 5 and y = 3x + 9 $y = -\frac{1}{8}x$ and $y = -\frac{1}{8}x + 6$ 2x + y = 9 and 2x + y = 13 y = 15 - 4x and y = 7 - 4x3 **a** $y = \frac{1}{2}x - 2$ **b** y = -x + 3 **c** y = 3x - 8 **d** $y = -\frac{1}{3}x + 10$ 4 **a** y = 2x + 4 **b** y = 17 - 3x**c** y = 3x - 1

Exercise 8H

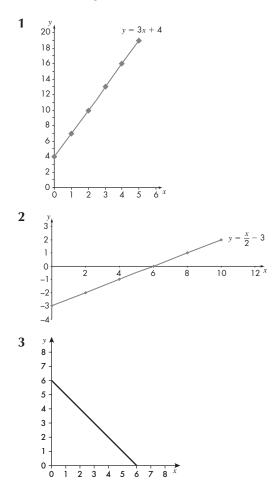
- 1 **a** i 8 $\frac{1}{4}$ kg ii 2 $\frac{1}{4}$ kg iii 9 lb iv 22 lb **b** 2.2 lb **c** Read off the value for 12 lb (5.4 kg) and multiply this by 4 (21.6 kg) **d** $m = \frac{5}{11}$ **e** $\frac{5}{11}$ kilograms per pound
- **2 a i** £100 **ii** £325 **b i** 500 **ii** 250
- **3 a i** 95 °F **ii** 68 °F **iii** 10 °C **iv** 32 °C **b** 32 °F **c** $m = \frac{5}{9}, \frac{5}{9}$ °C per °F
- a Check student's graph
 b 2:15 pm
 c m = 48, 48 cups of tea per hour
- 5 Check student's graph, £50
- 6 a Anya: CabCo £8.50, YellaCabs £8.40, so YellaCabs is best Bettina: CabCo £11.50, YellaCabs £11.60, so CabCo is best Calista: CabCo £10, YellaCabs £10, so either
 - **b** If they shared a cab, the shortest distance is 16 km, which would cost £14.50 with CabCo and £14.80 with Yellacabs.
- **7 a** \$642.86
- **b i** \$7500 **ii** £3666.67

Exercise 81

- 1 (4, 1)
- **2** (2, 3)

- (3, 10)3
- 4 (-2, 6)
- (-6, -9)5
- (1, -1)6
- 7 (2, 6)
- 8 (2, 8)
- 9 x + 2y = 9.5, 2x + y = 8.5Graphs intersect at (2.5, 3.5), so a bun costs £2.50 and a cake costs £3.50.
- 10 a P and R
 - **b** R and S
 - c P and Q
 - d Q and S
- **11** (0, 0), (-3, 3), (-3, -3), (-3, 2), (-2, 2), (2, 2)
- 12 a no solutions
 - **b** infinite solutions
 - **c** one solution
 - d a Parallel b Same line c Not parallel

Review questions



- 4 a $\frac{1}{10}$
 - **b** 24.5 cm
 - c 0.1 cm or 1 mm
 - **d** $l = 24.5 + \frac{W}{10}$ or Length = 24.5 + 1 mm/kg
- 5 A Q, B T, C P, D R, E S
- **6 a** (5, 5) **b** (1, 5) **c** (3, 16)
- 7 72 square units
- **b** y = 2x + 28 **a** 2 **c** y = 2x - 5
- 9 **a** x + y = 50 (or y = 50 - x) **b** -3 **c** x + y = 40 (or y = 40 - x)

Chapter 9 – Algebra: **Expressions and formulae**

Exercise 9A

- **a** x+21 **b** x - 6c hj **d** $y \div t$ or $\frac{y}{t}$ **e** a^2 $\mathbf{f} g^2$
- 2 **a** Dad: (72 + x) years, me: (T + x) years **b** 31
- For example, $2 \times 6m$, $1 \times 12m$, 6m + 6m, etc 3
- Any values picked for *l* and *w* and 4 substituted into the formulae to give the same answers
- 5 13 years
- 15p 6
- 7 a expression **b** formula **c** identity d equation

Exercise 9B

- 1 **a** 3 **b** 11 **c** 43
- 2 **b** 5 **a** 9 **c** –1
- 3 **a** £4.00 **b** 13 km c Yes, the journey will cost £5.00
- **a** 1.4 **b** 1.4 **c** -0.4 4
- a 2.5 **b** -20 **c** 2.5 5
- 150 **b** £925 6 а n
- 7 **a** $2 \times 8 + 6 \times 11 - 3 \times 2 = 76$
 - **b** $5 \times 2 2 \times 11 + 3 \times 8 = 12$

- 8 a One odd, one even value, different from each other.
 - **b** Any valid combination, e.g. x = 1, y = 2
- 9 a i Odd ii Odd iii Even iv Odd
 - **b** Any valid expression such as xy + z

10 a £20 **b** –£40 **c** 40 miles

- **11 a** First term is cost of petrol, each mile is a tenth of £1.20. Second term is the hire cost divided by the miles.
 - **b** 32 p per mile

Exercise 9C

- **1 a** 6+2*m* **b** 10 + 5l**c** 12 - 3y**d** 20 + 8k**e** 6 – 12*f* **f** 10 – 6*w* **g** 10*k* + 15*m* **h** 12*d* – 8*n* i $t^2 + 3t$ $k^2 - 3k$ **k** $4t^2 - 4t$ $8k - 2k^2$ $m 8g^2 + 20g$ **n** $15h^2 - 10h$ **o** $v^3 + 5v$ **p** $h^4 + 7h$ **q** $k^3 - 5k$ **r** $3t^3 + 12t$ **s** $15d^3 - 3d^4$ t $6w^3 + 3tw$ **u** $15a^3 - 10ab$ **v** $12p^4 - 15mp$ **w** $12h^3 + 8h^2g$ **x** $8m^3 + 2m^4$
- **2 a** 5(t-1) and 5t-5
 - **b** Yes, as 5(t 1) when t = 4.50 is $5 \times 3.50 =$ £17.50
- 3 a He has worked out 3 × 5 as 8 instead of 15 and he has not multiplied the second term by 3.
 b 15x 12
- 4 **a** 3(2y+3)**b** 2(6z+4) or 4(3z+2)

Exercise 9D

- **1 a** 7t **b** 3y **c** 9d **d** 3e **e** 3p **f** 2t **g** 5t² **h** 5ab **i** $3a^2d$
- **2 a** 22 + 5t **b** 21 + 19k **c** 22 + 2f**d** 14 + 3g
- **3 a** 2+2h **b** 9g+5 **c** 17k+16**d** 6e+20
- **4 a** 4m + 3p + 2mp **b** 3k + 4h + 5hk**c** 12r + 24p + 13pr **d** 19km + 20k - 6m
- **5 a** $9t^2 + 13t$ **b** $13y^2 + 5y$ **c** $10e^2 - 6e$ **d** $14k^2 - 3kp$
- **6 a** 17ab + 12ac + 6bc **b** 18wy + 6ty 8tw**c** 14mn - 15mp - 6np **d** $8r^3 - 6r^2$
- 7 **a** 5(f+2s) + 2(2f+3s) = 9f + 16s**b i** £270*f* **ii** £480*s*
 - **c** $\pm 42450 \pm 30000 = \pm 12450$

- 8 For *x*-coefficients, 3 and 1 or 1 and 4; for *y*-coefficients, 5 and 1 or 3 and 4 or 1 and 7
- 9 5(3x+2) 3(2x-1) = 9x + 13

Exercise 9E

1	а	6(m+2t)	b	3(3t -	+ <i>p</i>)	С	4(2m + 3k)
	d	4(r+2t)	e	m(n +	+ 3)	f	g(5g + 3)
	g	2(2w - 3t)	h	y(3y -	+ 2)	i	t(4t - 3)
	j	3m(m-p)	k	3p(2p)	(r + 3t)	I	2p(4t+3m)
	m	4b(2a - c)	n	5bc(b	-2)	0	2b(4ac + 3de)
	р	$2(2a^2+3a+4)$)	q	3b(2a -	+ 3	c + d)
	r	t(5t + 4 + a)		s	3mt(2t	- 1	1 + 3 <i>m</i>)
	t	2ab(4b + 1 - 2)	(a	u	5 <i>pt</i> (2 <i>t</i> -	+ 3	(+p)
2	а	Mary has tak	er	n out	a com	no	n factor.

- 2 a Mary has taken out a common factor.
 b Because the bracket adds up to £10
 c £30
- 3 a, d, f and h do not factorise
 - **b** m(5+2p) **c** t(t-7) **e** 2m(2m-3p) **g** a(4a-5b)**i** b(5a-3bc)
- 4 a Bernice
 - **b** Aidan has not taken out the largest possible common factor. Craig has taken *m* out of both terms but there isn't an *m* in the second term.
- 5 There are no common factors.
- 6 Perimeter = 2x + 8 + x + 5 + 5x + 4 + 9x 3 + 10 x = 16x + 24 = 8(2x + 3)

$$7 \quad \frac{4x^2 - 12x}{2x - 6} = \frac{4x(x - 3)}{2(x - 3)}$$

Exercise 9F

1	а	$x^2 + 5x + 6$	b	$t^2 + 7t + 12$
	С	$w^2 + 4w + 3$	d	$m^2 + 6m + 5$
2	а	$p^2 + 3p - 70$	b	$u^2 - 12u + 32$

- **c** $k^2 + 2k 15$ **d** $z^2 12z + 27$
- a should be 35 on the end
 b should be 80 c should be -10x
 d should be 12y e should be -9z

Exercise 9G

1	a $k^2 + 8k + $ c $x^2 + 2x - $ e $w^2 + 2w$	- 8	b $a^2 + 5a + 4$ d $t^2 + 2t - 15$ f $f^2 - f - 6$
2	a $r^2 - 10r$ c $d^2 - 17d$ e $q^2 - 20q$	<i>l</i> + 16	b $s^2 - 17s + 70$ d $m^2 - 9m + 18$ f $y^2 - 13y + 40$
3	a 20 <i>a</i> d –11 <i>d</i>	b 3 <i>b</i> e 12 <i>e</i> , 2	c 200

Exercise 9H

- **1 a** $g^2 3g 4$ **b** $y^2 + y - 12$ **c** $x^2 + x - 12$ **d** $p^2 - p - 2$ **e** $k^2 - 2k - 8$ **f** $y^2 + 3y - 10$ **g** $a^2 + 2a - 3$
- **2 a** $x^2 9$ **b** $t^2 25$ **c** $m^2 16$ **d** $t^2 - 4$ **e** $y^2 - 64$ **f** $p^2 - 1$ **g** $25 - x^2$ **h** $49 - g^2$ **i** $x^2 - 36$
- 3 (x+2) and (x+3)
- 4 **a** B: $1 \times (x 2)$ C: 1×2 D: $2 \times (x 1)$ **b** (x - 2) + 2 + 2(x - 1) = 3x - 2 **c** Area A = (x - 1)(x - 2) = area of square minus areas (B + C + D) = $x^2 - (3x - 2) = x^2 - 3x + 2$

5 a $x^2 + 2x + 1$ **b** $x^2 - 2x + 1$ **c** $x^2 - 1$

Exercise 91

- 1 a $6x^2 + 11x + 3$ **b** $12y^2 + 17y + 6$ c $6t^2 + 17t + 5$ **d** $8t^2 + 2t - 3$ e $10m^2 - 11m - 6$ f $12k^2 - 11k - 15$ **g** $6p^2 + 11p - 10$ **h** $10w^2 + 19w + 6$ i $8r^2 - 10r + 3$ i $6a^2 - 7a - 3$ **k** $15g^2 - 16g + 4$ $12d^2 + 5d - 2$ $m 8p^2 + 26p + 15$ **n** $6t^2 + 7t + 2$ **o** $6p^2 + 11p + 4$ **p** $6 - 7t - 10t^2$ **r** $6f^2 - 5f - 6$ **q** $12 + n - 6n^2$ s $12 + 7q - 10q^2$ t $3 - 7p - 6p^2$ **u** $4 + 10t - 6t^2$
- 2 a $(3x-2)(2x+1) = 6x^2 x 2$ $(2x-1)(2x-1) = 4x^2 - 4x + 1$ $(6x-3)(x+1) = 6x^2 + 3x - 3$ $(4x+1)(x-1) = 4x^2 - 3x - 1$ $(3x+2)(2x+1) = 6x^2 + 7x + 2$
- **3 a** $4x^2 1$ **b** $9t^2 4$ **c** $25y^2 9$ **d** $16m^2 - 9$ **e** $4k^2 - 9$ **f** $16h^2 - 1$ **g** $4 - 9x^2$ **h** $25 - 4t^2$ **i** $36 - 25y^2$ **j** $a^2 - b^2$ **k** $9t^2 - k^2$ **l** $4m^2 - 9p^2$ **m** $25k^2 - g^2$ **n** $a^2b^2 - c^2d^2$ **o** $a^4 - b^4$
- **4 a** $a^2 b^2$
 - **b** Dimensions: a + b by a b; Area: $a^2 b^2$ **c** Areas are the same, so $a^2 - b^2 = (a + b) \times (a - b)$
- 5 First shaded area is $(2k)^2 1^2 = 4k^2 1$ Second shaded area is $(2k+1)(2k-1) = 4k^2 - 1$

Exercise 9J

1a $x^2 + 10x + 25$ b $m^2 + 8m + 16$ c $t^2 + 12t + 36$ d $p^2 + 6p + 9$ e $m^2 - 6m + 9$ f $t^2 - 10t + 25$ g $m^2 - 8m + 16$ h $k^2 - 14k + 49$

- **2 a** $9x^2 + 6x + 1$ **b** $16t^2 + 24t + 9$ c $25y^2 + 20y + 4$ **d** $4m^2 + 12m + 9$ **e** $16t^2 - 24t + 9$ f $9x^2 - 12x + 4$ **g** $25t^2 - 20t + 4$ **h** $25r^2 - 60r + 36$ i $x^2 + 2xy + y^2$ i $m^2 - 2mn + n^2$ **k** $4t^2 + 4ty + y^2$ $m^2 - 6mn + 9n^2$ **m** $x^2 + 4x$ **n** $x^2 - 10x$ **o** $x^2 + 12x - 4$ **p** $x^2 - 4x + 8$
- **3 a** Bernice has just squared the first term and the second term. She hasn't written down the brackets twice.
 - **b** Pete has written down the brackets twice but has worked out $(3x)^2$ as $3x^2$ and not $9x^2$.
 - **c** $9x^2 + 6x + 1$
- 4 Whole square is $(2x)^2 = 4x^2$. Three areas are 2x - 1, 2x - 1 and 1. $4x^2 - (2x - 1 + 2x - 1 + 1) = 4x^2 - (4x - 1)$ $= 4x^2 - 4x + 1$

Exercise 9K

1		(x+2)(x+3) (m+2)(m+5)	-	(t+1)(t+4) (k+4)(k+6)
2	a c	(p+2)(p+12) (w+2)(w+9)	-	(r+3)(r+6) (x+3)(x+4)
3	a c	(a+2)(a+6) (f+21)(f+1)		(k+3)(k+7) (b+8)(b+12)
4	a c	(t-2)(t-3) (g-2)(g-5)	-	(d-4)(d-1) (x-3)(x-12)
5	a c	(c-2)(c-16) (y-4)(y-12)	-	(t-4)(t-9) (j-6)(j-8)
6		(p-3)(p-5) (t+4)(t-2)	-	(y+6)(y-1) (x+5)(x-2)
7	a c	(m+2)(m-6) (n+3)(n-6)	-	(r+1)(r-7) (m+4)(m-11)
8	a c	(w+4)(w-6) (h+8)(h-9)	-	(t+9)(t-10) (t+7)(t-9)
9		$(d+1)^2$ $(t-4)^2$	-	$(y + 10)^2$ $(m - 9)^2$
10		$(x-12)^2$ (t+4)(t-5)	-	(d+3)(d-4) (q+7)(q-8)

- 11 (x+2)(x+3), giving areas of 2x and 3x, or (x+1)(x+6), giving areas of x and 6x.
- **12 a** $x^2 + (a+b)x + ab$ **b i** p+q=12 **ii** pq=7
 - **c** 7 can only be 1×7 and $1 + 7 \neq 12$

Exercise 9L

- **1 a** (x+3)(x-3) **b** (t+5)(t-5) **c** (m+4)(m-4) **d** (3+x)(3-x) **e** (7+t)(7-t) **f** (k+10)(k-10) **g** (2+y)(2-y) **h** (x+8)(x-8)**i** (t+9)(t-9)
- **2 a** x^2
 - **b** i (x-2) ii (x+2) iii x^2 iv 4 v x^2-4
 - **c** $A + B C = x^2 4$, which is the area of D, which is (x + 2)(x 2).
- **3 a** $x^2 + 4x + 4 (x^2 + 2x + 1) = 2x + 3$
 - **b** (a+b)(a-b)
 - c (x+2+x+1)(x+2-x-1) = (2x+3)(1) = 2x+3
 - **d** The answers are the same.
 - **e** 4*x*

Exercise 9M

1 $k = \frac{T}{3}$ **2** y = X + 1 **3** p = 3Q**4** A - 9

4
$$r = \frac{A-9}{4}$$

- **5 a** m = p t**b** t = p - m
- 6 m = gv

7
$$m = \sqrt{t}$$

8
$$l = \frac{P-2w}{2}$$

9
$$p = \sqrt{m-2}$$

- **10** a $-40 32 = -72, -72 \div 9 = -8, 5 \times -8 = -40$ b $68 - 32 = 36, 36 \div 9 = 4, 4 \times 5 = 20$ c $F = \frac{9}{5}C + 32$
- 11 Average speeds: outward journey = 72 km/h, return journey = 63 km/h, taking 2 hours. He was held up for 15 minutes.

12 a
$$y = \frac{5x - 75}{9}$$

b Check by substitution

13 a
$$a = \frac{v-u}{t}$$

b $t = \frac{v-u}{a}$
14 $d = \sqrt{\frac{4A}{\pi}}$
15 a $y = \frac{x+w}{5}$
b $w = 5y-x$

16
$$p = \sqrt{\frac{k}{2}}$$

17 **a** $t = u^2 - v$
b $u = \sqrt{v + t}$
18 **a** $w = K - 5n^2$
b $n = \sqrt{\frac{K - w}{5}}$
19 **a** $D = \frac{P + Y(K - U)}{3(K - U)}$ or $\frac{\frac{P}{K - U} + Y}{3}$ or
 $D = \frac{P}{3(K - U)} + \frac{Y}{3}$
b 16

Review questions

1 t - xy**2** a 180 - p - q**b** 59° 3 **a** $r = \frac{C}{2\pi}$ **b** $r = \sqrt{\frac{A}{\pi}}$ **4 a** 20*x* + 16 **b** 5x + 4**5 a** $c = \frac{R - 3d - 5}{7}$ **b** 6 6 $12x^2 - xy - 35y^2$ 7 a i 3.5 ml ii 3.7 ml iii 3.84 ml **b** i 22 **ii** 38 iii 90 **8** 13.5 m² **9 a** 6r(r+h) **b** $h = \frac{A-6r^2}{6r}$ **c** 5 cm **10 a** $3 \times 15 \times 4 = 180$ **b** $6x^2 - 51x + 90$ **11 a** $x = \frac{A - y}{0.01y}$ **b** y(1 + 0.01x) **c** 22 g **12 a i** $15x^2 - 19x - 56$ ii 16x - 2**b** 162.25 cm² **13 a** $4x^2 + 4x + 1$ **b** 441 14 20 m **15 a** 2(x-8) **b** x(x-16) **c** (x-4)(x+4)**d** (x-7)(x-9)**16** a (x - 10)(x + 10)**b** (x-20)(x+20)c (x-200)(x+200)17 -3 + 7 is not -20(x - 21)(x + 1)

Chapter 10 – Ratio and proportion and rates of change: Ratio, speed and proportion

Exercise 10A

1 a 1:3 **b** 2:3 **c** 2:5 **d** 5:8 **f** 7:3 **e** 3:2 **g** 1:6 **h** 5:3 2 **a** 1:3 **b** 5:12 **c** 17:15 **d** 4:1 **e** 1:24 **f** 5:2 g 2:1 **h** 31:200 3 $\overline{10}$ $\frac{2}{5}$ 4 $a \frac{2}{5}$ **b** $\frac{3}{5}$ 5 6 2:1**a** Fruit crush $\frac{1}{6}$, lemonade $\frac{5}{6}$ 7

Fruit Crush	1.25	1	0.2	0.4	0.5
Lemonade	6.25	5	1	2	2.5

- **b** 0.4 litres **c** 2.5 litres
- 8 Sugar $\frac{5}{22}$, flour $\frac{3}{11}$, margarine $\frac{2}{11}$, fruit $\frac{7}{22}$

11 a 5:3:2 **b** 20 years old

12 $13\frac{1}{2}$ litres

Exercise 10B

a 160 g, 240 g **b** 80 kg, 200 kg 1 **c** 175 min, 125 min **d** £20, £30, £50 e £36, £60, £144 f 50 g, 250 g, 300 g 2 a 175 women **b** 30% **a** 40% 3 **b** 300 kg 4 21 horses 5 a 1:400 000 **b** 1: 125 000 c 1:250 000 **d** 1:25 000 **e** 1:20 000 f 1:40 000 **6 a** Map A 1 : 250 000, Map B 1 : 1 000 000 **c** 1.2 cm or $\frac{6}{5}$ cm **b** 2 km d 4.8 cm

- 7 a 1:1.6 b 1:3.25 c 1:1.125 d 1:1.44 e 1:5.4 f 1:1.5 g 1:4.8 h 1:42 i 1:1.25
- 8 Diesel : Petrol = 60 : 90. $\frac{1}{5}$ of 60 = 12. $\frac{4}{9}$ of 90 = 40. Total red cars = 52 which is more than $150 \div 3 = 50$, so yes.
- **9** $13 9 = 4.4 \div 5 = 0.8.2 \times 0.8 = 1.6, 9 + 1.6 = 10.6$
- 10 Athos has 3 more parts than Zena. $24 \div 3 = 8$, so 1 part is 8. Zena has 8 marbles.

Exercise 10C

- **1 a** 3:2 **b** 32 **c** 80
- 2 1000 g or 1 kg
- **3** 8100
- **4 a** 14 minutes **b** 75 minutes
- 5 Kevin £2040, John £2720
- 6 a Lemonade 20 litres, ginger 0.5 litres
 - **b** The one in **b**. In part **a** there are 50 parts in the ratio 40:9:1, so ginger is $\frac{1}{50}$ of total amount; in part **b** there are

13 parts in the ratio 10:2:1, so ginger is $\frac{1}{13}$ of total amount.

- $\frac{1}{13} > \frac{1}{50}$
- 7 296 seats
- 8 100 students
- 9 40 ml
- **10 a** Will as his multiple of 10 is also a multiple of 9
 - **b** Zeke has rounded off to 1dp and and Yoko has rounded off to 2 dp. They have not used a recurring decimal notation.
- 11 43 people (20 boys, 8 girls, 15 adults)
- **12** $\frac{6}{11}$
- **13** $\frac{1}{2}$

Exercise 10D

- 1 18 mph
- 2 280 miles
- 3 52.5 mph

- 4 11:50 am
- 5 a 75 mph b 6.5 h c 175 miles d 240 km e 64 km/h f 325 km g 4.3 h (4 h 18 min)
- 6 a 500 m or 0.5 km
 - **b** 12:06 pm
 - c His actual speed and distance may not be the same as his estimate, so he may not be back at the estimated time.
- **7 a** 2.25 h **b** 99 miles
- **8 a** 1.25 h **b** 1 h 15 min
- 9 a Sheffield to London via Midland mainline 74.38 mph. Sheffield to London via East Coast mainline 78.26 mph
 - **b** Doncaster to London 94.12 mph
- **10 a** 120 km **b** 48 km/h
- **11 a** 10 m/s **b** 3.3 m/s **c** 16.7 m/s
- **12 a** 90 km/h **b** 43.2 km/h **c** 1.8 km/h
- 13 18 m/s is 64.8 km/h. 40 km at 64.8 km/h is 0.617 hours ≈ 37 minutes so train arrives at 8.07 am

¹⁴

Time	Cyclist A	Cyclist B
10	16	0
10.15	20	6
10.30	24	12
10.45	28	18
11	32	24
11.15	36	30
11.30	40	36
11.45	44	42
12	48	48
12.15	52	54

Cyclist B catches cyclist A at 12 noon

15 Rebecca: 10 minutes at 50 mph covers 8.333 miles, 10 minutes at 70 mph covers 11.666 miles, so total distance is 20 miles in 20 minutes which is 60 mph, so Rebecca is correct. Nick: 10 miles at 40 mph takes 15 minutes, 10 miles at 60 mph takes 10 minutes, so total distance is 20 miles in 25 minutes, which is 48 mph, so Nick is wrong.

16 Josh should take 40 minutes. Nell should take $50 \div 70 \times 60 = 43$ minutes, but Josh is likely to meet traffic through town so is unlikely to travel at anywhere near 30 mph. Nell is likely to be able to travel at 70 mph on the motorway.

Exercise 10E

- 1 60 g
- **2** £5.22
- **3** 45 trees
- **4** £6.72
- 5 a £312.50 b 8 textbooks
- 6 a 56 litres b 350 miles
- **7 a i** 100 g, 200 g, 250 g, 150 g
 - ii 150 g, 300 g, 375 g, 225 g
 - iii 250 g, 500 g, 625 g, 375 g
 - **b** 24 biscuits
- 8 a Peter: £2.30 ÷ 6 = 38.33p each; I can buy four packs (24 sausages) from him (£9.20)

Paul: £3.50 ÷ 10 = 35p each; I can only buy two packs (20 sausages) from him (£7)

I should use Peter's shop to get the most sausages for £10.

- **b** Buy one pack from Peter and two packs from Paul. That would amount to 26 sausages for £9.30.
- 9 400 ÷ 10 = 40 loaves. 40 ÷ 3 = 13.333, so 13.333 × 1.8 = 24 kg of flour.
- 10 4 buns and 5 cakes

Exercise 10F

- **1 a** £4.50 for a 10-pack
 - **b** £1.08 for 6
 - c £2.45 for 1 litre
 - **d** Same value
- **2** a Large jar as more g per £
 - **b** 75 ml tube as more ml per £
 - c Large box as more g per £
 - d 400 ml bottle as more ml per £

- a £5.11
 b Large tin (small £5.11/l, medium £4.80/l, large £4.47/l)
- **4 a** 95p **b** Family size
- 5 Mary
- 6 Kelly
- 7 12-pack $360 \div 12 = 30$ p per sachet. 40-pack 1150 ÷ 40 = 28.75 p per sachet. 4 sachets cost 4 × 35 = £1.40 but you get 5, so 140 ÷ 5 = 28 p per sachet, so the offer is the best value.
- 8 a Abe uses $10 \times 0.75 = 7.5$ litres to do 100 km. Caryl uses $100 \div 14 = 7.14$ litres to do 100 km and Des (55 miles = 88 km) uses $100 \div 88 \times 4.55 = 5.17$ litres to do a 100 km, so Des's car is the most economical.
 - **b** It does not give a 'unit' value, i.e. miles per gallon or litres per mile.
- **9** Yes. Let the initial price be *x*. 50% off means the cost is 0.5*x* each. Two for the price of one means two will cost *x*, so one will cost 0.5*x*.
- **10** $$2.09 \div 1.51 = £1.38$ per US gallon.

 $\pm 1.38 \div 3.8 = \pm 0.36$ per litre in US.

 $\pm 1.09 \div \pm 0.36 = 3.02.$

Petrol is therefore approximately 3 times more expensive in UK than in the USA.

11 $\pounds 42 \times 1.2 = \pounds 50.40$

 $65 \div 50.4 = 1.29$

€1.29 = £1

12 a Shirts 4 U: $75 + 400 \times 3.45 = \pounds1455$ Top Tees: $100 + 200 \times 3.99 + 200 \times 2.75 = \pounds1448$

Therefore Top Tees is cheaper.

b Shirts 4 U: $75 + 3.45 \times 380 = \pounds1386$ Top Tees: $100 + 200 \times 3.99 + 180 \times 2.75 = \pounds1393$ Therefore Shirts 4 U is cheaper.

- 13 a Yogurt $3 \times 250 = 750$, Banana $5 \times 150 = 750$ Kiwi $17 \times 90 = 1530$ Ratio $1530: 750: 750 \approx 1500: 750: 750 = 2:1:1$ This is a sensible recipe because the ratio means they can use whole fruits and whole cartons of yoghurt.
 - b 12 banana = 1800 g, 5 kiwi = 450 g, 5 yogurt = 250 g
 1800 : 450 : 1250 ≈ 1800 : 450 : 1350 = 4 : 1 : 3 Other answers are possible.

Review questions

- 1 £3.20
- **2 a** 150 g **b** 472.5 ml
- 3 48 mph
- 4 225 km
- 5 72 km/h
- 6 Totals are 40 and 60 giving 2 : 3 and a total of 100. 9 : 11 is a ratio of 45 : 55 so swap 10 and 15
- 7 **a** 1.73 ÷ 0.04 = 43.25 so 43 horses, 2.64 ÷ 0.065 = 40.61 so 40 cattle and 0.95 ÷ 0.01 = 95. Total 43 + 40 + 95 = 178 animals.
 - **b** Horses in field A = 43, Sheep in field B = $2.64 \div 0.01 = 264$, Cattle in field C, $0.95 \div 0.065 = 14.61$, so 14 cattle. Total 43 + 264 + 14 = 321 animals.
- **8** 3:2

С

- 9 65 blue counters
- **10 a** 22.5 kg **b** 30 kg **c** £19.80
- **11 a** 42:63 = 2:3 **b** 60 out of 200 = 30%

	Men	Women
40 years or over	70	54
Under 40 years	54	72

Chapter 11 – Geometry and measures: Perimeter and area

Exercise 11A

1	a 24 cm, 35 cm ²	b 28 cm, 33 cm ²
	c 36 cm, 45 cm ²	d 34 cm, 70 cm ²
	e 28 cm, 48 cm ²	f 14 cm, 10 cm ²
	g 26 cm, 42 cm ²	h 36 cm, 77 cm ²
2	a 20 cm, 24 cm ²	b 36 cm, 80 cm ²
	c 3 cm, 26 cm	d 7 cm, 20 cm

- **e** 3 cm, 18 cm² f 6 cm, 30 cm²
- **a** 530 m **b** 17400 m² 3
- $160 \times 70 = 11\ 200,\ 11\ 200 \div 10\ 000 = 1.12$ 4 hectares
- 19 bags 5

Exercise 11B

1	a 10 cm	b 12 cm	С	12 cm
	d 14 cm	e 12 cm	f	12 cm

- 2 18 m
- 3 No, the perimeter is 30 cm as two sides will touch.
- 4 False, it is 28 cm. The sum of the lengths of all the sides is 28 cm.
- **a** 30 cm² **b** 40 cm² 5 **c** 51 cm² **d** 35 cm^2 **e** 43 cm² f 51 cm² $g 48 \text{ cm}^2$ **h** 33 cm²
- 6 24
- The correct answer is 44 cm², the length of 7 the bottom rectangle is 6 cm (10 - 4).
- 72 cm² 8
- 9 48 cm
- **10** Yes, the area to paint is 9.1 m²

Exercise 11C

- **a** 6 cm², 12 cm **b** 120 cm², 60 cm 1 c 30 cm², 30 cm
- 40 cm² 2
- 84 m² 3
- **b** 55 cm² **c** 165 cm² **a** 21 cm² 4
- 5 $c 75 \text{ cm}^2$

- 6 Mai is correct with 32 cm, but Maggie is incorrect, the area should be 36 cm², it looks like she has forgotten to halve her calculations.
- Area of rectangle = $5 \times 12 = 60$ cm². The 7 two triangles are the same with one side 6 cm (half of 12) and the other half of (21 - 5)which is 8 cm. Area of one triangle = $\frac{1}{2} \times 6$ $\times 8 = 24$ cm². Area of two triangles = $4\overline{8}$ cm², so total area = 60 + 48 = 108 cm².
- 8 a 5.5 m^2 **b** 4

Exercise 11D

- **1 a** 21 cm² **b** 12 cm^2 **c** 14 cm² f 140 cm²
 - **d** 55 cm² **e** 90 cm²
- 2 64 cm^2
- 3 **a** 40 cm² **b** 65 m² c 80 cm²
- **b** 50 m² **a** 65 cm² 4
- For example: height 10 cm, base 10 cm; 5 height 5 cm, base 20 cm; height 25 cm, base 4 cm; height 50 cm, base 2 cm
- 6 **a** 1500 cm² **b** 1800 cm²
- 7 Triangle c; a and b each have an area of 15 cm² but c has an area of 16 cm².
- For example: Let vertical side be *T*, then 8 area = $\frac{1}{2} \times 2 \times T = T \text{ cm}^2$. The perimeter is 2 + T + other side, which is bigger than T. So Tim is correct.

Exercise 11E

- 1 a 96 cm² **b** 70 cm^2 $c 20 \text{ cm}^2$ **d** 125 cm² **e** 10 cm² **f** 112 m²
- 2 No, it is 24 cm^2 , she used the slanting side instead of the perpendicular height.
- 3 For example: If x = 20, then the base of each parallelogram is $\frac{1}{2}(20 - 4) =$ 8. This would make the area of each parallelogram $8 \times 5 = 40$, making the whole shape $4 \times 40 = 160$, which is incorrect. The correct value of *x* is 16.
- 4 **a** 500 cm² **b** 15

Exercise 11F

- 2 a 27.5 cm, 36.25 cm² b 33.4 cm, 61.2 cm² c 38.6 m, 88.2 m²
- 3 Any pair of lengths that add up to 10 cm For example: 1 cm, 9 cm; 2 cm, 8 cm; 3 cm, 7 cm; 4 cm, 6 cm; 4.5 cm, 5.5 cm
- 4 Shape c. Its area is 25.5 cm²
- 5 Shape a. Its area is 28 cm²
- 6 45 cm²
- **7** 2 cm
- 8 1.4 m²
- **9 b** 64 cm²

Exercise 11G

1 Top of head-tangent, eyebrows-arcs, nosesector, mouth-segment, face-circle

2	Diameter Radius	The width of a circle The distance from the centre to the edge of the circle
	Circumference	The perimeter of a circle
	Chord	A line joining two points
		on a circumference
	Tangent	A line that touches the
		circumference of the circle
		at one point only
	Arc	A part of the
		circumference of a circle
	Sector	A part of a circle lying
		between two radii and an arc
	Segment	A part of the area of a circle, lying between a chord and an arc

- 3 Students' own drawings
- 4 Students' own drawings

Exercise 11H

1 a 25.1 cm b 15.7 cm c 44.0 cm d 22.0 cm e 18.8 cm f 47.1 cm g 28.9 cm h 14.8 cm

- 2 a 6.3 cm b 8.2 cm c 5.3 cm d 7.5 cm
- 3 a 31.4 cm b 18.8 cm c 9.4 cm d 25.1 cm e 5.7 cm f 15.7 cm g 81.7 cm h 39.6 cm
- **4 a** 198 cm **b** 505
- 5 a A 188.5 m, B 194.8 m, C 201.1 m, D 207.3 m b 18.8 m
- 6 879.6 or 880 cm
- 7 a 37.7 cm b 3770 cm c 37.7 m d 37.7 km
- 8 100 cm
- 9 24.2 cm
- 10 15.9 cm
- 11 25.7 cm
- **12 a** Fir: 62.8 cm, ash: 75.4 cm, elm: 69.1 cm, oak: 81.7 cm
 - **b** The difference between the distances round the circumferences of two trees is 2π times the difference between their radii, or π times the difference between their diameters.
 - **c** 6.28 m
- **13 a** Perimeters of shapes A and B are both 25.1 cm

0

b 25.1 cm

14
$$4a = 2\pi r$$
, so $2a = \pi r$, therefore $r = \frac{2a}{\pi}$

- **15** 7
- **16** a $4\pi = 12.6$ cm b New radius of small circle will be 3, giving new perimeter of the whole shape of 12π , which is three times larger than 4π .

Exercise 111

1	а	78.5 cm ²	b	28.3 cm ²	С	7.1 cm ²
	d	50.3 cm ²	e	2.5 cm ²	f	19.6 cm ²
	g	530.9 cm ²	h	124.7 cm ²		
2	a	3.1 cm ²	b	5.3 cm ²	С	2.3 cm ²

- **d** 4.5 cm²
- **3 a** 50.3 cm² **b** 19.6 cm² **c** 153.9 cm² **d** 38.5 cm² **e** 28.3 cm² **f** 176.7 cm² **g** 66.5 cm² **h** 17.3 cm²

- **4 a** 9.1 cm² **b** 2000 cm² **c** 138 **d** 1255.8 cm² or 1252.9 cm² using
 - unrounded answer from **a**
 - e 744.2 cm² or 747.1 cm², using unrounded answer from **a**
- 5 3848.5 m²
- **6 a i** 56.5 cm **ii** 254.5 cm²
 - **b i** 69.1 cm **ii** 380.1 cm²
 - **c i** 40.8 cm **ii** 132.7 cm²
 - **d** i 88.0 cm ii 615.8 cm²
- 7 962.9 cm² (or 962.1 cm²)
- **8 a** 56.5 cm² **b** 19.6 cm²
- **9 a** 50.3 m² **b** 44.0 cm²

10
$$a^2 = \pi r^2$$
, so $r^2 = \frac{a^2}{\pi}$, therefore $r = \frac{a}{\sqrt{\pi}}$

- 11 Area of the square is 100 cm², Area of circle is $\pi \times 5^2 = 78.54$ cm², leaving the shaded area as 100 - 78.54 = 21.46 cm². Percentage of shaded area = $\frac{21.46}{100} \times 100 = 21.46\%$, which rounds to 21%, so Lewis is correct.
- **12 a** 2π or 6.3 cm²
 - **b** i 8π or 25.1 cm² iii 18π or 56.5 cm² iii 32π or 101 cm² **c** $a = 2\pi r^2$

Exercise 11J

- **1 a** 4π cm **b** 20π cm **c** 15π cm **d** 4π cm
- **2 a** 16π cm² **b** 25π cm² **c** 9π cm² **d** 81π cm²
- 3 25 cm
- 4 10 cm

5 Rory is correct. Area =
$$\pi \times \left(\frac{100}{\pi}\right)^2$$
, so

Area = $\pi \times \frac{100^2}{\pi^2} = \frac{10\,000}{\pi}$, so Alice was incorrect. She needed to put an extra zero in the numerator.

- **6 a** 12.5π cm² **b** 16π cm² **c** $(16\pi + 80)$ cm² **d** $(50\pi + 100)$ cm²
- 7 **a** 32π cm² **b** 16π cm² **c** 8π cm² **d** 4π cm²
- $\mathbf{8} \quad 18\pi 9\pi = 9\pi$
- **9 c**; $80 + \frac{1}{4}(\pi \times 8^2) = 80 + 16\pi$

Review questions

- 1 30 cm²
- 2 48 tiles
- 3 Area = $\frac{1}{2} \times 12 \times 9 = 54$ cm², Tilly has forgotten the $\frac{1}{2}$ in her calculation.
- **4** 8 cm
- 5 209 sheep

6
$$\pi d = 30$$
, so $d = \frac{30}{\pi}$, so radius $= \frac{15}{\pi}$, so
area $= \pi \times \left(\frac{15}{\pi}\right)^2 = \frac{225}{\pi} = 71.6 \text{ cm}^2$

- 7 Circle area = $\pi \times 25$ = 78.5 cm², Parallelogram area = 9×8 = 72 cm², difference = 78.5 - 72 = 6.5 cm², Andy is correct.
- **8 a** 2.5 cm
 - **b** Area of large circle = $10^2 \times \pi = 100\pi$ cm², area of two small circles is $2 \times \pi \times 2.5^2 =$ 12.5π cm², the shaded part = (100 - 12.5) $\pi = 87.5\pi$. The percentage shaded = $\frac{87.5\pi}{100\pi} \times 100 =$ 87.5%
- 9 $\frac{20}{\pi}$ cm

10 25.7 cm

Chapter 12 – Geometry and measures: Transformations

Exercise 12A

1	a 4 d 4	b 5 e 6	c 6
2	a 2 d 2	b 2 e 2	c 2

- 3 A, B, C, D, E, F, G, J, K, L, M, P, Q, R, T, U, V, W, Y
- 4 for example:

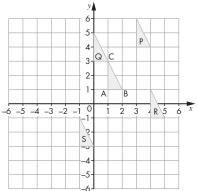
			nber o metry		es of
		0	1	2	3
Order of	1	D	А		
rotational symmetry	2	E		В	
	3				С

- 6 She is correct since the angle sum around the centre point is 360 and $360 \div 3 = 120$
- 7 Yes she is correct. A triangle can only have 1 or 3 lines of symmetry. If a triangle has 3 lines of symmetry it also has rotational symmetry of order 3, so this triangle must only have 1 line of symmetry. This will mean it has two angles identical and two equal sides, and hence an isosceles triangle.

Exercise 12B

- 1 Check students' translations.
- 2 Check students' translations.

3 **a** i
$$\begin{pmatrix} 1 \\ 3 \end{pmatrix}$$
 ii $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$ iii $\begin{pmatrix} 2 \\ -1 \end{pmatrix}$ iv $\begin{pmatrix} 5 \\ 1 \end{pmatrix}$
b i $\begin{pmatrix} -1 \\ -3 \end{pmatrix}$ ii $\begin{pmatrix} 3 \\ -1 \end{pmatrix}$ iii $\begin{pmatrix} -2 \\ 3 \end{pmatrix}$ iv $\begin{pmatrix} 3 \\ 3 \end{pmatrix}$
c i $\begin{pmatrix} -2 \\ -3 \end{pmatrix}$ ii $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$ iii $\begin{pmatrix} -5 \\ 4 \end{pmatrix}$ iv $\begin{pmatrix} 0 \\ 4 \end{pmatrix}$
d i $\begin{pmatrix} 3 \\ 2 \end{pmatrix}$ ii $\begin{pmatrix} -4 \\ 2 \end{pmatrix}$ iii $\begin{pmatrix} 5 \\ -4 \end{pmatrix}$ iv $\begin{pmatrix} -2 \\ -7 \end{pmatrix}$



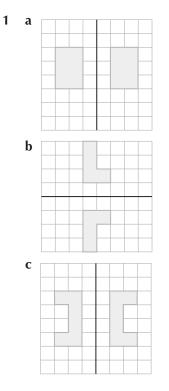
5 a
$$\begin{pmatrix} -3 \\ -1 \end{pmatrix}$$
 b $\begin{pmatrix} 4 \\ -4 \end{pmatrix}$ c $\begin{pmatrix} -5 \\ -2 \end{pmatrix}$
d $\begin{pmatrix} 4 \\ 7 \end{pmatrix}$ e $\begin{pmatrix} -1 \\ 5 \end{pmatrix}$ f $\begin{pmatrix} 1 \\ 6 \end{pmatrix}$
g $\begin{pmatrix} -4 \\ 4 \end{pmatrix}$ h $\begin{pmatrix} -4 \\ -7 \end{pmatrix}$
6 $10 \times 10 = 100 \text{ (including } \begin{pmatrix} 0 \\ 0 \end{pmatrix}$

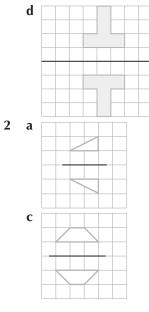
- 7 a Check students' designs for a Snakes and ladders board.
 - b because the ladders always mean moving up the board
 ii Because the snakes always mean moving down the board

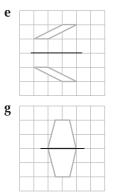
$$\mathbf{8} \quad \begin{pmatrix} -x \\ -y \end{pmatrix}$$

- 9 a Check student's diagram b
 - $\begin{array}{c} -300 \\ -500 \end{array}$
- 10 a Check student's diagram b
- 11 Multiply each part of the vector describing the move by -1

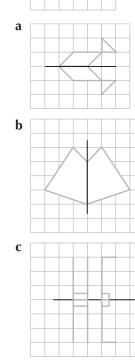
Exercise 12C

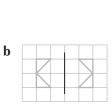


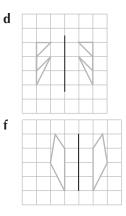




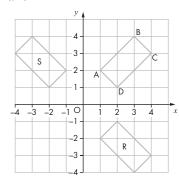




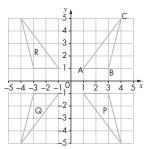




4 a-b

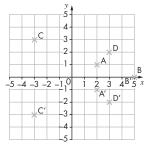


5 a–e

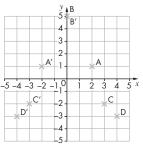


f Reflection in the *y*-axis

6 a-b

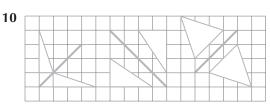


c *y*-value changes sign **d** (*a*, −*b*)

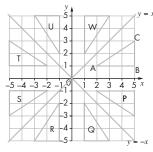


c *x*-value changes sign **d** (*-a*, *b*)

- 8 Possible answer: Take the centre square as ABCD then reflect this square each time in the line, AB, then BC, then CD and finally AD.
- **9** x = -1

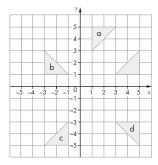


11 a-i

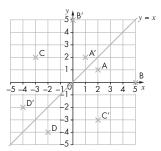


j A reflection in y = x

12 а-с



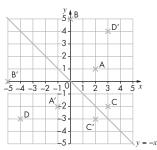
13 а-с



d Coordinates are reversed: *x* becomes *y* and *y* becomes *x*

e (*b*, *a*)

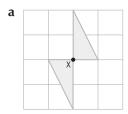
14 а-с

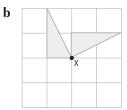


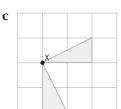
- d Coordinates are reversed and change sign, *x* becomes -*y* and *y* becomes -*x*e (-*b*, -*a*)
- 15 A reflection in the same line

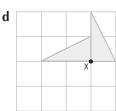
Exercise 12D

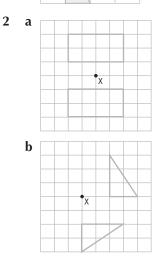
1

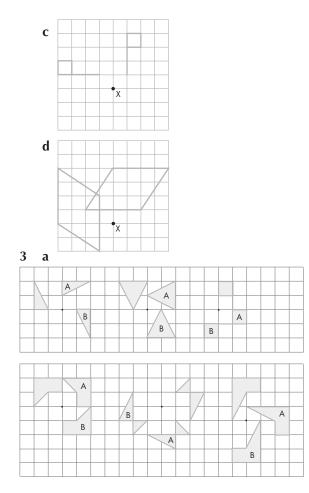




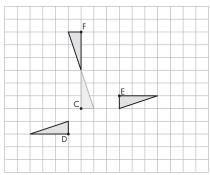


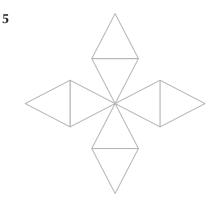




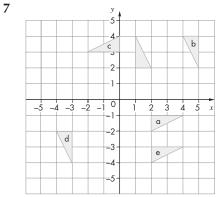


- b i Rotation 90° anticlockwiseii Rotation 90° clockwise
- 4 a-d



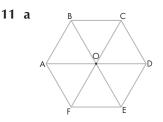


- **b** Rotate shape 60° around point B, then repeat another four times.
- 6 Possible answer: If ABCD is the centre square, rotate about A 90° anticlockwise, then rotate about A 180°, now rotate about new B 180°, and finally rotate about new C 180°.



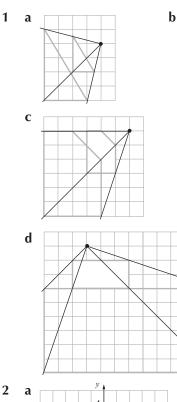
- **8** a Because the opposite rotations equal a total of 360°, which is the same point
 - b i 90° anticlockwise
 ii 270° anticlockwise
 iii 300° clockwise
 - iv 260° clockwise
- 9 Show by drawing a shape or use the fact that (*a*, *b*) becomes (*a*, -*b*) after reflection in the *x*-axis, and (*a*, -*b*) becomes (-*a*, -*b*) after reflection in the *y*-axis, which is equivalent to a single rotation of 180°.

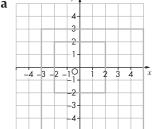
10 She is correct.

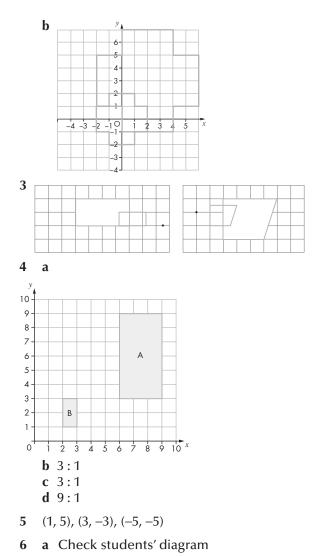


- b i Rotation 60°clockwise about O
 ii Rotation 120°clockwise about O
 iii Rotation 180°about O
 - iv Rotation 240° clockwise about O
- c i Rotation 60°clockwise about O ii Rotation 180°about O
- **12** Rotation 90° anticlockwise about (3, -2)
- **13** A rotation of the same angle but in the opposite direction. In this case the direction would be in the clockwise direction.

Exercise 12E







- **b** Rotation 180° around (–1, 2)
- 7 **a** Enlargement by scale factor -2 from centre of enlargement (1, 3) (1)
 - **b** Enlargement by scale factor $-\begin{pmatrix} 1\\3 \end{pmatrix}$ from centre of enlargement (1, 3)

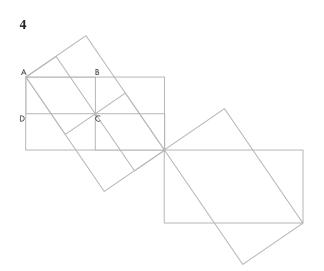
Exercise 12F

1 a-b Check students' diagram

c (-4, -3) and (-2, -1)

- 2 **a** (-5, 2) **b** (-5, -2) **c** Rotation of 180° about the origin.
- 3 A: translation $\begin{pmatrix} 1 \\ -2 \end{pmatrix}$, B: reflection in *y*-axis,

C: rotation 90° clockwise about (0, 0), D: reflection in x = 3, E: reflection in y = 4, F: enlargement by scale factor 2, centre (0, 1)



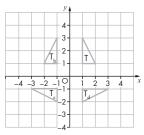
a T_1 to T_2 : rotation 90° clockwise about (0, 0) 5 **b** T_1 to T_6 : rotation 90° anticlockwise about (0, 0)

c T_2 to T_3 : translation

- **d** T_6 to T_2 : rotation 180° about (0, 0)
- e T_6° to T_5^{-1} : reflection in y-axis

f
$$T_5$$
 to T_4 : translation $\begin{pmatrix} 4 \\ 0 \end{pmatrix}$

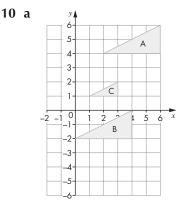
6 a-d



- **e** T_d to T: rotation 90° anticlockwise about (0, 0)
- 7 (3, 1)
- For example: Reflection in *x*-axis, 8

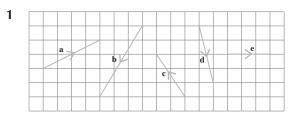
, rotation 90°clockwise translation about (0, 0)

9 For example: Translation , reflection in x-axis, rotation 90° clockwise about (0, 0)

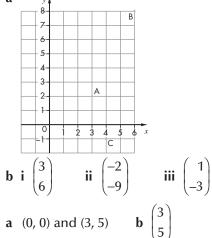


- **b** enlargement scale factor 2 from (0, -2)
- 11 No, the two reflections will result in the original orientation.

Exercise 12G





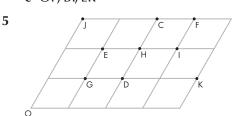


- 3 **a** (0, 0) and (3, 5) b
- 4 **a** (2, 2), (6, 1), (6, 4) **b** (-6, -1), (-2, -2), (-2, 1)
- 5 (1, 5)
- **b** (6, -6) 6 **a** (3, 8)

Exercise 12H

- **a** Any three of: \overrightarrow{AC} , \overrightarrow{CF} , \overrightarrow{BD} , \overrightarrow{DG} , \overrightarrow{GI} , \overrightarrow{EH} , 1 HI, IK
 - **b** Any three of: \overrightarrow{BE} , \overrightarrow{AD} , \overrightarrow{DH} , \overrightarrow{CG} , \overrightarrow{GJ} , \overrightarrow{FI} , \overrightarrow{IK}

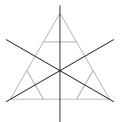
- c Any three of: AO, CA, FC, IG, GD, DB, KJ, JH, HE
- **d** Any three of: \overrightarrow{BO} , \overrightarrow{EB} , \overrightarrow{HD} , \overrightarrow{DA} , \overrightarrow{JG} , \overrightarrow{GC} , \overrightarrow{KI} , \overrightarrow{IF}
- 2 a 2a b 2b c a + b d 2a + b e 2a + 2b f a + 2b g a + b h 2a + 2b i 3a + b j 2a k b l 2a + b
- **3 a** Equal **b** \overrightarrow{AI} , \overrightarrow{BJ} , \overrightarrow{DK}
- 4 **a** $\overrightarrow{OJ} = 2\overrightarrow{OD}$ and parallel **b** \overrightarrow{AK} **c** \overrightarrow{OF} , \overrightarrow{BI} , \overrightarrow{EK}

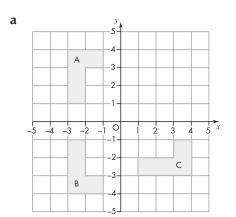


- a Lie on same straight line
 b All multiples of a + b and start at O
 c 4a + 2b
- a Equal but in opposite directions
 b Any three of: DA, EF, GJ, FI, AH
- **9 a** Opposite direction and $\overrightarrow{AB} = -\frac{1}{2}\overrightarrow{CK}$
 - **b** \overrightarrow{BJ} , \overrightarrow{CK}
 - $\mathbf{c} \ \overline{\mathsf{EB}}, \overline{\mathsf{GO}}, \overline{\mathsf{KH}}$
- 10 a i 3a + 2b ii 3a + b iii 2a - b iv 2b - 2a
 - **b** \overrightarrow{DG} and \overrightarrow{BC}

Review questions

- **1** a 3
 - **b** There will be 3 lines all through a vertex and the opposite side's midpoint.



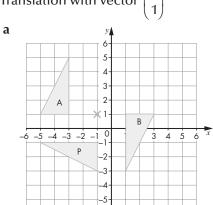


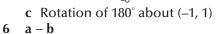
- **b** 90° anticlockwise rotation about (0, 0)
- **3** 180° rotation about (0, 0)

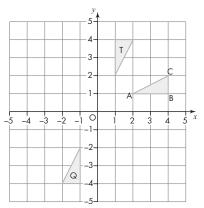
2

5

4 Translation with vector $\begin{bmatrix} 4 \\ 1 \end{bmatrix}$







- c Rotation of half a turn around the origin
- 7 (9, 0), (11, -3), (2, -1)
- 8 i -b ii -a iii b iv a v a + b vi a b
- 9 Students' diagram.
- **10** For example: Reflection in the *y* axis, reflection in the line *y* = 1

Chapter 13 – Probability: Probability and events

Exercise 13A

1	a $\frac{1}{6}$	b $\frac{1}{6}$	$c \frac{1}{2}$	d $\frac{1}{13}$	$e \frac{1}{4}$
	$f \frac{1}{2}$	g 1	h $\frac{1}{26}$	i $\frac{1}{13}$	j 0
2	a 0		b	1	
3	a $\frac{1}{10}$	b $\frac{1}{2}$	$\mathbf{c} \frac{2}{5}$	d $\frac{1}{5}$	e $\frac{3}{5}$
4	a $\frac{1}{2}$	b	$\frac{1}{3}$	$c \frac{1}{6}$	
	$\frac{1}{50}$				
6	a $\frac{1}{13}$	b - 1	$\frac{1}{3}$	$\mathbf{c} \frac{1}{2}$	d $\frac{1}{26}$
7	a i $\frac{12}{25}$	ii	$\frac{7}{25}$	iii $\frac{6}{25}$	
	b They c All po			s are used	d.
8	a AB, A	C, AD, /	AE, BC, B	D, BE, CD	, CE, DE
	b 1	c $\frac{1}{10}$	d 6	e $\frac{3}{5}$	f $\frac{3}{10}$
9	There n	night no	t be the	same nur	nber of

9 There might not be the same number of boys as girls in the class.

10 Class U

Exercise 13B

1	a $\frac{19}{20}$	b 55%	c 0.2
2	a i $\frac{3}{13}$		$\frac{10}{13}$
	b i $\frac{1}{4}$	ii	$\frac{3}{4}$
	c i $\frac{2}{13}$	ii	$\frac{11}{13}$
3	a $\frac{1}{2}$	b 1	c $\frac{1}{3}$
4	a $\frac{6}{11}$	b $\frac{5}{11}$	c $\frac{6}{11}$
5	a $\frac{1}{2}$	b $\frac{1}{5}$ c $\frac{4}{5}$	d $\frac{7}{10}$
6	a $\frac{7}{15}$	b $\frac{2}{15}$ c $\frac{13}{15}$	d $\frac{8}{15}$
	e $\frac{7}{15}$	f 0	

- 7 P(Noah will lose) = $\frac{1}{2}$ and P(Phoebe will lose) = $\frac{1}{3}$, so P(Noah will not lose) = $\frac{1}{2}$ and P(Phoebe will not lose) = $\frac{2}{3}$. Phoebe has a better chance of not losing as $\frac{2}{3} > \frac{1}{2}$
- 8 Because it might be possible for the game to end in a draw.

9 a i
$$\frac{1}{4}$$
 ii $\frac{3}{4}$
b i $\frac{3}{11}$ ii $\frac{8}{11}$

10 35%

11 0.5

Exercise 13C

1	a $\frac{1}{6}$	b $\frac{1}{6}$	c $\frac{1}{3}$	
2	a $\frac{1}{4}$	b $\frac{1}{4}$	$\mathbf{c} \frac{1}{2}$	
3	a $\frac{2}{11}$	b $\frac{4}{11}$	c $\frac{6}{11}$	
4	a $\frac{1}{3}$	b $\frac{2}{5}$ c $\frac{11}{15}$	d $\frac{11}{15}$	e $\frac{1}{3}$
5	a 0.8	b 0.2		
6	a $\frac{17}{20}$	b $\frac{2}{5}$	c $\frac{3}{4}$	

7 Because these are not mutually exclusive events and probability cannot exceed 1.

8
$$\frac{3}{2}$$

- 9 The probability for each day stays the same, at $\frac{1}{4}$.
- **10 a** The choices of drink and snack are not mutually exclusive.
 - **b** (C, D), (T, G), (T, R), (T, D), (H, G), (H, R), (H, D)
 - c i (C, D) = 0.12, (T, G) = 0.15, (T, R) = 0.05, (T, D) = 0.3, (H, G) = 0.09, (H, R) = 0.03, (H, D) = 0.18
 - ii The total is 1 as all the outcomes are exhaustive.

Exercise 13D

1	a B	bВ	c C	d A
	еB	f A	g B	h B

- **2 a** 0.2, 0.08, 0.1, 0.105, 0.148, 0.163, 0.1645 **b** 6 **c** 1 **d** $\frac{1}{6}$
- **a** 0.095, 0.135, 0.16, 0.265, 0.345 **b** 40
 - **c** No; all numbers should be close to 40.
- **4 a** 0.2, 0.25, 0.38, 0.42, 0.385, 0.3974 **b** 79
- 5 a Caryl, threw the greatest number of times.
 - **b** 0.39, 0.31, 0.17, 0.14
 - **c** Yes; all the relative frequencies should be close to 0.25.
- 6 Thursday; the day with the highest relative frequency
- 7 The missing top numbers are 4 and 5, the bottom two numbers are both likely to be close to 20.
- 8 Although he might expect the probability to be close to $\frac{1}{2}$, giving 500 heads, the actual number of heads is unlikely to be exactly 500, but should be close to it.
- **9** Roza is correct, as the expected numbers are: 50, 12.5, 25, 12.5. Sylwester has not taken into account the fact that there are four red sectors.

Exercise 13E

1	а	$\frac{1}{6}$			b :	25			
2	а	$\frac{1}{2}$			b	10	00		
3			ii <u>1</u> 13 ii 40				1 4 130		v $\frac{1}{52}$ v 10
4	a	$\frac{1}{37}$			b !	5			
5	a	150	b 1	00		С	250	(0 1
6	a	167			b	83	3		
7	a	0.6			b	12	0		
8	а								
	Sco	ore	1	2	3		4	5	6
		ected urrences	10	10	10)	10	10	10
	b								

 $\frac{1 \times 10 + 2 \times 10 + 3 \times 10 + 4 \times 10 + 5 \times 10 + 6 \times 10}{60} = \frac{210}{60} = 3.5$

- **c** Find the average of the scores, which is $\frac{21}{6} = 3.5$
- **9 a** 0.111 **b** 40
- 10 281 days
- 11 Multiply the number of plants by 0.997.
- **12** 400

Exercise 13F

- **1 a** 48 **b** 12
- **2** 40
- 3 a (BS, BT), (BS, RT), (BS, GT), (WS, BT), (WS, RT), (WS, GT), (GS, BT), (GS, RT), (GS, GT)

b
$$\frac{7}{9}$$

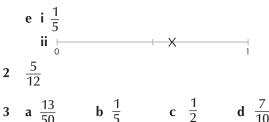
- 4 $10^9 = 1\ 000\ 000\ 000\ (1\ billion)$
- 5 a ¹/₂
 b HHH, HHT, HTH, HTT, THH, THT, TTH, TTT ³/₈
- **6** 20
- **7** $2^5 = 32$
- **8** 56
- 9 $26^2 \times 10^2 = 67\ 600 > 50\ 000$
- **10** a $2 \times 26 \times 999\ 999 \times 4 = 207\ 999\ 792$ b $\frac{1}{4}$
- **11 a** 24 **b** $\frac{1}{6}$
- 12 $\frac{11}{21}$. Number of possible permutations is 21, £2 + any coins = 6, £1 + any coin other than £2 = 5, etc, so total is 6 + 5 + 4 + 3 + 2 + 1 = 21, Only the ones with a £2 or a £1 in will give a total greater than £1 = 11 ways
- **13 a** 6, 16, etc.. up to 196 which is 20 plus 60, 61 up to 69, which is 9 (66 already counted) plus 160, 162 up to 169 which is 9 (166 already counted) giving a total of 38
 - **b** $\frac{38}{200} = \frac{19}{100}$
 - c $\frac{11}{200}$
- **14 a** Key pad A, 10⁴ = 10 000; Keypad B 13⁴ = 28 561

b
$$3 \times 10^3 = 3000$$
 c $\frac{1}{24}$

15 a i 5040 **ii** 2.43×10^{18} (3 sf) **b** This depends on your calculator but $69! = 1.71 \times 10^{98}$, which is about the number of atoms in 1 quintillion universes. (Look this term up if you're not sure what it means).

Review questions

- **1 a** April and May
 - **b** Daffodil
 - c February
 - d Crocus



- **4** a 1
 - **b** There are five possible outcomes and only two of them are 2, so the probability is $\frac{2}{5}$.
- **5 a** 0.5
 - **b** yes, as you would expect all the probabilities to be close to 0.25
- **6 a** $\frac{3}{8}$ **b** 12
- 7 **a i** 0.8
 - **b** No, as $P(six) = \frac{1}{6}$, so Tom is likely to throw 10 sixes

ii 12

8 a

Colour	White (W)	Green (G)	Blue (B)
Relative frequency	$\frac{1}{4}$	$\frac{9}{20}$	$\frac{3}{10}$

- **b** The second table, as there were more trials
- **9 a** (H, 1), (H, 2), (H, 3), (H, 4), (H, 5), (H, 6), (T, 1), (T, 2), (T, 3), (T, 4), (T, 5), (T, 6)
 - **b** $\frac{2}{12} = \frac{1}{6}$ as (H, 3) scores 6 and (T, 6) scores 6
- **10** $\frac{3}{6} = \frac{1}{2}$. There are 6 combinations, 2 + 14 = 16, 11 + 14 = 25 and 14 + 22 = 36 give square numbers

11 a $10^3 = 1000$ **b** $\frac{1}{100}$ **c** Trial and improvement $9^5 = 59049$

Chapter 14 – Geometry and measures: Volumes and surface areas of prisms

Exercise 14A

1 a

Name	Number of faces (F)	Number of vertices (V)	Number of edges (E)
Cuboid	6	8	12
Square-based pyramid	5	5	8
Tetrahedron	4	4	6
Octahedron	8	6	12
Triangular prism	5	6	9
Hexagonal prism	8	12	18
Hexagon based pyramid	7	7	12

b F + V = E + 2

- 2 a i 6, 12 ii 24, 96 b i 2 ii 4 iii 8 c ii 2, 4 ii 18, 108 d i 3 ii 9 iii 27
- 3 She might have calculated this by multiplying 5 by 5 by 4 to get 100.
- **4** 65 cm²
- 5 6
- 6 David is correct. A pentagon has 5 sides, so a pentagonal prism has 5 + 5 + 5 edges, and 2 + 5 faces. 5 + 5 + 5 + 2 + 5 = 22

Exercise 14B

1	a i 198 cm ³	ii 234 cm ²
	b i 90 cm ³	ii 146 cm ²
	c i 1440 cm ³	ii 792 cm ²
	d i 525 cm ³	ii 470 cm ²

- **2** 24 litres
- **3 a** 160 cm³ **b** 480 cm³ **c** 150 cm³

- 4 a i 64 cm³
 b i 343 cm³
 c i 1000 mm³
 d i 125 m³
 e i 1728 m³
 ii 96 cm²
 ii 294 cm²
 ii 600 mm²
 ii 150 m²
 ii 864 m²
- **5** 86
- **6 a** 180 cm³ **b** 5 cm **c** 6 cm **d** 10 cm **e** 81 cm³
- 7 320 litre is equivalent to 320×1000 cm³ = 320 000 cm³. V = lwh, so 65×31 $\times h = 320 000$, so $h = \frac{32000}{(65 \times 31)} = 158.8$ cm.
- 8 Volume = base area × height, so base area = volume/height = $\frac{168}{3.5}$ = 48 m². So Peter is only correct if he has rounded to the nearest ten.
- **9 a** 3 cm **b** 5 m **c** 2 mm **d** 1.2 m
- **10 a** 148 cm³ **b** 468 cm³
- 11 If this was a cube, the side length would be 5 cm, so total surface area would be $5 \times 5 \times 6 = 150$ cm²; so this particular cuboid is not a cube.
- **12** 600 cm²

Exercise 14C

- **1 a i** 21 cm² **ii** 63 cm³ **b i** 48 cm² **ii** 432 cm³ **c i** 36 m² **ii** 324 m³
- **2 a** 432 m³ **b** 225 m³ **c** 1332 m³
- 3 a

1.2 m

- **b** About $3\frac{1}{2}$ hours
- 4 $V = (1.5 + 3) \div 2 \times 1.7 \times 2 = 7.65 \text{ m}^3$
- 5 $27 = 3 \times 3 \times 3$, $27 + 37 = 64 = 4^3$, 4 3 = 1. Hence the side length is 1 small cube longer, hence 2 cm longer
- **6 a i** 21 cm³ **ii** 54 cm² **b i** 210 cm³ **ii** 270 cm²
- 7 10.2 tonnes
- 8 She was silly because 26 880 is simply all the dimensions multiplied together. The volume is 672 cm³.

Exercise 14D

1 a i 226 cm³ **ii** 207 cm²

	b i 14.9 cm ³	ii 61.3 cm ²
	c i 346 cm ³	ii 275 cm ²
	d i 1060 cm ³	ii 636 cm ²
2	a 251 cm ³	b 445 cm ³
	c 2150 cm ³	d 0.25 m ³

- 3 Volume = $\pi \times (0.3)^2 \times 4.2 = 0.378\pi$ Cost = $0.378 \times \pi \times \pounds 67.50 = \pounds 80.16$ which is $\pounds 80$ to 2 sf
- 4 1.23 tonnes
- 5 665 cm³
- 6 Label should be less than 10.5 cm wide so that it fits the can and does not overlap the rim and more than 23.3 cm long to allow an overlap.
- 7 Volume = $\pi \times 32.5^2 \times 100 = 331\ 831\ cm^3$ 1 litre = 1000 cm³ volume = 331 831 ÷ 1000 = 331.831 litres = 332 litres (3 sf)
- 8 There is no right answer. Students could start with the dimensions of a real can. Often drinks cans are not exactly cylindrical. One possible answer is height of 6.6 cm and diameter of 8 cm.
- 9 About 127 cm
- **10** Volume of $A = 2^2 \times \pi \times 5 = 20\pi$, volume of $B = 1^2 \times \pi \times 21 = 21\pi$, B has the larger volume.
- 11 146 cm³
- 12 78 m³ (78.3 m³)
- 13 327 litres

2.2 r

10 m

Review questions

- **1 a** 60 cm³ **b** 104 cm²
- 2 38 cm²
- 3 Arrange small boxes so that the 8 by 8 part fills one layer in the 32 by 32 box, giving 4×4 boxes. Then this will give 5 layers of 4×4 boxes giving $5 \times 4 \times 4 = 80$ boxes.
- 4 Area of circular end = $\pi r^2 = \pi \times 4.5^2 =$ 63.617251, curved surface area = $\pi dh = \pi \times$ 9 × 21 = 593.76101, total area = 2 × 63.617251 + 593.76101 = 720.99551 = 721 cm² (nearest whole number)
- 5 5740 cm³ (to 3 sf)
- 6 610 g (2 sf)

- 7 600 cm³
- **8** 360 g

Chapter 15 – Algebra: Linear equations

Exercise 15A

1	a $x = 4$	b $w = 14$
	c $x = 5$	d $x = 6$
	e $z = 24$	f $x = 2.5$

2 Any valid equation such as 4x = 16 or x + 3 = 7

3	a 6	b 9	c 7
	d 3	e 1	f 5
	g 4	h 2	i 8

Exercise 15B

1	a $x = 2$	b $x = 13$
	c $x = 13$	d $y = 6$
	e <i>x</i> = 9	f $x = 5$
	g $t = 18$	h $y = 24$
	i k = 18	j $h = 40$

3 27p

Exercise 15C

$\mathbf{h} x$	c = 0
	h x

- **2 a** -4 **b** 15
- 3 Any valid equation such as 3x + 8 = 2, 6x + 20 = 8
- 4 a Betsy
 - **b** Second line: Amanda subtracts 1 instead of adding 1; fourth line: Amanda subtracts 2 instead of dividing by 2.

Exercise 15D

1	a $k = 5$	b $h = 28$	c $w = 5$
	d $x = 35$	e $y = 33$	f $f = 23$

- **2 a** 33 **b** 48
- **3 a** x = 2 **b** x = 7 **c** $y = 2\frac{4}{5}$ **d** y = 1 **e** $x = 11\frac{1}{2}$ **f** $t = \frac{1}{5}$
- 4 Any valid equations

- 5 a Anwar
 - **b** First line: Brody adds 4 instead of multiplying by 5.

Second line: Brody adds 5 instead of multiplying by 5.

Fourth line: Brody subtracts 2 instead of dividing by 2.

6 a
$$\frac{x+10}{5} = 9.50$$

b £37.50

7 **a** $\frac{8}{3}$ **b** Student's own working

Exercise 15E

1	a $\frac{1}{2}$	b $1\frac{1}{5}$	c 2	d -2
	e −1	f -2	g -2	h –1

- 2 Any values that work, e.g. a = 2, b = 3 and c = 30.
- **3** 3 cm
- **4** 5
- 5 Multiplying out the brackets and collecting like terms gives 4x 24 = 0 which has the solution x = 6.
- **6** 168°

Exercise 15F

- **1 a** x = 2 **b** y = 1 **c** a = 7 **d** t = 4 **e** p = 2 **f** k = -1**g** m = 3 **h** s = -2
- 2 3x 2 = 2x + 5, x = 7
- **3 a** d=6 **b** x=11 **c** y=1**d** h=4 **e** b=9 **f** c=6
- 4 **a** 6x + 3 = 6x + 10; 6x 6x = 10 3; 0 = 7, which is obviously false. Both sides have 6x, which cancels out.
 - **b** Multiplying out the brackets gives 12x + 18 = 12x + 18 which is true for all values of *x*.
- 5 8x + 7 + x + 4 = 11x + 5 x 4, x = 10, so the total value of silver coins is £1.90
- 6 70 cm²
- **7** a 15
 - **b** -1
 - **c** 2(n+3), 2(n+3) 5

d 2(n+3) - 5 = n, 2n + 6 - 5 = n, 2n + 1 = n, n = -1

8 4x + 18 = 3x + 1 + 50, x = 33. Large bottle 1.5 litres, small bottle 1 litre

Review questions

- **1 a** x=6 **b** x=9 **c** $x=\frac{2}{3}$ **d** x=-5 **e** x=72
- **2** 3 years
- **3** x = -6
- **4 a** x = -3 **b** x = -3 **c** x = -3
- 5 C
- **6** 8
- 7 Length is 5.5 m, width is 2.5 m and area is 13.75 m². Carpet costs £123.75
- 8 a All the sides of a square are equal b $42\frac{1}{4}$ m²
- **9** *x* = 10
- 10 14 cm
- **11 a** B: $\frac{3}{8}x$, C: $\frac{3}{8}x$, D: $\frac{1}{4}x$ **b** $\frac{3}{8}x = 300$, x = 800 cars

$$\mathbf{c}: \frac{1}{4} x = 500, x = 2000 \text{ cars}; 750 \text{ exit at B}$$

12 No, as x + x + 2 + x + 4 + x + 6 = 360 gives $x = 87^{\circ}$ so the consecutive numbers (87, 89, 91, 93) are not even but odd

Chapter 16 – Ratio and proportion and rates of change: Percentages and compound measures

Exercise 16A

1	a $\frac{2}{25}$	b $\frac{7}{20}$	c $\frac{9}{10}$
2	a 0.27	b 0.85	c 0.13
3	a $\frac{3}{25}$	b $\frac{2}{5}$	c $\frac{9}{20}$
4	a 29%	b 60%	c 125%
5	a 28%	b 30%	c 95%

	d	34%	e 2	27.5%	f	87.5%		
6	a	0.6	b(0.075	С	0.76		
	d	0.3125				0.125		
7	n	one						
8	a	77%	b 3	39%	С	63%		
9	27	7%						
10	a	50%	b 2	20%	С	80%		
11	а	87.5%, 75%	%, 6	2.5%, 50%	6,2	25%		
	b	12.5%						
12	a	$\frac{3}{5}$ k	b 0.	6 c	6	60%	d	60%
13		63%, 83%, English	. 39°,	%, 62%, 7	7%			
14	10)%						
15	34	4%, 0.34, <u>17</u>	; 85	%, 0.85, 1/2	7;	7.5%, 0	.075	$5, \frac{3}{40};$
		5%, 0.45, $\frac{9}{20}$						40
	$\frac{2}{2}$; 84%, 0.84	$, \frac{21}{25}$; 45%, 0.4	5, -	$\frac{9}{20}; 37.5$	%,	
	5	375, $\frac{3}{8}$	23			20		
16		₅ or 90%						
Exe	ero	cise 16B						
1	a	0.88 b 0).3	c 0.25	C	0.08	e	1.15
2	a	78% b 4	0%	c 75%	C	5%	e	110%
3	d	£45 1.125 kg £0.12 33.88 min	e h	2.94 m	t i	f 37.8 i £7.60	cm)	
4	a	504		b 4	8			
5	£2	2410						
6	a	86%		b 2	15			
7	85	320						

- 7 8520
- **8** 287
- **9** A total of 91% were allocated, leaving 9% or 8100 tickets for celebrities
- **10** 990
- 11 Mon: 816, Tue: 833, Wed: 850, Thu: 799, Fri: 748

12	а	£3.25	b	2.21 kg	С	£562.80
	d	£6.30	e	42.93 m	f	£24

- **13** 480 cm³ nitrogen, 120 cm³ oxygen
- **14** 13

15 £270

16 More in 2014 as it was 3% of a higher amount than in 2013

Exercise 16C

- **1 a** 1.1 **b** 1.03 **c** 1.2 **d** 1.07 **e** 1.12
- **2 a** 0.92 **b** 0.85 **c** 0.75 **d** 0.91 **e** 0.88
- **3 a** 391 kg **b** 824.1 cm **c** 253.5 g **d** £143.50 **e** 736 m **f** £30.24
- **4 a** 731 m **b** 83.52 g **c** 360 cm **d** 117 min **e** 81.7 kg **f** £37.70
- **5** 448
- 6 No, as the total is £101. She will save £20.20, which is less than the £25 it would cost to join the club.
- 7 A 7% pay rise. 7% is £1925 per year; £150 per month is £ 1800 per year.
- **a** £6.13 (£6.125) **b** *x* × 0.025
 - **c** $y \div 1.175 \times 1.2$
- 9 Offer B is the better offer:

Offer A gives 360 grams for £1.40, i.e. 0.389 pence per gram.

Offer B gives 300 grams for £1.12, i.e 0.373 pence per gram.

Or: Offer A is 360 for 1.40 = 2.6 g/p, offer B is 300 for 1.12 = 2.7 g/p.

- **10** c Both the same as $1.05 \times 1.03 = 1.03 \times 1.05$
- **11 a** Shop A as $1.04 \times 1.04 = 1.0816$, so an 8.16% increase.
- 12 £425.25

13 $0.9 \times 1.10 = 0.99$ (99%)

Exercise 16D

1	e 41.7%	<pre>b 60.6% f 60% j 8.3%</pre>	g 20.8%	h 10%
2	32%			
3	6.5%			
4	33.7%			

- **5 a** 49.2% **b** 64.5% **c** 10.6%
- **6** 4.9%

- 7 90.5%
- 8 Stacey had the greater percentage increase. Stacey: $(20 - 14) \times 100 \div 14 = 42.9\%$ Calum: $(17 - 12) \times 100 \div 12 = 41.7\%$
- **9** Yes, as 38 out of 46 is over 80% (82.6%)
- **10** Let z = 100. y = 75, $x = 0.6 \times 75 = 45$, so x is 45% of z
- 11 Let *z* be 100, *x* = 60. If *x* is 75% of *y*, *y* = 80, so *y* is 80% of *z*.
- **12** 30% of 4800 = 1440. 1.2 × 4800 = 5760. 70% of 5760 = 4032. 4032 1440 = 2592.

2592 ÷ 1440 = 1.8, so the increase in numbers owning a mobile phone is 180%.

13 31 ÷ 26 = 1.19 which is a 19% increase. 31% is 5% more of the total votes cast than 26%

Exercise 16E

1	a £260	b £307.50	С	£323.75	d	£289
2	a £7.50	b £9.05	С	£5.80	d	£10.75
3	a 38 h	b $41\frac{1}{2}$ h	С	35 h	d	40 h
4	a Fewer hours			More pa	уp	er week
5	a £540		b	£702		
6	£6.90					
7		= 45, 45 ÷ 6 = < 7.50) ÷ 7.50				
8	$\pm 1\frac{1}{4}x \text{ or } \pm \frac{5}{4}$	$\frac{5x}{4}$				
9	Pay is £442	2.50 tax is £8	8.50	0, NI is 44	12.5	50 -

- $88.50 327.45 = 26.55, 26.55 \div 442.5 = 0.06,$ so the NI rate is 6%
- **10** 407 factorises to 1 × 407 or 11 × 37, so Antoine works 37 hours a week at £11 per hour.

Exercise 16F

- 1 0.75 g/cm³
- **2** 4 Pa
- 3 8.33 g/cm³
- 4 2.5 N
- 5 32 g
- 6 5 m²
- 7 120 cm³

- **8** 156.8 g
- 9 The 30 cm \times 20 cm face
- **10** The handles exert greater pressure as there is less area in contact with your hands.
- **11** To reduce the pressure they exert, which helps prevent them sinking into soft sand.
- 12 a 19.3 kg
 - b 19.3 kg. The scale shows the mass, which is the same
 c (a) 9650 Pa, (b) 38 600 Pa
- 13 The first statue is a fake
- 14 The 400 g piece has a bigger volume by 1 cm³
- **15** If the soles of the shoes and slippers are the same size he will exert the same pressure
- 16 They are smooth and narrow so cut through snow. They have a big area so they don't push into the snow
- 17 Lay down and slide. Less pressure is exerted on the ice
- **18** Each wheel takes some of the mass so the pressure on the road or a weak bridge is less.
- **19** A, D, C, B. If they have the same mass, the one with the largest area will exert the least pressure.
- 20 a Same, as the area is the sameb Cone, as all the mass is concentrated on the point which has negligible area.
- **21** 0.34 m³
- $22 \hspace{0.1in} 1 \hspace{0.1in} m \times 0.8 \hspace{0.1in} m \times 0.5 \hspace{0.1in} m$
- 23 a True b False c False

Review questions

- 1 £144.00
- **2** £208.25
- **3** £317.55
- **4** £8.90
- 5 France. Their speed limit is equivalent to 75 mph.
- 6 a 1.73 ÷ 0.04 = 43.25 so 43 horses, 2.64 ÷ 0.065 = 40.61 so 40 cattle and 0.95 ÷ 0.01 = 95. Total 43 + 40 + 95 = 178 animals.

- b Horses in field A = 43, Sheep in field B = 2.64 ÷ 0.01 = 264, Cattle in field C, 0.95 ÷ 0.065 = 14.61, so 14 cattle. Total 43 + 264 + 14 = 321 animals
- 7 25%
- **8** £8.98
- 9 8 g/cm³
- **10** 0.88
- 11 240 Pa
- **12** Shop B
- **13 a** £9.00 **b** £13.20
- 14 £322
- **15** Yes, the council exceeded the promise which was for a maximum of 1200 unemployed people.
- **16** The 20% reduction will reduce the prices by more than the original VAT because they will be reducing prices by 20% of a bigger amount.
- **17 a** 150 men, 100 women **b** 12%
- $18\ 13\%$

Chapter 17 – Ratio and proportion and rates of change: Percentages and variation

Exercise 17A

1	а	£400	b	£90	С	£499.46 d £12.80
2	а	10.5 g	b	11.03 g	С	12.16 g d 14.07 g
3	а	2550		b 2168		c 1331
4	a	£6800		b £5440		c £3481.60
5	a	i 51 980		ii 84 752	2	iii 138 186
6	а	8 years			b	12 years
7	12	2 years				
8	а	£14 272.2	27		b	20 years
9		i 1.9 m ii 1.6 m iii 1.2 m 10th Aug	illi illi	on litres	5	
10	a	21 years			b	21 years

Exercise 17B

- 1 a 800 g b 250 m c 60 cm d £3075 e £200 f £400
- **2** 80
- 3 T-shirt £8.40, Tights £1.20, Shorts £5.20, Sweater £10.75, Trainers £24.80, Boots £32.40
- **4** £833.33
- 5 £300
- **6** 240
- 7 £350
- 8 4750 blue bottles
- **9** £22
- 10 a £1600
 - **b** Yes. With 10% cut each year he earns $\pm 1440 \times 12 \pm \pm 1296 \times 12 = \pm 17\ 280 \pm \pm 15\ 552 = \pm 32\ 832$. With an immediate 14% cut he earns $\pm 1376 \times 24 = \pm 33\ 024$, so he made the correct decision.

Exercise 17C

1	a	£3.40	b	17		c 12
2		100 cm				20 inches
3	a	82 inches 12 30	is l	onge	r b	$33\frac{1}{3}$ hours
4	a	150			b	6
5	a	22.5			b	12
6	a	175 miles			b	8 hours
7	a	£66.50			b	175 kg
8	a	44			b	84 m ²
9	a	50				
10	17	7 minutes 3	80 s	econ	ds	
11						allons is 27.3 litres les per litre
Ex	ero	cise 17D				

1	a 12.5 watts	b 2.5 m
2	8 hours	
3	a 5 cm	b 10 cm
4	a 625 cm ³	b 0.625 bar
5	a 6	b 12.5

- 6 a 27 min 31.2 sec b 34.4 km/h
- **7** a £150 b 36
 - **a** 3 °C **b** 12 km

8 9

X	8	24	16
y	1	$\frac{1}{3}$	$\frac{1}{2}$

10 a 120 miles **b** 7.5 miles

Review questions

- 1 £2120
- 2 £19 728
- **3** £112.50
- 4 a 37p b 3 hours c 20 minutes d 36 kg e 1 hour f 16 hours g Three days h 21 minutes i 2 hours j 6:00 pm
 5 She should choose A
 6 £8357.35
- 7 **a** 3 days **b** 2 days
- **8** £8.60
- **9** £38.50
- 10 a 6
 b 100

 11 a 4
 b 32
- 12 £375

 13 a 66
 b 1.75
- **14 a** 8 **b** 0.5
- 15 _

		25	50	400	
	y	10	20	160	
16	a 12	25		b	

17 $P = k_1 Q$, $k_1 = \frac{P}{Q} = \frac{4}{10} = 0.4$. So P = 0.4Q. $QR = k_2 = 2 \times 8$. So QR = 16. When R = 0.8, then $Q = 16 \div 0.8 = 20$.

 $\frac{1}{2}$

So $P = 0.4Q = 0.4 \times 20 = 8$

Chapter 18 – Statistics: Representation and interpretation

Exercise 18A

- 1 a secondary data
 - **b** primary data
 - c primary or secondary data
 - d primary or secondary data
 - e primary data
 - f primary data
- 2 Plan the data collection: Choose a random sample of 30 boys and 30 girls from Year 11.

Collect the data: Ask each student to spell the same 10 words. This will avoid bias. Pick words that are often misspelt, eg accommodation, necessary, separate

Choose the best way to process and represent the data: Calculate the mean number and range for the number of correct spellings for the boys and for the girls. Draw a dual bar chart to illustrate the data.

Interpret the data and make conclusions: Compare the mean and range to arrive at a conclusion. Is there a clear conclusion or do you need to change any of the 10 words or take a larger sample?

3 Plan the data collection: Choose a random sample of 20 boys and 20 girls from Year 11.

Collect the data: Ask each student, on average, how many hours of sport they play and how many hours of TV they watch each week.

Choose the best way to process and represent the data: Calculate the mean number of hours for the number of hours playing sport and the number of hours watching TV. Draw a dual bar chart to illustrate the data.

Interpret the data and make conclusions: Compare the means and arrive at a conclusion. Is there a clear conclusion or do you need to take a larger sample?

- 4 One more girl
- **5 a** 4:3
 - **b** It has been assumed that the ratio of males to females in the sample is the same as the ratio of males to females attending the match.

6 28.5%

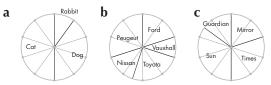
7

1

а		Male	Female	Total
	Full time	13	7	20
	Part time	4	6	10
	Total num	30		

b The numbers have been rounded.

Exercise 18B



- 2 Pie charts with the following angles:
 - **a** 36°, 90°, 126°, 81°, 27°
 - **b** 90°, 108°, 60°, 78°, 24°
 - **c** 168°, 52°, 100°, 40°
- 3 a Pictogram with suitable keyb Bar chart correctly labelled
 - **c** Vertical line chart correctly labelled
 - **d** Pie chart with these angles: 60°, 165°, 45°, 15°, 75° and correctly labelled
 - e Vertical line chart. It shows the frequencies, the easiest one to draw and comparisons can be made.
- **4 a** 36
 - b Pie chart with these angles: $50^\circ,\,50^\circ,\,80^\circ,\,60^\circ,\,60^\circ,\,40^\circ,\,20^\circ$ and correctly labelled
 - c Bar chart correctly labelled
 - d Bar chart, because it is easier to make comparisons
- 5 a Pie chart with these angles: 124° , 132° , 76° , 28° and correctly labelled
 - **b** Split of parties can be seen at a glance
- 6 a Pie charts with these angles: Strings: 36°, 118°, 126°, 72°, 8° Brass: 82°, 118°, 98°, 39°, 23°
 - **b** Overall, the strings candidates did better, as a smaller proportion scored the lowest grade. a higher proportion of brass candidates scored the highest grade.
- 7 The missing angle is 40°, so P(Don't know)

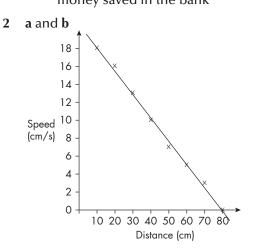
	40	1
=	360	$=\overline{9}$

8 a 55° **b** 22 **c** $33\frac{1}{3}\%$

Exercise 18C

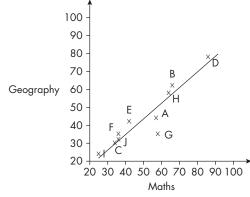
1 a i Good positive correlation

- ii Time increases with the number of press-ups
- **b i** Strong negative correlation
 - ii You complete a crossword quicker as you get older
- c i No correlationii Speed of cars on M1 is not related to the temperature
- d i Weak positive correlationii Older people generally have more money saved in the bank

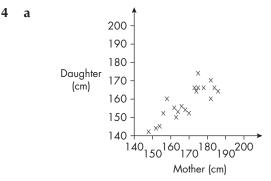


c about 19 cm/s **d** about 34 cm

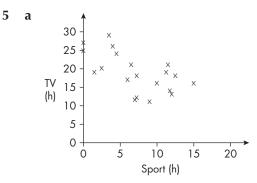




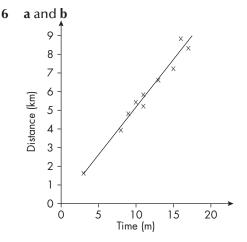
- **c** Grace
- d about 70
- e about 70



b Yes, as good positive correlation



b No; Little correlation, so cannot draw a line of best fit



- c about 2.4 km
- d about 8 minutes
- e you cannot extrapolate values from a scatter diagram or the data may change for longer journeys

- 7 about 23 mph
- 8 Points showing a line of best fit sloping down from top left to bottom right

Exercise 18D

- **1 a** i $30 < x \le 40$ ii 29.5 iii $30 < x \le 40$ **b** i $0 < y \le 100$ ii 158.3 iii $100 < y \le 200$ **c** i $5 < z \le 10$ ii 9.43 iii $5 < z \le 10$ **d** i 7-9 ii 8.41 iii 7-9
- **2 a** $100 < m \le 120$ **b** 10.86 kg **c** 108.6 g
- **3 a** 175 < *h* ≤ 200 **b** 31%
 - c 193.3 hours
 - **d** No, the mean was under 200.
- a Yes, average distance is 11.7 miles per day.
 b Because shorter runs will be run faster which will affect the average
 - c Yes, because the shortest could be 1 mile, the longest 25 miles.
- **5** 24
- 6 Soundbuy; average increases are Soundbuy 17.7p, Springfields 18.7p, Setco 18.2p
- 7
 a 160
 b 52.6 minutes

 c
 Modal group
 d 65%
- 8 The first 5 and the 10 are the wrong way round.
- **9** Find the midpoint of each group, multiply that by the frequency and add those products. Divide that total by the total frequency.

Review questions

- **1 a** 18 **b** 80°
- a i Diagram C ii Diagram A iii Diagram B
 b Diagram A: strong negative correlation, diagram B: no correlation, diagram C: strong positive correlation
- 3 a/b Time on horizontal axis from 0 to 20 and Distance (km) on vertical axis from 0 to 10 with the following points plotted: (3, 1.7) (17, 8.3) (11, 5.1) (13, 6.7) (9, 4.7) (15, 7.3) (8, 3.8) (11, 5.7) (16, 8.7) (10, 5.3) and with line of best fit drawn.
 c/d Answers depend on student's plotting
- **4 a** $10 < t \le 20$ **b** $10 < t \le 20$ **c** 19 minutes

- a Because over half the students have more than £10 pocket money, so the mean must be more than £10
 b £11.00
- 6 120 boys and 200 girls

Chapter 19 – Geometry and measures: Constructions and loci Exercise 19A

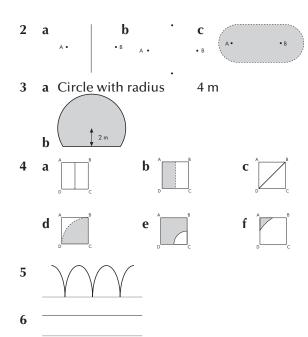
- **a** BC = 2.9 cm, \angle B = 53°, \angle C = 92° **b** EF = 7.4 cm, ED = 6.8 cm, \angle E = 50° **c** \angle G = 105°, \angle H = 29°, \angle I = 46°
 - **d** $\angle J = 48^{\circ}$, $\angle L = 32^{\circ}$, JK = 4.3 cm
 - $e \angle N = 55^{\circ}$, ON = OM = 7.0 cm
 - **f** $\angle P = 51^{\circ}, \angle R = 39^{\circ}, QP = 5.7 \text{ cm}$
- **2 a** Students can check one another's triangles.
 - **b** $\angle ABC = 44^{\circ}, \angle BCA = 79^{\circ}, \angle CAB = 57^{\circ}$
- **3 a** 5.9 cm **b** 18.8 cm²
- 4 BC = 2.6 cm, 7.8 cm
- 5 a 4.3 cm b 10.8 cm²
- **6 a** 4.3 cm **b** 34.4 cm²
- 7 An equilateral triangle of side 4 cm
- 8 Even with all three angles, you need to know at least one length

Exercise 19B

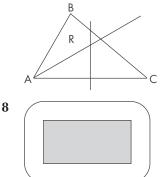
- 1–9 Practical work; check students' constructions
- 10 The centre of the circle
- 11 Start with a base line AB; then construct a perpendicular to the line from point A. At point B, construct an angle of 60°. Ensure that the line for this 60° angle crosses the perpendicular line; where they meet will be the final point C.
- 12–14 Practical work; check students' constructions

Exercise 19C

1 Circle with radius: a 2 cm b 4 cm c 5 cm



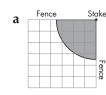
7 Construct the bisector of angle BAC and the perpendicular bisector of the line AC.



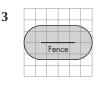
- 9 Start with a base line, AB, 3 cm long. At point A, draw a few points all 3 cm away from A towards the upper right side. Lightly join these dots with an arc. You can now find the point that is 3 cm away from point B and draw the equilateral triangle.
- 10 Gary is correct about the triangle inside, but not a triangle outside as there will be three straight lines, parallel to each side of the triangle, then these straight lines will be joined with arcs centred on the vertex between the lines.

Exercise 19D

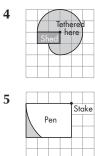


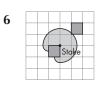


2



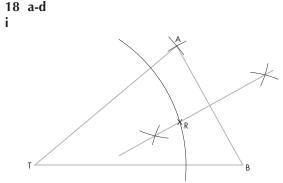




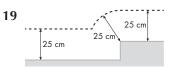


- 7 a Sketch should show a circle of radius 6 cm around London and one of radius 4 cm around Glasgow.
 - b No
 - **c** Yes
- 8 a Yes
 - **b** Sketch should show a circle of radius 4 cm around Leeds and one of radius 4 cm around Exeter. The area where they overlap should be shaded.
- **9 a** This is the perpendicular bisector of the line from York to Birmingham. It should pass just below Manchester and just through the top of Norwich.
 - b Sketch should show a circle of radius7 cm around Glasgow and one of radius5 cm around London.
 - **c** The transmitter can be built anywhere on line constructed in part **a** that is within the area where the circles shown in part **b** overlap.
- 10 Sketch should show two circles around Birmingham, one of radius 3 cm and one of radius 5 cm. The area of good reception is the area between the two circles.

- 11 Sketch should show a circle of radius 6 cm around Glasgow, two circles around York, one of radius 4 cm and one of radius 6 cm and a circle around London of radius 8 cm. The small area in the Irish Sea that is between the two circles around York and inside both the circle around Glasgow and the circle around London is where the boat can be.
- 12 Sketch should show two circles around Newcastle upon Tyne, one of radius 4 cm and one of radius 6 cm, and two circles around Bristol, one of radius 3 cm and one of radius 5 cm. The area that is between both pairs of circles is the area that should be shaded.
- 13 Sketch should show the perpendicular bisector of the line running from Newcastle upon Tyne to Manchester and that of the line running from Sheffield to Norwich. Where the lines cross is where the oil rig is located.
- 14 Sketch should show the perpendicular bisector of the line running from Glasgow to Norwich and that of the line running from Norwich to Exeter. Where the lines cross is where Fred's house is.
- 15 Leeds
- 16 No, if you accurately draw a diagram showing the path of each boat, you will find the boat leaving from point B meets the path of the other boat in much shorter time as it's a smaller distance than from A to the cross over point.
- 17 On a map, draw a straight line from Newcastle to Bristol, construct the line bisector, then the search will be anywhere on the sea along that line.

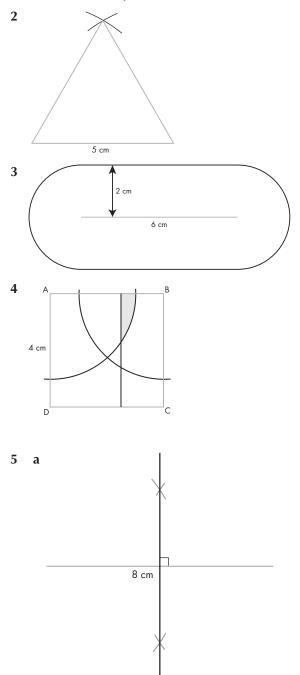


ii 20 km

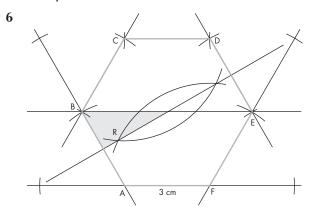


Review questions

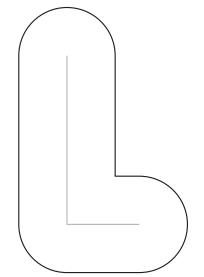
a - b Students' construction
 c Students' explanation.

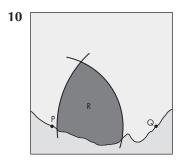


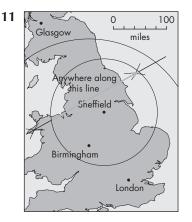
b an equal distance from A and B, or equidistant from A and B.



- 7 **a** Student's construction **b** 20 cm²
- 8 a Student's constructionb 18 cm²
- 9 Oliver is incorrect as the correct shape is:







Chapter 20 – Geometry and measures: Curved shapes and pyramids

Exercise 20A

1		i 5.58 cm i 5.24 cm	ii 22.3 cm ² ii 13.1 cm ²
	С	i 11.00 cm i 16.34 cm	ii 19.24 cm ² ii 98.02 cm ²

2	a i 6.8 cm	ii 18.8 cm
	b i 7.9 cm	ii 25.9 cm
	c i 8.4 cm	ii 16.4 cm
	d i 17.5 cm	ii 37.5 cm
	e i 3.3 cm	ii 20.3 cm

- 3 Arc length = 2π , area of sector = 6π
- **4 a** 270° **b** 51.8 cm **c** 73.8 cm
- 5 area of sector = $\frac{1}{4} \times \pi \times 8^2 = 16\pi$, area of circle = $\pi \times 4^2 = 16\pi$
- **6 a** 28.6° **b** 66.8° **c** 54.9°
- 7 Area A = 107 cm², area B = 173 cm². Half of B is 86.5 which is less than 107, so Gabby is wrong, the area of A is more than half the area of B.
- **8** 43.6 cm
- **9 a** 66.8° **b** 10 cm²

Exercise 20B

- 1 a 56 cm³ b 168 cm³ c 1040 cm³ d 84 cm³ e 160 cm³
- 2 $\frac{1}{3}$ base area $\times h = \frac{1}{3} \times 9 \times 9 \times 10 = 270$ cm³
- **3 a** 73.3 m³ **b** 45 m³ **c** 3250 cm³

- 4 208 g
- 5 1.5 g/cm³
- 6 $\frac{1}{3} \times 6.4 \times 6.4 \times h = 81.3$ so $h = \frac{3 \times 81.3}{6.4 \times 6.4} = 5.95 = 6.0$ cm (2 sf)
- 7 14.4 cm

Exercise 20C

- **1 a** 72 cm² **b** 172.5 cm²
- 2 Area of base = 9^2 = 81 cm², area of one triangle = $\frac{1}{2} \times 9 \times 10 = 45$ cm², total surface area = (4 × 45) + 81 = 261 cm².
- 3 Total area = 32.46 m^2 , so 3 tins are needed
- 4 Surface areas are $a = 1200 \text{ cm}^2$, $b = 576 \text{ cm}^2$, $c = 864 \text{ cm}^2$, $d = 526.5 \text{ cm}^2$, Volumes are $a = 960 \text{ cm}^3$, $b = 512 \text{ cm}^3$, $c = 960 \text{ cm}^3$, $d = 540 \text{ cm}^3$. This does not show that the larger the volume, the larger the surface area, so Andrew is incorrect.
- 5 Yes, the area is 218.7 m² and will cost £2515.05 to retile.

Exercise 20D

- **1 a** 17.5 cm² b 103 cm² c 94.2 cm²
- 2 c Radii are 1.1 cm, 4.7 cm, 5 cm
- 3

Sector		Radius of cone, r		$\pi \times \mathbf{r} \times \mathbf{I}$
а	17.5 cm ²	1.1 cm	5 cm	17.3 cm ²
b	103 cm ²	4.7 cm	7 cm	103 cm ²
С	94.2 cm ²	5 cm	6 cm	94.2 cm ²

4 a They are the same **b** Curved surface area = πrl

Exercise 20E

1	a i 151 cm ³	ii 176 cm ²
	b i 75 cm ³	ii 108 cm ²
	c i 872 cm ³	ii 550 cm ²
	d i 3560 cm ³	ii 1426 cm ²
	e i 314 cm ³	ii 283 cm ²
	f i 1018 cm ³	ii 679 cm ²

2 935 g

- 3 $\pi r l + \pi r^2 = 3\pi l + 9\pi = 75.4$ $3\pi l = 75.4 - 28.27 = 47.13$ $l = \frac{47.3}{3\pi} = 5 \text{ cm}$
- **4 a** 816π cm³ **b** 720π mm³
- 5 The total surface area, to 3sf, is 75.4 cm², so Mandy is correct if the figure was rounded to 1 sf. Neil is incorrect as he has cut off his final answer instead of rounding it, or he may have used the height instead of the slant height.

Exercise 20F

- **1 a** 113 cm³ **b** 905 cm³ **c** 4189 cm³
- **2 a** 113 cm² **b** 314 cm² **c** 616 cm²
- 3 Volume = 4500π cm³, surface area = 900π cm²
- a 1960 cm² (to 3 sf)
 b 7444 cm³ (to nearest unit)
- 5 125 cm
- **6** 6232

Review questions

- **1 a** 43.9 cm **b** 112 cm²
- 2 49 000 m³
- 3 Volume of top cube = $30^3 = 27\ 000$, volume of bottom pyramid = $\frac{1}{3} \times 30^2 \times 10 = 3000$ cm³, total volume = top + bottom = $27\ 000 + 3\ 000 = 30\ 000$ cm³
- 4 Bottle will hold = $\pi r^2 h = \pi \times 4.5^2 \times 25 = 1590.4$ cm^{3.} One glass will hold $\frac{1}{3}\pi r^2 h = \frac{1}{3} \times \pi \times 2.5^2 \times 6 = 39.27$ cm^{3.} So 1590.4 ÷ 39.27 = 40.5 glasses can be filled. David is wrong as just over 40 glasses will be filled.
- 5 One bearing has volume = $\frac{4}{3}\pi r^3 = \frac{4}{3} \times \pi \times 0.75^3 = 1.767$ cm³, so one ball bearing has a mass of $1.767 \times 7.3 = 12.900$ g. 20 ball bearings have a mass of 258.00 g or 258 g (nearest whole number).
- 6 0.5 cm
- 7 34.6 m²
- 8 a A is largest at 1018 cm²
 b B is smallest at 1003 cm²
 Surface area of C is 1016 cm².
- **9** 0.825 m³

- 10 7.25 cm
- 11 Neither of them is correct as the surface area of the sphere is 1257 cm², surface area of the cube is 1262 cm² but the surface area of the cone is 1282 cm², so the cone has the greatest surface area
- 12 91.5 cm

Chapter 21 – Algebra: Number and sequences

Exercise 21A

- **1** a 11111 × 11111 = 123 454 321, 111111 × 11111 = 12 345 654 321
 - **b** 99999 × 99999 = 9 999 800 001, 999999 × 999999 = 999 998 000 001
- **2 a** $7 \times 8 = 7^2 + 7$, $8 \times 9 = 8^2 + 8$ **b** $50 \times 51 = 2550$, $60 \times 61 = 3660$
- 3 a $1+2+3+4+5+4+3+2+1=25=5^2$, 1+2+3+4+5+6+5+4+3+2+1=36 $=6^2$
 - **b** $21 + 23 + 25 + 27 + 29 = 125 = 5^3$, $31 + 33 + 35 + 37 + 39 + 41 = 216 = 6^3$
- **4 a** 1+6+15+20+15+6+1=64, 1+7+21+35+35+21+7+1=128
 - **b** 12 345 679 × 45 = 555 555 555, 12 345 679 × 54 = 666 666 666
- 5 **a** $1^3 + 2^3 + 3^3 + 4^3 = (1 + 2 + 3 + 4)^2 = 100,$ $1^3 + 2^3 + 3^3 + 4^3 + 5^3 = (1 + 2 + 3 + 4 + 5)^2 =$ 225
 - **b** $36^2 + 37^2 + 38^2 + 39^2 + 40^2 = 41^2 + 42^2 + 43^2 + 44^2$, $55^2 + 56^2 + 57^2 + 58^2 + 59^2 + 60^2 = 61^2 + 62^2 + 63^2 + 64^2 + 65^2$
- 6 a 12 345 678 987 654 321
 - **b** 999 999 998 000 000 001
 - c $12^2 + 12$
 - **d** 8190
 - **e** $81 = 9^2$
 - **f** $512 = 8^3$
 - **g** 512
 - ĥ 999 999 999
 - i $(1+2+3+4+5+6+7+8+9)^2 = 2025$
- 7 1 + 500 = 501, 2 + 499 = 501, 250 + 251 = 501, 250 × 501 = 125 250

Exercise 21B

1 a 21, 34: add previous 2 terms

- b 49, 64: next square number
- c 47, 76: add previous 2 terms
- **2** 15, 21, 28, 36
- **3** 61, 91, 127
- **4** 6, 11, 16, 21, 26 ...
- 5 $\frac{1}{2}, \frac{3}{5}, \frac{2}{3}, \frac{5}{7}, \frac{3}{4}$
- **6 a** 6, 10, 15, 21, 28
 - **b** It is the sums of the natural numbers, or the numbers in Pascal's triangle or the triangular numbers.
- **7 a** 2, 6, 24, 720
 - **b** 69! (may vary depending on the calculator)
- 8 *X*. There are 351 (1 + 2 + ... + 25 + 26) letters from A to Z. $3 \times 351 = 1053$. 1053 - 26 =1027, 1027 - 25 = 1002, so, as Z and Y are eliminated, the 1000th letter must be X.
- 364: Daily totals are 1, 3, 6, 10, 15, 21, 28, 36, 45, 55, 66, 78 (these are the triangular numbers). Cumulative totals are: 1, 4, 10, 20, 35, 56, 84, 120, 165, 220, 286, 364.
- 10 29 and 41
- 11 No, because in the first sequence, the terms are always one less than in the 2nd sequence
- **12** 4n 2 = 3n + 7 rearranges as 4n 3n = 7 + 2, so n = 9

Exercise 21C

1	а	13, 15, 2 <i>n</i> + 1		b	25, 2	9, 4 <i>n</i> + 1
	С	33, 38, 5 <i>n</i> + 3		d	32, 3	8, 6 <i>n</i> – 4
	e	20, 23, 3 <i>n</i> + 2		f	37, 4	4, 7 <i>n</i> – 5
	g	21, 25, 4 <i>n</i> – 3		h	23, 2	7, 4 <i>n</i> – 1
	i	17, 20, 3 <i>n</i> – 1		j	-8, -	18, -10n + 42
	k	4, 0, -4 <i>n</i> + 24		Í	-1, -	6, -5n + 29
2	а	3 <i>n</i> + 1, 151		b	2 <i>n</i> +	5, 105
	С	5 <i>n</i> – 2, 248		d	4n -	3, 197
	e	8 <i>n</i> – 6, 394		f	<i>n</i> + 4	, 54
	g	5 <i>n</i> + 1, 251		h	8n -	5, 395
		3 <i>n</i> – 2, 148		i	3 <i>n</i> +	18, 168
	-	-7n + 47, -303		,		+ 41, -359
3	а	33rd		b	30th	
	С	100th = 499				
4	а	i 4 <i>n</i> + 1	ii	401	iii	101, 25th
	b	i 2 <i>n</i> + 1	ii	201	iii	99 or 101, 49th
						and 50th

c i 3n + 1ii 301 iii 100, 33rd **d** i 2n + 6**ii** 206 iii 100, 47th **e i** 4*n* + 5 ii 405 iii 101, 24th f **i** 5*n*+1 ii 501 iii 101, 20th **g i** 3*n* – 3 ii 297 iii 99, 34th **h** i 6*n* – 4 ii 596 iii 98, 17th **i i** -8*n* + 205 iii 101, 13th **ii** –595 **i** -2*n* + 227 ii 27 iii 99 or 101, 63rd and 64th 5 a $\frac{2n+1}{3n+1}$ **b** Getting closer to $\frac{2}{3}$ (0.6) **c i** 0.667 774 (6dp) ii 0.666 778 (6dp) **d** 0.666 678 (6dp), 0.666 667 (6dp) $\frac{4n-1}{5n+1}$ 6 а **b** Getting closer to $\frac{4}{5}$ (0.8) **c i** 0.796 407 (6dp) **ii** 0.799 640 (6dp) **d** 0.799 964 (6dp), 0.799 996 (6dp) a £305 **b** £600 **c** 3 7 **d** 5 **a** $\frac{3}{4}, \frac{5}{7}, \frac{7}{10}$ 8 **b i** 0.666 666 777 8 **ii** $\frac{2}{3}$ **c** For large n, $\frac{2n+1}{3n+1} \approx \frac{2n}{3n} = \frac{2}{3}$ 9 **b** 8*n* + 1 **c** 8*n* **d** £8 **a** 8*n* + 2

- 10 a Sequence goes up in 2s; first term is 2 + 29
 b n + 108
 c Because it ends up as 2n ÷ n
 - **d** 79th
- 11 The expressions show that the terms in the sequence 2n 1 are always one less than those in the 2n sequence, so they will have no numbers in common.
- **12** Difference is 19 10 = 9. $9 \div 3 = 3$ so a = 3. $3 \times 5 + b = 10$, b = -5

Exercise 21D

1	a Even,							
	+	Odd	Even					

+	Oaa	Even
Odd	Even	Odd
Even	Odd	Even
h Odd		

o Ouu,							
×	Odd	Even					
Odd	Odd	Even					
Even	Even	Even					

- **2 a** $1+3+5+7=16=4^2$, $1+3+5+7+9=25=5^2$
 - **b i** 100 **ii** 56

- a 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144
 b Because odd + odd = even, odd plus even = odd and even + odd = odd
 - c i a+2b, 2a+3b, 3a+5b, 5a+8b, 8a+13b
 ii The coefficients of both a and b each form a Fibonacci sequence

4	a Even	b Odd	c Odd
	d Odd	e Odd	f Odd
	g Even	h Odd	i Odd

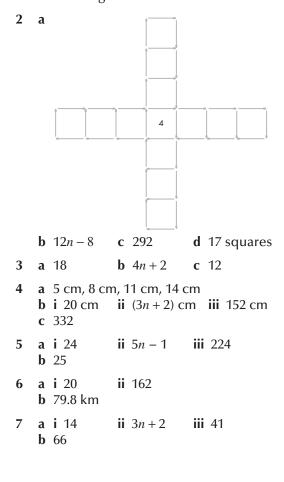
- 5aOdd or evenbOdd or evencOdd or evendOddeOdd or evenfEven
- **6 a i** Odd **ii** Even **iii** Even **b** Any valid answer, e.g. x(y + z)
- 7 **a** 64, 128, 256, 512, 1024 **b i** $2^n - 1$ **ii** $2^n + 1$ **iii** 3×2^n
- 8 a The number of zeros equals the power.b 6
 - **c i** $10^n 1$ **ii** 2×10^n
- 9 a 125, 216
 b 1+8=9, 1+8+27=36, 1+8+27+64= 100... the answers are square numbers
- **10 a** 28, 36, 45, 55, 66
 - **b** i 210 ii 5050
 - c You get the square numbers.
- 11 a i If n is odd, n + 1 is even. If n is even, n + 1 is odd. Even times odd is always even.
 ii 2n must be even, so 2n + 1 must be odd.
 - **b** Odd Odd Even Even Odd **c** $(2n+1)^2 = 4n^2 + 4n + 1$ or $(2n)^2 = 4n^2$ $4n^2 + 4n$ is even so adding 1 makes it odd
 - $4n^2$ is $2 \times 2n^2$ which is even
- **12** 11th triangular number is 66, 18th triangular number is 171
- **13** a 36, 49, 64, 81, 100 b i $n^2 + 1$ ii $2n^2$ iii $n^2 - 1$
- **14 a i** 4, 16, 64, 256, 1024 **ii** 7, 49, 343, 2401, 16 807 **iii** 5, 25, 125, 625, 3125 **iv** 9, 81, 729, 6561, 59 049 **v** 8, 64, 512, 4096, 32 768 **b i** 60 **ii** 40

- 15 2. Only 2 plus a prime will give another prime, but not always. This is because after 2, all primes are odd, and odd + odd is always an even number. No even numbers after 2 are prime.
- **16** a There are many answers, 5 + 31 = 36, 7 + 29 = 36, 2 + 47 = 49 etc.
 - **b** There are many answers, 49 36 = 13, 81 – 64 = 17
- **17** a 3, 6, 11, 18, 27
 - **b** 102
 - **c** 20th
 - **d** No. Because the terms of the sequence n² alternate between even and odd, and adding 2 to each term will not change this even-odd pattern.

Exercise 21E

1 a b 2n + 1c 121

d 49 triangles



- 8 a i 5 ii *n* iii 18 b 20 tins
- **9** 2*n* − 1
- **10** $(n+1)^2$
- **11 a** 2ⁿ
 - **b** i $100 \times 2^{n-1}$ ml ii 1600 ml **c** Next sizes after super giant are 3.2 *l*, 6.4 *l* and 12.8 *l* with weights of 3.2 kg, 6.4 kg and 12.8 kg, so the largest size is 6.4 litres.
- 12 The *n*th term is $\left(\frac{3}{4}\right)^n$, so as *n* gets very large, the unshaded area gets smaller and smaller and eventually it will be zero; so the shaded area will eventually cover the triangle.
- **13** Yes, as the number of matches is 12, 21, 30, 39, ... which is 9n + 3; so he will need $9 \times 20 + 3 = 183$ matches for the 20th step and he has $5 \times 42 = 210$ matches.
- **14 a** 20 **b** 120
- **15** Alex's answer gives 4(n + 2) = 4n + 8Colin's method gives 4n + 4Ed's method gives 4(n + 1) = 4n + 4Gail's method gives $2 \times n + 2(n + 2) = 2n + 2n + 4 = 4n + 4$ Linear sequence is 8, 12, 16, 20, Which has an *n*th term of 4n + 4 so they are all valid methods except for Alex who forgot that the corners overlap and should have taken the 4 overlapping corners away to get 4n + 8 - 4 = 4n + 4

16 a £128 **b** £31 **c** £4095

Review questions

- 1 No. Sequence is 7, 10, 13, 16, 19, 22, 25, 28, ... so the first three odd terms are prime but 25 is not prime.
- **2** a 13, 9
 - **b** Subtract 4
 - c All the terms are odd and -4 is even
- **3 a i** 40, 34 **ii** 32, 64 **b** 4, 16, 64
- 4 a Always even b Odd or even
- **5** 0, 3, 8
- **6 a** 5, 3

- **b** 15, 14.5
- c He is right as when it gets nearly to 14, the next term will be $\frac{14+14}{2} = 14$
- 7 **a** i 6, 11, 16 ii All terms end in 1 or 6 **b** No. When n = 1 then $(1 + 2)^2 - 9 = 9 - 9 = 0$ and after that $(n + 2)^2$ is always greater than 9
- **8 a** 4*n* + 1
 - b All the terms are odd and 112 is even c 28^{th} term is 113
- 9 *n*th term is 5n + 1. $5 \times 150 + 1 = 751$
- **10 a** 6*n* + 3
 - **b** No, 3*n* + 2 generates the sequence 5, 8, 11, 14, 17, 20, 23, ... so the even terms of this sequence are always 1 less than the terms of the original sequence
- 11 a Always odd b Always odd
- **12** For example: $0.5^2 = 0.25$, 0.25 < 0.5
- **13 a** $2 \times n$ is always even, any even number plus 1 is odd
 - **b** $Odd \times odd = odd$, even \times even = even

Chapter 22 – Geometry and measures: Right-angled triangles

Exercise 22A

1	b 90°	c 9, 16, 25	d $9 + 16 = 25$
2	b 90°	c 25, 144, 169	9 d 25+144=169
3	b 90°	c 36, 64, 100	d $36 + 64 = 100$
4	$c^2 = a^2 + b$	b^2	
5	b 7.8 cm	c 7.8 cm	

Exercise 22B

1	а	10.3 cm	b	5.9 cm	С	8.5 cm
	d	20.6 cm	e	18.6 cm	f	17.5 cm
	g	32.2 cm	h	2.4 m	i	500 m
	i	5 cm	k	13 cm		10 cm

- 2 14.4 cm
- 3 Diagonal² = $6^2 + 6^2 = 72$, diagonal = $\sqrt{72} = 8.4852841 = 8.5$ cm to 1 decimal place
- 4 50 cm, 1.2 m and 1.3 m or 1.5 m, 2 m and 2.5 m
- 5 Because $6^2 + 7^2 = 85$ and $\sqrt{85} = 9.2$ not 10
- 6 a 15 b 13 c 7.3 d 14.2

- **7 a** 9, 12, 15
- **b** 25, 60, 65
 - c Any six more Pythagorean triples, for example 10, 24, 26

Exercise 22C

1	a 15.0 cm	b 14.7 cm	c 6.3 cm
	d 18.3 cm	e 5.4 cm	f 217.9 m
	g 0.4 cm	h 8.0 m	
2	a 20.8 m	b 15.5 cm	c 15.5 m
	u 20.0 m		
		e 22.9 m	

- **3 a** 5.0 m **b** 6.0 m **c** 3.0 m **d** 50.0 cm
- 4 The 12×30 has diagonal length of 32.31 cm, the 11×30 has a diagonal length of 31.95cm, so the 11×30 is the closest to 32 cm.
- 5 Many different combinations are possible, such as: 8 cm and 11.5 cm, 10 cm and 9.8 cm, 12 cm and 7.2 cm.
- $6 \quad 80^2 + 60^2 = 6400 + 3600 = 10\ 000 = 100^2$
- 7 a Student's own diagram
 - **b** i The large square is 17 by 17 giving 289 square units.
 - ii The red and yellow triangles all have shorter lengths of 5 and 12, with an area of 30 square units each. The four red triangles have an area of $4 \times 30 =$ 120 square units
 - iii The area of the inner square (green and yellow) must be $289 - 4 \times 30 =$ 169, so the hypotenuse of the red and yellow triangles must be $\sqrt{169} = 13$
 - **c** The above working shows that $5^2 + 12^2 = 13^2$

Exercise 22D

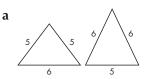
- 1 No. The foot of the ladder is about 6.6 m from the wall.
- 2 2.06 m
- 3 11.3 m
- 4 About 17 minutes
- 5 27.4 m
- 6 4.58 m
- **7 a** 3.87 m **b** 1.74 m
- 8 3.16 m

- 9 This creates a right-angled triangle with two short sides of 5 and 12. Use Pythagoras' theorem to show length of line $=\sqrt{(5^2 + 12^2)} = 13$
- **10 a** 4.85 m
 - **b** 4.83 m (There is only a small difference.)
- 11 Yes, because $24^2 + 7^2 = 25^2$
- 12 6 cm
- **13** He is partly correct. The perimeter must be larger than 20 cm or the rectangle has no width, and the area is largest when it's a square, giving a perimeter of 28.3 cm (3sf). So he should have said the perimeter is between 20 and 28.3 cm.

Exercise 22E

- **1 a** 32.2 cm^2 **b** 2.83 cm^2 **c** 50.0 cm^2
- **2** 22.2 cm²
- 3 15.6 cm²

4



b The areas are 12 cm² and 13.6 cm² respectively, so triangle with 6 cm, 6 cm, 5 cm sides has the greater area.



b 166.3 cm²

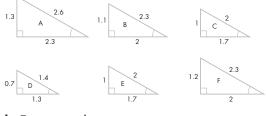
- 6 259.8 cm²
- 7 **a** No, areas vary from 24.5 cm^2 to 27.7 cm^2

1 c i For example:

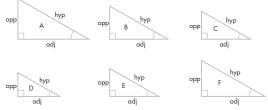
- **b** No, the equilateral triangle gives the largest area.
- c The closer the isosceles triangle gets to an equilateral triangle the larger its area becomes.
- 8 The right-angled triangle made with hypotenuse 6.5 m and base 7.4 ÷ 2 = 3.7 gives the height of the triangle as 5.344 cm. Use area = $\frac{1}{2} \times 7.4 \times 5.344$ to give 19.7733 which rounds to 19.8 m² (3sf)
- **9** 48 cm²
- **10 a** 10 cm **b** 26 cm **c** 9.6 cm
- 11 6 or 8 cm
- 12 Andrew didn't round off any answers until the last calculation, and Olly used a rounded off value to find an intermediate result.

Exercise 22F

1 a For example:



b For example:



Triangle	Opposite	Adjacent	Hypotenuse	<u>Opposite</u> Hypotenuse	<u>Adjacent</u> Hypotenuse	<u>Opposite</u> Adjacent
А	1.3	2.3	2.6	0.500	0.885	0.565
В	1.1	2	2.3	0.480	0.870	0.550
С	1	1.7	2	0.500	0.850	0.588
D	0.7	1.3	1.4	0.500	0.929	0.538
E	1	1.7	2	0.500	0.850	0.588
F	1.2	2	2.4	0.520	0.833	0.600

ii Regardless of the size of the triangle the ratios are similar in each case.

- **2 b** Yes, the pattern is the same.
- 3 a The answer the calculator gives is almost the same as the $\frac{\text{opposite}}{\text{hypotenuse}}$.
 - **b** The answer the calculator gives is almost the same as the <u>adjacent</u> . hypotenuse
 - c The answer the calculator gives is almost the same as the $\frac{\text{opposite}}{\text{adjacent}}$.
 - **d** Yes
 - e Match up calculator result with student table result from above.

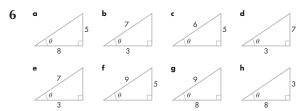
Exercise 22G

a x is opp, y is hyp, w is adj
b x is adj, y is opp, w is hyp
c x is hyp, y is opp, w is adj
d x is adj, y is hyp, w is opp
e x is hyp, y is opp, w is adj
f x is adj, y is hyp, w is opp

2	b sin $\theta = \frac{5}{13}$, cos $\theta = \frac{12}{13}$, tan $\theta = \frac{5}{12}$
	$\mathbf{c} \sin \theta = \frac{9}{41}$, $\cos \theta = \frac{40}{41}$, $\tan \theta = \frac{9}{40}$
3	a $\sin \theta = \frac{12}{20}$, $\cos \theta = \frac{16}{20}$, $\tan \theta = \frac{12}{16}$
	b sin $\theta = \frac{5}{13}$, cos $\theta = \frac{12}{13}$, tan $\theta = \frac{5}{12}$
	c $\sin \theta = \frac{24}{26}, \cos \theta = \frac{10}{26}, \tan \theta = \frac{24}{10}$
	d $\sin \theta = \frac{20}{25}$, $\cos \theta = \frac{15}{25}$, $\tan \theta = \frac{20}{15}$
	e $\sin \theta = \frac{36}{39}, \cos \theta = \frac{15}{39}, \tan \theta = \frac{36}{15}$
	f sin $\theta = \frac{40}{50}$, cos $\theta = \frac{30}{50}$, tan $\theta = \frac{40}{30}$
4	b $\cos \theta = \frac{\mathrm{adj}}{\mathrm{hyp}} = \frac{5}{7}$ c $\tan \theta = \frac{\mathrm{opp}}{\mathrm{adj}} =$
	d $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{8}{11}$ e $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{1}{11}$

f
$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{5}{13}$$

5 If the triangle is right-angled, then the sides are 3, 4 and 5. This is a Pythagorean triple and so he could be correct.



7 **a** i tan $x = \frac{3}{4}$ ii sin $x = \frac{3}{5}$ iii cos $x = \frac{4}{5}$ **b** i tan $y = \frac{4}{3}$ ii sin $y = \frac{4}{5}$ iii cos $y = \frac{3}{5}$ **c** i the same ii the same **d** One is the reciprocal of the other

Exercise 22H

1	d		e	0.829 0.707 0			0.922 0.342
2	d	0		0.559 0.707 1			0.388 0.940
3	45	0					
4	b c d	i 0.574 i 0.208 i 0.391 Same i sin 15° ii cos 82° iii sin <i>x</i> is	ii ii is	0.208 0.391 the sa the sa	me	as	sin 8°
5	d	0.933 Infinite 0.404	e	1		-	2.38 0.364
6			e	0.819			2.16 0.577
7	Та	n has some	e v	alues	>1		
8		10.7 Infinite			b 5 d 0		
9		3.56 28.4			b 8 d 8		
10		.5315389 + 4 6 = 2.990408				5 +	0) = 8.9904079

11 0.6

10

7 12

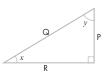
Exercise 221

1	a	9.5 cm	b	3.8 cm
	С	4.4 cm	d	8.3 cm
	е	12.0 cm	f	4.2 cm
	g	10.3 cm	h	19.6 cm
	i	5.1 cm	i	9.2 cm
	k	6.1 cm	Ì	13.3 cm

2 Yes because one side = $10 \sin 60^\circ = 8.7 \text{ cm}$ (1 dp) and the other $10 \cos 60^\circ = 5 \text{ cm}$

3 Opposite = $8 \tan 38^{\circ} = 6.25 \text{ cm} (2 \text{ dp})$

4 Sin $x = \frac{\text{opp}}{\text{hyp}} = \frac{P}{R}$, cos $y = \frac{\text{adj}}{\text{hyp}} = \frac{P}{R}$ so where *x* and *y* are the two acute angles in a right-angled triangle, the sine of one is equal to the cosine of the other.



Exercise 22J

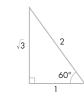
1	a 30.0°	b 51.7°	c 39.8°
	d 61.3°	e 87.4°	f 45.0°
2	a 60.0°	b 50.2°	c 2.6°
	d 45.0°	e 78.5°	f 45.6°
3	a 31.0°	b 20.8°	c 41.8°
	d 46.4°	e 69.5°	f 77.1°
4	a 53.1°	b 41.8°	c 44.4°
	d 56.4°	e 2.4°	f 22.6°
5	a 36.9°	b 48.2°	c 45.6°
	d 33.6°	e 87.6°	f 67.4°
6	a 31.0°	b 37.9°	c 15.9°
	d 60.9°	e 57.5°	f 50.2°

- 7 a His statement is true.
 - **b** It is true for cosine for the same reason as sine. It is not true for tangent because tan *x* is larger than 1 when the opposite is larger than the adjacent.
 - c Largest value 1
- 8 a i 17.5° ii 72.5° iii 90° b Yes

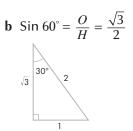
9	а	61.0°	b	26.4°	С	36.9°	d	45.6°
	e	43.3°	f	54.3°	g	51.3°	h	49.4°
	i	36.9°	j	41.4°	k	39.5°	L	69.4°

Exercise 22K





a The opposite side is $\sqrt{3}$ from Pythagoras. Tan 60° = $\frac{O}{A} = \frac{\sqrt{3}}{1} = \sqrt{3}$



2 a The adjacent side is $\sqrt{3}$ from Pythagoras. Tan $30 = \frac{O}{A} = \frac{1}{\sqrt{3}}$

b Cos 30° =
$$\frac{A}{H} = \frac{\sqrt{3}}{2}$$

- **3 a** 4.5 cm **b** 5 cm **c** 3.5 cm
- 4 The ratio to use is the $\cos \theta = \frac{A}{H} \cdot \cos 60 = \frac{3.5}{AC}$. Therefore AC = 7 cm. lain is correct.
- 5 i-iv

6

In each of the diagrams the smaller the side at the bottom the more each of sin 90° tends towards 1, cos 0° tends towards 1, sin 0° tends towards 0, and cos 90° tends towards 0.



- a From the diagram above, $\tan x = \frac{O}{A} = \frac{1}{1} = 1$. As the triangle is isosceles each acute angle is equal and therefore x = 45 degrees.
- **b** The hypotenuse is $\sqrt{2}$ due to Pythagoras' theorem. Therefore $\cos x = \frac{A}{H} = \frac{1}{\sqrt{2}}$ and $\sin x = \frac{O}{H} = \frac{1}{\sqrt{2}}$

Exercise 22L

- **1** 65°
- 2 The safe limits are between 1.04 m and 2.05 m. The highest the ladder will reach is 5.9 m up the wall.
- **3** 44°
- 4 6.82 m
- **5** 31°
- **6 a** 25°
 - **b** 2.10 m
 - c Thickness of wood has been ignored

- **7 a** 20° **b** 4.78 m
- 8 She would calculate 100 tan 23°. The answer is about 42.4 m
- 9 21.1 m
- 10 $\frac{\text{Height}}{3000}$ = sin5.1, so height = 3000sin5.1 = 266.68 = 267 (to 3 sf)
- **11** 8.2 m (2 sf)

Exercise 22M

- 1 10.1 km
- **2** 22°
- 3 429 m
- 4 **a** 156 m **b** No, the new angle of depression is $\tan^{-1}(\frac{200}{312}) = 33^{\circ}$ and half of 52° is 26°
- **5 a** 222 m **b** 42°
- **6 a** 21.5 m **b** 17.8 m
- 7 13.4 m. We don't know if the angle of elevation is from Sunil's feet or head. This would make a difference to the answer as we would need to add Sunil's height if the angle was from his head.
- 8 Sin $\theta = \frac{1}{3}$ so sin⁻¹ 0.3333 = 19.5° (3sf)
- **9** The angle is 16° so Cara is not quite correct.

Exercise 22N

- **1 a** 73.4 km **b** 15.6 km
- **2 a** 14.7 miles **b** 8.5 miles
- 3 Draw a diagram representing the relative places. Your diagram will show the angle

of the bearing to fly is $\tan^{-1}(\frac{70}{120}) + 90^{\circ} =$ 120.256° which rounds to 120° (3 sf).

- **4 a** 59.4 km **b** 8.4 km
- 5 a 15.9 km b 24.1 km c 31.2 km d 052°
- 6 2.28 km
- **7** 235°
- 8 The distance North is 120cos35 = 98.298245 km, so he hasn't gone as far as 100 km, but rounded to the nearest ten he is correct.

Exercise 220

1	a 5.79 cm	b 48.2°
	c 7.42 cm	d 81.6 cm

- 2 9.86 m
- **3 a** 36.4 cm² **b** 115 cm² **c** 90.6 cm² **d** 160 cm²
- **4** 473 cm²

Review questions

- 1 8.6 cm
- 2 6.7 cm
- 3 5.7 cm (1 dp)
- 4 Height = 5sin75 = 4.8296 m, which is just higher than 4.8 m so Michael is correct.
- 5 13.6 cm²
- 6 2 pm
- **7** 237°
- **8** 52.3°
- **9 a** 5.9 m **b** 82°
- **10 a** 75.5° **b** 47.4 cm²
- 11 The areas are parallelogram 85.8 cm², triangle 82.8 cm² and circle 84.9 cm². So all answers are close, but Joe is correct, the parallelogram does have the greatest area.
- **12 a** 32.60 m **b** 10.07 m **c** 4.10 m **d** 9.34 m

Chapter 23 – Geometry and measures: Congruency and similarity

Exercise 23A

1		SAS SSS		SSS ASA		RHS ASA		
2		i SSS i SAS		,		P, C to (Q, C to	•	
3	а	60°	b	80°	С	40°	d	5 cm

- 4 The triangle is made of parallel lines so each triangle has a set of corresponding angles with each other. Because the squares share sides with the triangles, each triangle has the same-sized sides. Hence each triangle is congruent, ASA.
- 5 SSS or RHS
- 6 SSS or SAS or RHS
- 7 a always
 - **b** always
 - c always
 - d sometimes; it's true if the scale factor is 1
- **8 a** The square has rotated through angle *x*, so each side has rotated the same angle.
 - **b i** ED and DG are both sides of the same square **ii** CD and AD are both sides of the same square
 - **c** SAS, where CD corresponds to AD, DG corresponds to DE and the angle between them is *x* in each case.
- **9** AB and PQ are the corresponding sides to the 42° angle, but they are not equal in length.

Exercise 23B

- 1 a–b Check students' drawings.
 - c Each triangle has the same angles as the other.
 - **d** They are all twice as large.
 - **e** 2
- 2 a-b Check students' drawings.
 - c Each triangle has the same angles as the other
 - **d** They are all three times as large.
 - **e** 3
- 3 a-b Check students' drawings.
 - c Each triangle has the same angles as the other.
 - **d** yes
 - **e** 1.5
- 4 a–c Check students' drawings.
 - d Each triangle has the same angles as the other.
 - **e** 2
- 5 **a–c** Check students' drawings.
 - **d** Each triangle has the same angles as the other.
 - **e** 3

Exercise 23C

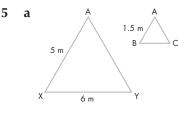
- 1 a similar, scale factor 3
 - **b** similar, scale factor 2
 - c similar, scale factor 1.5
 - d not similar as two corresponding sides have a scale factor of 5, the other one doesn't
- **2 a** 3 **b** angle R **c** BA
- 3 **a** angle $B = 180 (75 + 50) = 55^{\circ}$ and angle $P = 180 (55 + 50) = 75^{\circ}$, so both triangles have the same angles of 50^{\circ}, 55^{\circ} and 75^{\circ}
 - **b** PR **c** BC **d i** 28 cm **ii** 6 cm
- **4 a** 40° **b** 1.5
 - c Multiply length AB by 1.5
- **5 a** 8 cm **b** 7.5 cm
- 6 a i ABC with DEF
 - **ii** 3
 - iii x = 3 cm, y = 18 cm
 - **b i** GHI with LKJ **ii** 0.5
 - iii x = 8 cm, y = 3.5 cm
 - c i PQR with TUS
 - **ii** 1.5
 - iii x = 5.33 cm, y = 12 cm
 - d i MNL with WUV
 - **ii** 5
 - iii x = 9 cm, y = 40 cm
- 7 a Sides in same ratio
 - **b** 3 **c** 13 cm **d** 39 cm
- 8 a The interior angles of all regular hexagons are 120°, so all the angles of each hexagon will correspond, hence similar shapes.
 - **b** 12 cm
 - **c** 6.928 cm

Exercise 23D

1 82 m

2
$$\frac{\text{pole}}{330} = \frac{400}{600}$$
, pole = $330 \times \frac{4}{6} = 220$ feet

- 3 15 m
- 4 3.3 m



. . . .

b 1.8 m

- 6 a i ABC and ADE ii 9 cm **b i** ABC and ADE **ii** 12 cm
- 7 а 34° 9 cm 9 cm 34°/_____B **b** $\frac{BC}{9} = \frac{9}{6}$, BC = $9 \times \frac{9}{6} = 13.5$ cm
- 8 c 4 cm

Review questions

- 1 **a** B, C and D
 - **b i** rotation
 - ii reflection
 - iii reflection
 - iv enlargement
 - **v** no transformation
 - **c** It is not true because E, the enlarged triangle, is not congruent, and nor is F.
- Ellie is correct: 2
 - a both triangles have an identical set of angles: 90°, 65° and 25°

- **b** both shapes are rectangles and the lengths of the large rectangle are four times larger than the small one, so the large rectangle is an enlargement of the small one.
- 3 a always
 - **b** always
 - c sometimes
 - **d** sometimes
 - e always
- a congruent SAS 4 **b** congruent RHS c not congruent **d** congruent SSS
- 5 Scale factor between similar triangles is $1000 \div 40 = 25$, hence tree height = 140×25 = 3500 cm = 35 m
- 6 Construction of a triangle with sides exactly the same size as the given triangle
- ABX with DCX and ADX with BCX 7
- 8 Andrew is correct. Eve has calculated the length of AD (8 cm) so ED should be 2 cm.
- **9** 4.5 cm²

Chapter 24 – Probability: Combined events

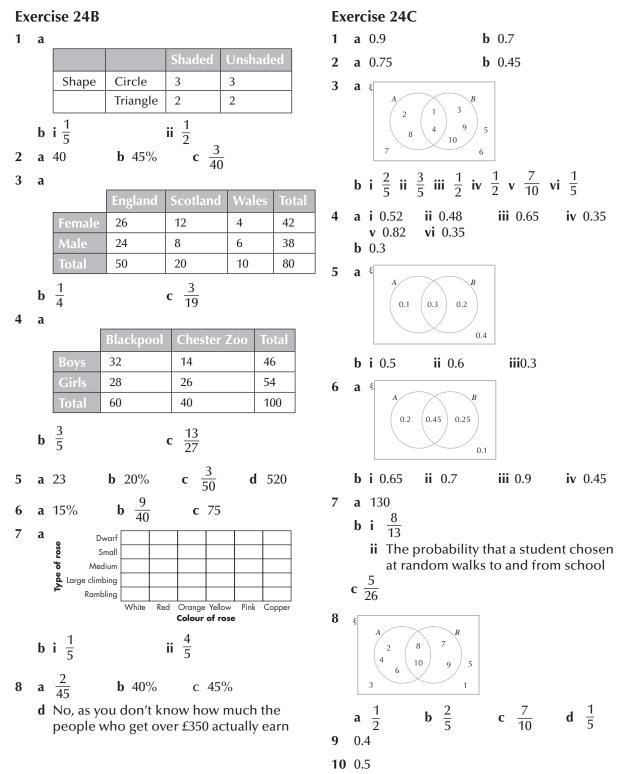
Exercise 24A

1 a 7

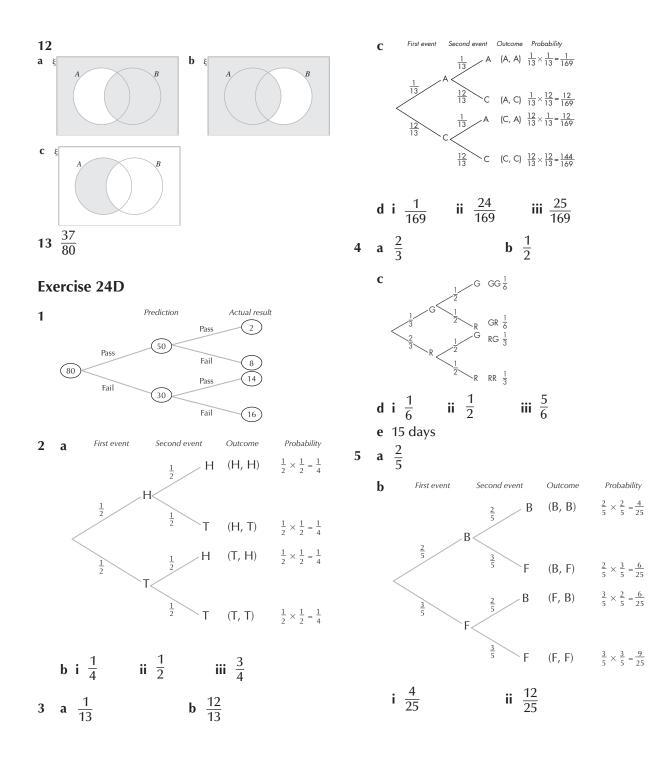
b 2 and 12

	a C	1	U			
		Score	Probability	/		
		2	$\frac{1}{36}$			
		3	$\frac{1}{18}$			
		4	$\frac{1}{12}$			
		5	$\frac{1}{9}$			
		6	$\frac{5}{36}$			
		7	$\frac{1}{6}$			
		8	$\frac{5}{36}$			
		9	$\frac{1}{9}$			
		10	$\frac{1}{12}$			
		11	$\frac{1}{18}$			
		12	$\frac{1}{36}$			
	d	$\frac{1}{12}$	ii $\frac{1}{3}$	iii $\frac{1}{2}$		
		iv $\frac{7}{36}$		vi $\frac{5}{18}$		
2	a	$\frac{1}{12}$	b $\frac{11}{36}$	c $\frac{1}{6}$	d	$\frac{5}{9}$
3	a	$\frac{1}{36}$		c $\frac{5}{18}$		
4	a	$\frac{1}{4}$	b $\frac{1}{2}$	c $\frac{3}{4}$	d	$\frac{1}{4}$
5	a ,	<u>1</u> 12	b $\frac{1}{4}$	c $\frac{1}{6}$		

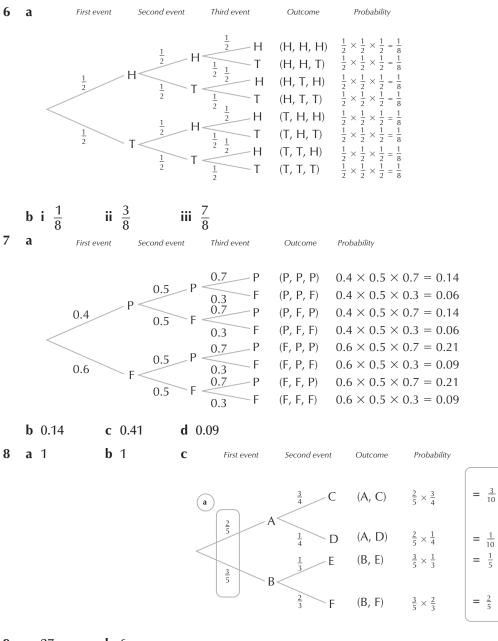
6	a ey (5 5	4	3	2	1	0			
	id di	5 4	3	2	1	0	1]		
	Score on second dice	5 4 4 3 3 2	2	1	0	1	2			
	on se	3 2	1	0	1	2	3			
	ore	2 1	0	1	2	3	4			
	Sc	1 0	1	2	3	4	5			
		1	2	3	4 first	5 dice	6			
			5001	e on	11151	uice	3			
	b i $\frac{5}{18}$,	0		$i \frac{1}{9}$		iv	0	v	$\frac{1}{2}$
7	a	5 4 3 2 1	6	7	8 0	7 1	0			
	conc	4	5	6	7 8		9			
	n se	3	4	5	6 7		8			
	ore o sni	2	3	4	5 0		7			
	Sco	1	2	3	4		6			
		L	1	2	3 4	4 3	5			
			S		on f	irst				
				spi	nner					
	b 6		1	3			1			3
	c i $\frac{4}{25}$	5	$\frac{1}{2}$	25		iii	$\frac{1}{5}$		iv	$\frac{5}{5}$
8	$\frac{8}{64} = \frac{1}{8}$	<u>1</u> 8								
9	It will	show	/ all	the	pos	sibl	e p	orodu	cts.	
10	a HHI	H, HI	НТ, I	HTF	I <i>,</i> T⊦	ΙH,	ΗТ	Т, ТН	Τ,	
	TTH	I, TTT	-							
	b i $\frac{1}{8}$	$\frac{3}{8}$	iii	$\frac{1}{8}$	iv $\frac{7}{8}$	r R				
11	a 16	0	b 3	0			10	24	d	2 ⁿ
12										
		1	2	3	4	5		6		
	1	2	3	4	5	6		7		
	2	3	4	5	6	7		8		
	3	4	5	6	7	8		9		
	4	5	6	7	8	9		10		
	5	6	7	8	9	1	0	11		
	6	7	8	9	10	1	1	12		



11 a $(A \cup B)'$ **b** $(A \cap B)'$



(b)

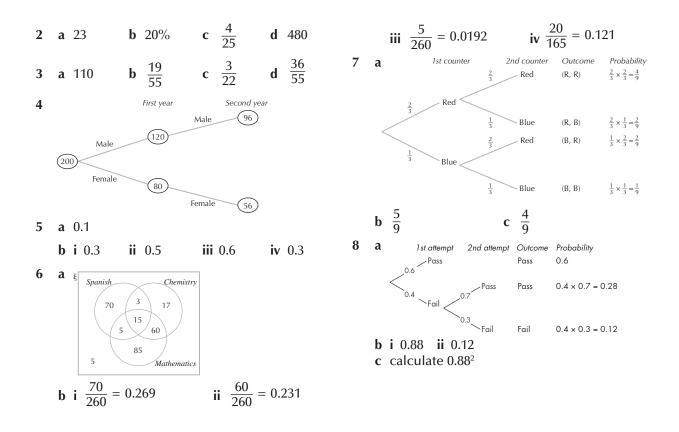


9 a 27 **b** 6 **10 a** $\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{16}$ **b** $\frac{1}{2}n$

Review questions

1	а							
				Spinner				
				1	2	3	4	5
		Coin	Н	1, H	2, H	3, H	4, H	5, H
			Т	1, T	2, T	3, T	4, T	5, T
			-					

b $\frac{3}{10}$



Chapter 25 - and standard		oer: Pov	vers	2	a x^8 e x^{12} i x^{16}		$x^9 x^{13}$	c g	x^8 x^{11}		$x^5 x^{10}$
Exercise 25A				3	a 6 ³		6 ⁵	С		d	6 ⁰
		c 7 ² g 4 ¹	d 5 ³ h 1 ⁷		e 6^1 i 6^2	f	6 ³	g	6 ²	h	6 ¹
i 0.5 ⁴ j	100 ³	8 .		4	a x^4		x ⁵	С		d	
$\begin{array}{ccc} \mathbf{a} & 3 \times 3 \times 3 \times 3 \\ \mathbf{b} & 9 \times 9 \times 9 \end{array}$	5				e x^6 i x^9	t	<i>x</i> ⁵	g	<i>x</i> ²	h	X°
c 6×6				5	a 1	b	6 ⁰	С	1		
$\begin{array}{c} \mathbf{d} 10 \times 10 \times 10 \\ \mathbf{e} 2 \times 2 \times 2 \times 2 \end{array}$		· · · · · · · · ·		6	a 1	b	5 ⁰	С	1		
f 8		. ~ _ ^ _ ^ _ ^ _ ^ _ ^ _ ^ _ ^ _ ^ _ ^ _		7	Answers for	or p	ower 0 ar	e a	lways 1.		
g $0.1 \times 0.1 \times 0$ h 2.5×2.5 i $0.7 \times 0.7 \times 0$				8	Two values example <i>a</i>				h a sum (of 7	7, for
i $0.7 \times 0.7 \times 0$ j 1000×1000				9	a $a = 1$ and b $x = 1$	dx	= 2				
	b 243 d 125 f 1296			10	a $6a^5$ d $-6a^4$		$9a^2$ $8a^8$	c f	8 <i>a</i> ⁶ -10 <i>a</i> ⁻³		
	n 1)		11	a 3 <i>a</i> d 6 <i>a</i>		$4a^{3}$ $4a^{3}$	c f	3a ⁴ 5a ⁻⁴		
c 36 c	b 729 d 100 000			12	a Possibleb Possible						
	i 8 h 6.25			13	a $3a^{3}b^{2}$	b	$3a^2c^4$	С	$8a^2b^2c^3$		
i 0.343 j	1 000 000)		14	a $8a^5b^4$ d $2ab^3$		$10a^{3}b$ $8a^{-5}b^{7}$		$30a^{-2}b^{-2}$ $4a^{5}b^{-5}$		
	2 ³	J ⊏ 2		15	a 4 ⁶	b	4 ¹⁵	с	46		
		d 5^2			d 4 ⁻⁶	e	46	f	4 ⁰		
7 a 1 b d 1 e		c 1		16	12 (<i>a</i> = 2, <i>b</i>	= 1	, <i>c</i> = 3)				
8 Any power of	1 is equal	to 1.		Exe	ercise 25C						
9 10 ⁶				1	a 60 000	b	120 000	с	150		
10 10 ⁶					d 42 000		1400	f	300		
	-1 -1	c 1			g 400 j 4500	k	8000 8000	i I	160 000 250 000		
		c –1		2	a 5 e 7	b f	50 300	C σ	25 6		30 30
d 1 e	1				i 1	j	15	g k	40	ï	5
13 2 ²⁴ , 4 ¹² , 8 ⁸ , 16 ⁶					m 40	n	320				
14 $x = 7$				3	a 54 400	b	16 000				
Exercise 25B				4	30 × 90 000						
1 a 5 ⁴ b		c 5 ⁵ g 5 ⁶	d 5 ³ h 5 ⁹		600×8000 5000×4000 $200\ 000 \times 7$) = (20 000 000				

i 5⁸

5 1400 million

6	a	31	b	310	С	31	00	d	31 000
7	a	65	b	650	С	65	00	d	65 000
8	a	0.31	b	0.031	С	0.0	0031	d	0.000 31
9	a	0.65	b	0.065	С	0.0	0065	d	0.000 65
10	d g j m	346 246 23 456		 b 34.5 e 207.89 h 0.76 k 98 765 n 6000) 5.4	f i I	56 78 999 (43 23	000	00
11	a c e g i k	0.025 0.004 (0.207 (0.0246 0.000 (0.098 7 0.000 (57 39 000 765			d f h j I	0.000 0.000	5 043 000	000 06
12		57 000	000	b 57 0 e 21 h 98	6				0

13 They are all true.

Exercise 25D

1	a	0.31	b	0.031	С	0.0031	d	0.000 31
2	a	0.65	b	0.065	С	0.0065	d	0.000 65
3		9999999999999999999999999999999999999						
4	a	31	b	310	С	3100	d	31 000
5	a	65	b	650	С	6500	d	65 000
6	a	250		b 34	1.5	c 0.	004	67
	d	34.6		e 89	97 (000 f 0.	008	65
	g	60 000	000	h 0.	000) 567		
7	c e g	2.5×10^{-10} 4.67×10^{-10} 2.078×10^{-10} 5.6004	10 ⁴ : 10	d ¹⁰ f h	3.4 5.6	5×10^{-1} $\times 10^{9}$ 78×10^{-4} 7×10^{-3}		
8	2.	7797 × 1	04					

- $\textbf{9} \quad 2.815 \; 81 \times 10^{5} \text{, } 3 \times 10 \text{, } 1.382 \; 101 \times 10^{6}$
- **10** 1.298×10^7 , 2.997×10^9 , 7.4×10^4

	a 5.67×10^3 b 6×10^2 c 3.46×10^{-1} d 7×10^3 e 1.6 f 2.3×10^7 g 3×10^{-6} h 2.56×10^6 i 4.8×10^2 j 1.12×10^2 k 6×10^{-1} l 2.8×10^6
13	a 2×10^{13} , 1×10^{-10}
	b mass = 2×10^3 g (2 kg)
14	5×10^4
15	7800, $3.7 \times 2.1 \times 10^4$, 7.85×10^4 , 79×10^3
16	$0.0005, 4 \times 10^{-3}, 0.52 \times 10^{-2}, 6 \times 10^{-2}$
	a 2.75×10^{12} b 1.24×10^7 c 1.8×10^5 d 1.2×10^8
	a 1.8×10^4 b 1.7×10^7 c 8.8×10^7 d 1.9×10^5
	 a 1×10° b 1.0×10 c It is easier to use ordinary numbers in

c It is easier to use ordinary numbers in this case

Review questions

1	a	64	b	64	С	10 000 0	000	
2	a	62	b	4900	С	3.47	d	0.123
3	a	6 000	b	300 000	С	80	d	40
4	a	196	b	units dig should e			25	so it
5	b			ied the po e added t			out	he
6	a	t^8	b	m^5	С	$9x^6$	d	$10a^{7}h^{5}$
7	a	<i>x</i> ¹¹	b	m^{-5}	С	$8k^{5}m^{3}$		
-		x^{11} 7.5 × 10 ⁴			С	$8k^5m^3$		
8	a	7.5×10^{4}	b		С	8 <i>k</i> ⁵ <i>m</i> ³		
8 9	a a	7.5×10^{4}	b	0.009	С	8 <i>k</i> ⁵ <i>m</i> ³		
8 9	a a a	7.5×10^4 2y	b b	0.009	C	8 <i>k</i> ⁵ <i>m</i> ³		

Chapter 26 – Algebra: Simultaneous equations and linear inequalities

Exercise 26A

1	a $x = 4\frac{1}{2}, y = 1\frac{1}{2}$	b $x = -2, y = 4$
	c $x = 2\frac{1}{2}, y = -1\frac{1}{2}$	d $x = 3, y = 10$
	e $x = 9, y = -2$	f $x = 0.5, y = 4$
2	a <i>a</i> = 7, <i>b</i> = 10	b $c = 4, d = 11$
	c $e = 5, f = 3$	d $g = -1, h = 6$
	e $j = 13, k = 2$	f $m = 1.5, n = -7$
3	x = 12, y = 2	

Exercise 26B

1	a $x = 9, y = -2$	b $x = \frac{1}{2}, y = 5$
	c $x = -3, y = -10$	d $x = -12, y = -6$
	e $x = 3, y = 5$	f $x = 0.5, y = 6.5$
2	a $x = 2\frac{1}{4}, y = 6\frac{1}{2}$	b $x = 4, y = 3$
	c $x = 5, y = 3$	d $x = 4, y = 5$
	e $x = 11, y = -3$	f $x = -7, y = 2$
3	a $x = 1, y = 3$	b $x = 5, y = 9$

Exercise 26C

1	a $x = 2, y = 5$ c $x = 1, y = 7$	b $x = 4, y = -3$ d $x = 1, y = -3$
	c $x = 1, y = 7$	d $x = \frac{1}{2}, y = -\frac{3}{4}$
	e $x = -1, y = 5$	f $x = 1\frac{1}{2}, y = \frac{3}{4}$
2	a $x = 5, y = 1$	b $x = 3, y = 8$
	c $x = 9, y = 1$	d $x = 7, y = 3$
	e $x = 4, y = 2$	f $x = 6, y = 5$
3	a $a = 10, b = \frac{1}{2}$	b $c = -3, d = 5$
	c $e = 1, f = 14$	d $g = -2, h = -5$
	e $m = 8, n = 0$	f $p = 3\frac{1}{2}, q = -2$
	g $r = 7, s = 7$	h $t = \frac{2}{3}, u = -1$
	i v = 56, w = 32	

Exercise 26D

- **1 a** 14*a* + *b* = 47 **b** *a* = 3, *b* = 5 **c** 146, 443
- **a** 3t + 5b = 810, 3t + 3b = 630 **b** i £1.20 ii 90p **c** £10.20
- **a** 10*x* + 5*y* = 840, 8*x* + 10*y* = 1044 **b** £4.07

- 4 (1, -2) is the solution to equations A and C;
 (-1, 3) is the solution to equations A and D;
 (2, 1) is the solution to B and C; (3, -3) is the solution to B and D.
- 5 84p
- 6 10.3 kg
- 7 p = 36, c = 22. Total weight for Baz is 428 pounds so he can carry the load safely on his trailer.
- **8** £4.40
- 9 $b = \pm 3.50$, $p = \pm 1.75$. Camilla needs ± 35 so she will not have enough money.
- **10 a** My age minus 6 equals 2 × (my son's age minus 6)
 - **b** x = 46 and y = 26
- 11 Amul £7.20, Kim £3.50
- **12 a** They are the same equation. Divide the first by 2 and it is the second, so they have an infinite number of solutions.
 - **b** Double the second equation to get 6x + 2y = 14 and subtract to get 9 = 14. The left-hand sides are the same if the second is doubled so they cannot have different values.

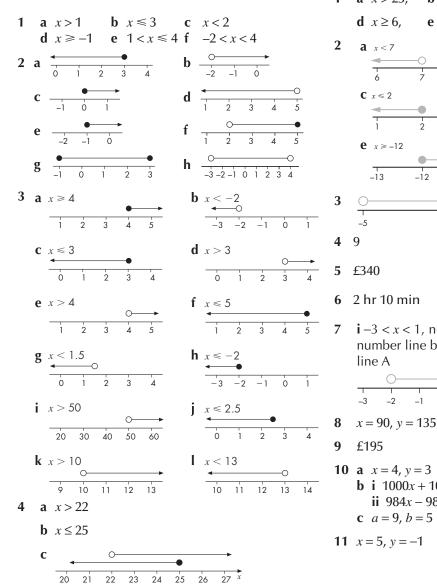
Exercise 26E

	a x < 3 e y < 3 i t > 18	b $t > 8$ f $t > 5$ j $x < 7$	 c p > 10 g x < 6 k x < 3 	h <i>y</i> < 15
	a 7 d 3	b 6 e 7	c 16	
-	a 11 d 3	b 16 e 7	c 16	

- 4 2*x* + 3 < 20, *x* < 8.50, so the most each could cost is £8.49
- 5 a Because 3 + 4 = 7, which is less than the third side of length 8
 - **b** *x* + *x* + 2 > 10, 2*x* + 2 > 10, 2*x* > 8, *x* > 4, so smallest value of *x* is 5
- 6 **a** x = 6 and x < 3 scores -1 (nothing in common), x < 3 and x > 0 scores +1 (1 in common for example), x > 0 and x = 2scores +1 (2 in common), x = 2 and $x \ge 4$ scores -1 (nothing in common), so we get -1 + 1 + 1 - 1 = 0

- **b** x > 0 and x = 6 scores +1 (6 in common), x = 6 and $x \ge 4$ scores +1 (6 in common), $x \ge 4$ and x = 2 scores -1 (nothing in common), x = 2 and x < 3 scores +1 (2 in common). +1 + 1 - 1 + 1 = 2
- **c** Any acceptable combination, e.g. x = 2, $x < 3, x > 0, x \ge 4, x = 6$
- **7 a** $y \le 4$ **b** $x \ge -2$ **c** $x \le \frac{14}{5}$ **d** x > 38 **e** $x < 6\frac{1}{2}$ **f** $y \le \frac{7}{5}$
- **8** a 3 < x < 6 b 2 < x < 5 c $-1 < x \le 3$ **d** $1 \le x < 4$ **e** $2 \le x < 4$ **f** $0 \le x \le 5$
- 9 6 bottles

Exercise 26F



d Apples could cost 23p, 24p or 25p.

1 and 4 5

6

a
$$x > 2$$

 $find the definition of the defini$

Review questions

- **1 a** x > 23, **b** $x \le 15$, **c** x < 48, **e** $5 \le x \le 25$ **d** $x \ge 6$, 2 **a** x < 7 **b** x > 1516 14 15 **d** $x \ge 4$ $\mathbf{C} x \leq 2$ -**e** $x \ge -12$ **f** x < 1312 13 -12 -13 3 _____ 9 4 5 £340 6 2 hr 10 min 7 **i** -3 < x < 1, number line B; **ii** -2 < x < 4, number line below; iii - 1 < x < 2, number line A -3 -2 -1 0 1 2 3 £195 **10** a x = 4, y = 3
 - **b** i $1000x + 1000y = 7000 \rightarrow x + y = 7$ ii $984x - 984y = 984 \rightarrow x - y = 1$ **c** a = 9, b = 5

11
$$x = 5, y = -1$$

12 Let straight part of track = D, inner radius of end = r, outer radius = r + xx being the width of the track Length of inner track = $2D + 2\pi r = 300$i Length of outer track = $2D + 2\pi (r + x) = 320$

.....ii Subtract equation i from ii to give

 $2\pi (r + x) - 2\pi r = 20$ $2\pi r + 2\pi x - 2\pi r = 20$ $2\pi x = 20$ x = 3.2 m (2sf)

Chapter 27 – Algebra: Non-linear graphs

Exercise 27A

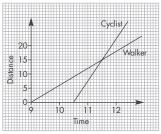
- **1 a** 1 hour **b** $1\frac{1}{2}$ hours
 - **c** $1\frac{1}{2}$ hours **d** 45 km per hour
 - e 30 km per hour
- **2 a i** 2 h **ii** 3 h **iii** 5 h **b i** 40 km/h **ii** 120 km/h **iii** 40 km/h
- **3 a** $2\frac{1}{2}$ km/h **b** 3.75 m/s **c** $2\frac{1}{2}$ km/h
- **4 a** 30 km **b** 40 km **c** 50 km **d** 100 km/h
- 5 a i 263 m/min (3 sf) ii 15.8 km/h (3 sf) b i 500 m/min
 - c Paul by 1 minute
- 6 a Patrick ran quickly at first, then had a slow middle section but he won the race with a final sprint. Araf ran steadily all the way and came second. Sean set off the slowest, speeded up towards the end but still came third.
 - **b i** 1.67 m/s **ii** 6 km/h
- 7 There are three methods for doing this question. This table shows the first, which is writing down the distances covered each hour.

Time	Walker	Cyclist
9am	0	0
9:30	3	0
10:00	6	0
10:30	9	0
11:00	12	7.5
11:30	15	15
12:00	18	22.5
12:30	21	30

The second method is algebra:

Walker takes *T* hours until overtaken, so $T = \frac{D}{6}$; Cyclist takes *T* – 1.5 to overtake, so *T* – 1.5 = $\frac{D}{15}$. Rearranging gives 15T - 22.5 = 6T, 9T = 22.5, T = 2.5.



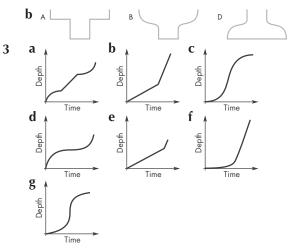


All methods give the same answer of 11:30 when the cyclist overtakes the walker.

- 8 a Vehicle 2 overtook Vehicle 1
 - **b** Vehicle 1 overtook Vehicle 2
 - c Vehicles passed travelling in different directions
 - d Vehicle 2 overtook Vehicle 1
 - **e** 17:15
 - f 32 mph if you only count travelling time, or 11.3 mph if you count total time.

Exercise 27B

- 1 a Two taps on
 - **b** One tap on
 - c Maureen gets in the bath
 - d Maureen has a bath
 - e Maureen takes the plug out, water leaves the bath
 - f Maureen gets out of the bath
 - g Water continues to leave the bath until the bath is empty
- 2 a Graph C



Exercise 27C

For questions 1-5 check that the graph is correct for the values in the table.

x	-5	-4	-3	-2	-1	0	1	2	3	4	5
y	-25	-16	-9	-4	-1	0	1	4	9	10	25

2

<u> </u>											
x	-3	-2	-1	0	1	2	3				
у	27	12	3	0	3	12	27				

3 a

<u> </u>	~										
x	-5	-4	-3	-2	-1	0	1	2	3	4	5
y	27	18	11	6	3	2	3	6	11	18	27

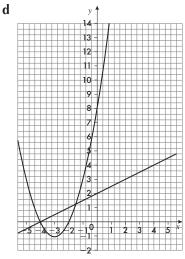
b y = 2

4 a

x	-5	_4	-3	-2	-1	0	1	2	3	4	5
x^2	25	16	9	4	1	0	1	4	9	16	25
-3x	15	12	9	6	3	0	-3	-6	-9	-12	-15
у	40	28	18	10	4	0	-2	-2	0	4	10

b 1.8 **c** -1.2, 4.2 **d** y = 0

- **5 a** Values of *y*: 7, 0, -5, -8, -9, -8, -5, 0, 7
 - **b** -6.75
 - **c** −0.45 or 4.45
- **6 a** Values of *y*: 15, 8, 3, 0, -1, 0, 3, 8, 15



e (-4, 0) and (-1.5, 1.25)

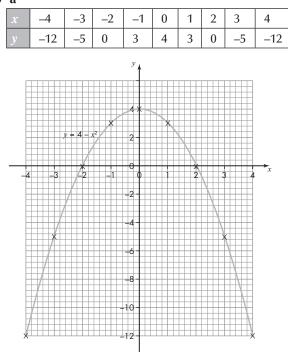
- 7 **a** Values of *y*: 8, 3, 0, -1, 0, 3, 8 **b** (0, 0) and (3, 3)
- **a** They have the same value, y = 4**b**

~												
x	-3	-2	-1	0	1	2	3	4	5	6	7	
y	28	19	12	7	4	3	4	7	12	19	28	

Since the quadratic graph has a vertical line of symmetry and the *y*-values for x = 1 and x = 3 are the same, this means that the *y*-values will be symmetric about x = 2. Hence the *y*-values will be the same for x = 0 and x = 4, and so on.

- **9 a** Values of *y*: 12, 5, 0, -3, -4, -3, 0, 5, 12 **b** (2, 0) and (-2, 0)
 - **c** –1.75
 - **d** x = 3.5 or -3.5

10 a

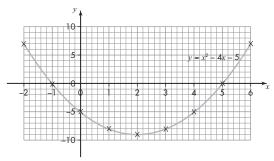


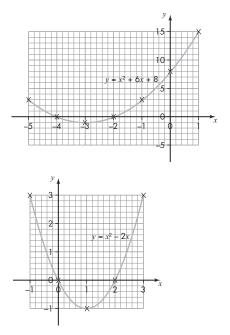
- **b** (2, 0) and (-2, 0)
- **c** 1.75
- **d** x = 3.5 or -3.5
- e The curves are reflections in the *x*-axis.

- **a** −2, −5 **c** -6, 3 1 **b** 4, 9 **d** −3, −1 **e** −6, −4 **f**−3, 2 **g** -1, 3 **h** -4, 5 i 1, -2 **j** 2, -5 **k** 7, −4 **3**, 2 **m** 1, 5 **n** 4, 3 **o** -7, 5 **2** a -2, -3 **b** -4, -1 c 2,4 **d** -2.5 e -3.5 f -6.3 **g** –1, 2 **h** –5 i 7 **i** −9, −2 **k** 3, 5 **I** -6, 2 **m** -2 **n** 4 **o** −2, −6
- **3 a** $x^2 + 6x 55 = 25 + 30 55 = 0$ **b** x = -11
- 4 a 5, -10 b 7, -8 c 1, 18 d -2, -11 e 2, -15 f 3, 10 g -1, -999 h 1 i -10, 1
- 5 $x^2 + 8x + 16 = (x + 2)(x + 6) = 0$ so the answers are -2 and -6
- 6 $x^2 + 5x 6 = (x + 6)(x 1) = 0$ so the answers are 1 and -6
- 7 **a** Area = $(x + 1)(x + 2) = x^2 + 3x + 2 = 42$, therefore $x^2 + 3x - 40 = 0$
 - **b** x = 5 cm (discard the negative value as x is a length)
 - c Perimeter = 26 cm
- 8 x = 9 cm

Exercise 27E

- **1 a** (0, -5), (0, 8) and (0, 0).
 - **b** Each equation is written in the form $x^2 + ax + b$. You should find that the *y*-intercept is the value of *b*.



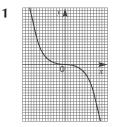


- **2 a** *x* = -1 or 5; *x* = -2 or -4; *x* = 0 or 2 **b** (-1, 0), (5, 0); (-4, 0), (-2, 0); (0, 0), (2, 0)
- 3 (2, -9), (-3, -1), (1, -1)

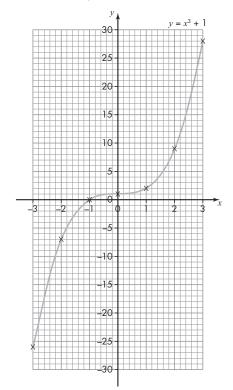
Exercise 27F

- **1 i** (0, 5) **ii** (-5, 0) and (1, 0) **iii** (-2, 9)
- **2** i (0, -3) ii (-1, 0) and (3, 0) iii (1, -4)
- a roots: (-2, 0) and (2, 0); y-intercept (0, -4)
 b roots: (0, 0) and (6, 0); y-intercept (0, 0)
 c roots: (-1, 0) and (3, 0); y-intercept (0, -3)
 d roots: (-11, 0) and (-3, 0); y-intercept (0, 33)
- 4 (2, -1)
- **5** i (0, 9) ii (3, 0) and (-3, 0) iii (0, 9)
- **6 i** (0, 16) **ii** (2, 0), (8, 0) **iii** (5, -9)
- 7 i (0, -15) ii (3, 0), (-5, 0) iii (-1, -16)
- 8 i (0, -6) ii (-2, 0), (1.5, 0) iii (-0.25, -6.1)

Exercise 27G

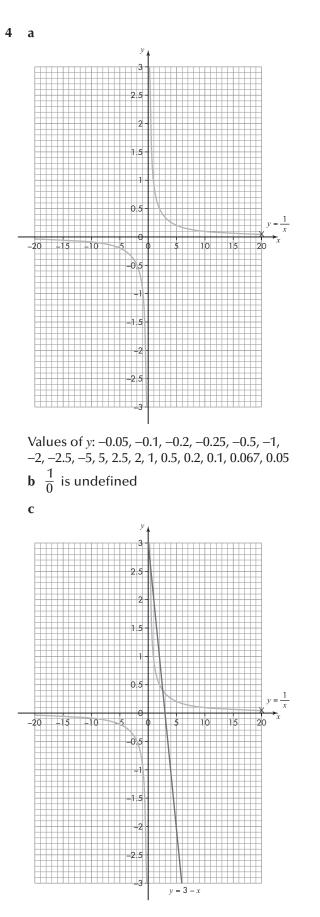


2 a Values of *y*: -26, -7, 0, 1, 2, 9, 28



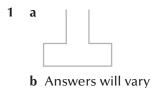
b 16.6

a Values of y: -24, -12.63, -5, -0.38, 2, 2.9, 3, 3.13, 4, 6.38, 11, 18.63, 30
 b 4.7 c (-1.45, 0)

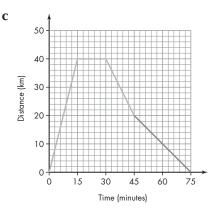


- **d** 0.4 and 2.6
- 5 a Quadratic b Linear c None
 d Reciprocal e None f Cubic
 g Linear h None i Quadratic

Review questions



- 2 a 160 km/h
 - **b** 80 km/h



- **d** 14:41
- 3 x = 9 or 10
- **4** 23, 10, 5, 2

