Guidance	on the use of codes for this mark scheme
М	Method mark
Α	Accuracy mark
В	Working mark
cao	Correct answer only
oe	Or equivalent
ft	Follow through

Question	Working	Answer	Mark	AO	Notes	Grade
1 ai ii iii		No Yes Yes	B1 B1 B1	2		В
iv bi		Assume third angle is 90°. 180° – 90° = 90°. So both the remaining angles must be acute. If the third angle is bigger than 90° both remaining must also be acute. If the third angle is acute you would need to make one of the other angles at least 90°.	B1 B1 B1		B1 for full explanation B1 for clarity of explanation	
ii		Example with 2 acute angles.	B1		B1 for giving an example that works	
iii		Example with 1 obtuse angle.	B1		B1 for giving an example that works	
iv		The obtuse angles will be $(90^{\circ} + x)$ and $(90^{\circ} + y)$ , adding these together you get $180^{\circ} + x + y$ , which is more than the sum of the angles in a triangle, so it's impossible.	B1 B1		B1 for a correct explanation B1 for clear communication	
С		If you draw a line between two parallel lines, the two allied angles formed add up to 180°, which leaves nothing for a third angle.	B1 B1		B1 for clear explanation B1 for clarity of the communication	

	1		1	1		1
2		Sometimes. Here are examples, one of	B1	2	B1 for sometimes	В
		when it is not true and on of when it is	B2		B1 for example that shows it can be true	
		true.			B1 for example that shown it can be false	
		5 cm	B1		B1 for clear communication of both	
		A 2 cm				
		6 cm				
		B 2 cm				
		8 cm				
		C 1 cm				
		Chana A: parimeter of 14 am				
		Shape A: perimeter of 14 cm				
		area 10 cm <sup>2</sup>				
		Shape B; perimeter of 16 cm				
		area 12 cm <sup>2</sup>				
		Shape C; perimeter of 18 cm				
		area 8 cm <sup>2</sup>				
		Statement is true for A and B, but false				
		for B and C.	4			
			4			
3		True. Demonstration of proof of area	B1	2	B1 for true	В
		triangle equal to half area of rectangle	B1	3	B1 for clear explanation	
		true also for non-right angled triangle.	M1		M1 for concise communication with clear diagrams	
		B -	IVII		With for concise communication with clear diagrams	
		4 cm				
		9 cm T 3 cm C				
		Area of ABT = $\frac{1}{2}$ of AEBT				
		2				
		1 -4 -2 - 2 -42 - 2				
		$=\frac{1}{2}$ of 36 cm <sup>2</sup> = 18 cm <sup>2</sup>				
		_				
		Area of CTB = $\frac{1}{2}$ of CTBF				
		2				
		4				
		$=\frac{1}{1}$ of 12 cm <sup>2</sup> = 6 cm <sup>2</sup>				
		$=\frac{1}{2}$ of 12 cm <sup>2</sup> = 6 cm <sup>2</sup>				
		<u>=</u>				
		Area of triangle ABC = $18 + 6 = 24 \text{ cm}^2$				
		Area of triangle ABC = $18 + 6 = 24 \text{ cm}^2$				
		<u>=</u>				
		Area of triangle ABC = $18 + 6 = 24 \text{ cm}^2$ = $\frac{1}{2} \times 4 \times 12$				
		Area of triangle ABC = $18 + 6 = 24 \text{ cm}^2$				
		Area of triangle ABC = $18 + 6 = 24 \text{ cm}^2$ = $\frac{1}{2} \times 4 \times 12$	3			

4  A rotation of 90° anticlockwise around point $(2, 2)$ .		M1 A1 A1 B1	3	M1 for a process of finding the centre of rotation A1 for indicating 90° anticlockwise (or 270°clockwise) A1 for indicating centre of rotation as (2, 2) B1 for full, clear description	В
		_			
Area of front and back = $2 \times 12 \times 25 = 600 \text{ m}^2$		M1	2	M1 for correct formula for area of rectangle	В
Area of sides = $2 \times 12 \times 12 = 288 \text{ m}^2$ Area of openings = $40 \times 2 \times 1 = 80 \text{ m}^2$		M1		M1 for correct method of finding total surface area	
Total area to be painted = $600 + 288 - 80$ = $808 \text{ m}^2$ For 2 coats of paint, area = $2 \times 808$ = $1616 \text{ m}^2$		A1 B1		A1 for 808 cao	
Number of litres of paint needed = 1616 ÷ 16 = 101 litres Number of cans of paint = 101 ÷ 10 = 10.1		M1		M1 for correct method of finding number of tins	
11 cans are needed.		A1		A1 for correct number of tins used	
Cost of paint = 11 x £25 = £275		M1 A1		M1 for method of finding cost of tins A1 for 275 cao	
		AI		AT 101 273 Cd0	
Assume painters work 5 days per week. Number of days = $2 \times 5 = 10$		M1		M1 for method of calculating cost for two days	
Cost of painters = $10 \times 3 \times 120 = £3600$		A1		A1 for 3600 cao	
Total cost = £275 + £3600 + £500 = £4375 Add 10%: £4375 × 1.1 = £4812.50		A1 M1		A1 for 4375 cao M1 for correct calculation of 10%	
Add 20% VAT: £4812.50 × 1.2 = £5775		M1		M1 for correct calculation of 20%	
	The builder should charge the council	A1		A1 for correct total cost £5775	
	£5775.	B2		B1 for clear explanation marks with structure and technical use of language in explanation and	
				B1 for stating any necessary assumptions	
		16			

6 a	Area of face = $4^2$ = $16 \text{ m}^2$ Area of circle = $\pi r^2$ Using $\pi$ = $3.142$ area of circle = $\pi 1.2^2$ = $4.524  ext{ 48 m}^2$ Remaining SA of front face = $16 - 4.524  ext{ 48}$ = $11.475  ext{ 52 m}^2$ Total remaining surface area: front and back = $2  ext{ x } 11.47552$ = $22.95104  ext{ m}^2$ Area of other four sides = $4  ext{ x } 16 = 64  ext{ m}^2$		M1 M1 A1 A1 A1	3	M1 for the correct method of finding area of a rectangle M1 for correct method of finding area of a circle A1 for correct area of circle A1 for correct area of face with circle.  A1 for correctly combining front and back A1 for correct area of the other 4 sides	В
b	Total = 64 + 22.951 04 = 86.951 04 m <sup>2</sup> Volume of original cuboid = $4^3$ = 64 m <sup>3</sup> Volume of cylinder = $\pi r^2 h$ = $\pi r^2 4$ = 4.524 48 × 4 = 18.097 92 m <sup>3</sup> Remaining volume = 64 - 18.097 92 = 45.902 08 m <sup>3</sup>	87.0 m <sup>2</sup> 45.9m <sup>3</sup>	M1 A1 M1 A1 A1		A1 for correct total area, rounded to 2,3 or 4 sf  M1 for correct method for finding volume of cube A1 for 64 M1 for correct method for finding volume of cylinder A1 for a correct volume of cylinder (any rounding)  A1 for correct total volume, rounded to 2,3 or 4 sf	
С	Amount of light blue paint = outside area $\div$ coverage of 1 litre of paint = $87 \div 9 = 9.666$ Surface area inside cylinder = $2\pi rh$ = $2 \times 3.142 \times 1.2 \times 4$ = $30.1632 \text{ m}^2$ $30.1632 \div 9 = 3.3515$	Amount of light blue = 9.7 litres  Amount of dark blue = 3.4 litres	M1 A1 M1 A1 A1		M1 for dividing total outside surface by 9 A1 for correct answer rounded to 1,2,3 or 4sf  M1 for correct method of finding curved surface area A1 for a correct surface area (any rounding) A1 for correct answer to 2,3 or 4 sf	
7		Yes, he is correct. This is one of the conditions for being able to draw a triangle (SAS).	B1 <b>1</b>	3	B1 for clear communication that he is correct	М
8		60° 60° 9 60° 9	B4 <b>4</b>	3	B1 for each different possible triangle shown and clearly labelled	М
9	A 5 cm B	The locus is none of these as it is a point, so d.	B1 B1 M1	3	B1 for stating d is the only correct option B1 for a clear explanation of why M1 for clear communication, using diagrams to illustrate answer	M

10 a	Angles in a triangle add up to 180°.		B1	2	B1 for clear explanation	М
10 a	You can split any quadrilateral into two		M1	2	M1 for communication with clear diagram	IVI
	triangles.					
	The vertices the sum of the interior angles of					
	Therefore, the sum of the interior angles of any quadrilateral = $2 \times 180^{\circ}$ .					
	arry quadrilateral = 2 x 100 .					
	$x$ $i = 108^{\circ}$		B1			
	x $y$ $z$ $z$ $z$		"		B1 for showing inter angles of quadrilateral = 2 x 180	
b						
	$\delta = 108^{\circ}$		M1		M1 for a clear diagram correctly showing the three	
	0 = 100		5.4		triangles	
	x $y$ $y$		B1		B1 for identifying each angle of the triangles with symbols showing which angles are equal	
					Symbols showing which angles are equal	
	For the two outside triangles, use the sum of		B1		B1 for clear explanation	
	the angles in triangle = 180° and the interior		M1		M1 for correct method of finding angle x	
	angle of a regular pentagon = $108^{\circ}$ . $108^{\circ} + 2x = 180^{\circ}$					
	$2x = 180^{\circ} - 108^{\circ}$					
	$2x = 72^{\circ}$					
	<i>x</i> = 36°		A1		A1 for 36°	
	For the middle triangle, use interior angle of		M1		M1 for correct method of finding angle y	
	regular pentagon = 108°.					
	$y = 108^{\circ} - x$ $y = 108^{\circ} - 36^{\circ}$					
	y = 108 - 36 $y = 72^{\circ}$		A1		A1 for 72°	
	Using the sum of angles in triangle = 180°:		AI		AT 101 72	
	z = 180 - 2y		M1		M1 for correct method of finding angle <i>z</i>	
	z = 180 - 144					
	$z = 36^{\circ}$ Or $2x + z = 108^{\circ}$		A1		A1 for 36°	
	$x = 36^{\circ}$					
	$so 2 \times 36^{\circ} + z = 108^{\circ}$	Two triangles with one angle = 108°	B1		B1 for clear argument and stating assumptions used	
	$z + 72^{\circ} = 108^{\circ}$	and two other equal angles of 36°.	M1		M1 for use of diagram with clarity of explanation	
	z = 36°	One triangle with one angle = 36° and two angles = 72°.				
		two angles = 12.	14	1		

11		A line of symmetry has the same number of vertices on each side of the line, so there is an even number of vertices and therefore an even number of sides.	B2 M1	2	B1 for line of symmetry and number of vertices link B1 for reference to even number of vertices oe M1 for use of diagram to illustrate the answer	М
			3			
12 a		Suitable diagram, e.g.	B1	3	B1 for a correct diagram	М
b		Suitable diagram, e.g. as part a	B1		B1 for a correct diagram	
С		In a parallelogram opposite sides are equal. In a trapezium at least one set of opposite sides are parallel. Therefore every parallelogram is also a trapezium.	B1 M1		B1 for a correct diagram of a parallelogram M1 for a correct explanation to support the diagram	
13		Always true. To follow a path around the perimeter of any polygon, you must turn through a total of 360° to get back to where you started. Therefore the external angles of every polygon sum to 360°.	B1 B1 M1	2	B1 for always true B1 for a satisfactory explanation M1 for use of diagram to illustrate answer	М
14	Ratio = $6:5:7$ 6+5+7=18 Sum of the angles in a triangle = $180^{\circ}$ and $180^{\circ} \div 18 = 10^{\circ}$ Therefore the angles are: $6 \times 10^{\circ} = 60^{\circ}$ $5 \times 10^{\circ} = 50^{\circ}$		M1 B1 M1	2	M1 for summing parts of ratio B1 for clear statement regarding angle sum of triangle M1 for dividing 180° by 18	M
	$7 \times 10^{\circ} = 70^{\circ}$	60°, 50°, 70°	B3		B1 for each correct angle found	
	Check: $60 + 50 + 70 = 180$		M1 7		M1 for showing the check that the answers sum to 180°	

15	Assume the height of one large triangle is	25 cm <sup>2</sup>	M1	2	M1 for stating assumptions clearly	М
.	equal to the radius of the large circle, 6 cm,	20 0111	1711	_	Will for stating assumptions slearly	171
	and its base is equal to the diameter of the					
	small circle, 3 cm.					
	6 - 1.5 = 4.5  cm					
	1.5 cm					
	Consider one shaded triangle.					
	Its height is (6 – 1.5) = 4.5 cm		B1		B1 for correct triangle height	
	The shaded triangle and the large triangle shown are similar triangles, where		N.4.4		NA for a consible way to active to triangle have longth	
	•		M1		M1 for a sensible way to estimate triangle base length	
	$\frac{\text{base of shaded triangle}}{3} = \frac{4.5}{6}$		A1		A1 for an accurate calculation at this point	
	Hence shaded base = $3 \times \frac{4.5}{6} = 2.25$					
	The area of one shaded triangle will be					
	area = $\frac{1}{2}$ × 2.5 × 4.5 = 5.0625 cm <sup>2</sup> .		M1		M1 for correct method of finding area of triangle	
	As an estimate, call this 5 cm <sup>2</sup> .					
	7.5 dir commate, can trio 5 cm .		A1		A1 for an suitably estimated area (1 or 2 sf)	
	So a reasonable estimate for the area of the					
	five shaded triangles could be:		M1		M1 for multiplying one area by 5	
	$5 \times 5 = 25 \text{ cm}^2$		A1		A1 for correct final estimation (integer value)	
			M1		M1 for clear explanation supporting the working	
			M1		M1 for clear diagrams illustrating the approach	
			10			

16 a	The interior angle of an equilateral triangle is 60°.  The interior angle of a square is 90°.  The interior angle of a regular hexagon is 60°.  All three are factors of 360° so these shapes will tessellate around a point.  This is not true for other regular polygons as their interior angles are not factors of 360°.  The interior angle of a regular octagon is 135°.  The interior angle of a square is 90°.  Using a similar argument to part a: 2 × 135° + 90° = 270° + 90° = 360°	M1 M1 B1 B1 M1	2	M1 for clear explanation of all three shapes M1 for use of clear diagrams to support the explanation B1 for clear explanation. B1 for clear explanation M1 for use of clear diagrams to support the explanation	M
		8			
17	All three sides (SSS). Two sides and the included angle (SAS). Two sides and a non-included angle (SSA). Two angles and a side (ASA or AAS).	B4 4	3	B1 for each correct statement	М

b  True. A frombus with right angles must be a square.  True. A frombus with right angles must be a square.  True. A frombus with right angles must be a square.  True. A frombus with same length so it does not flave to be a rhombus.  B1  B1 for clear explanation  M1 for clear use of diagrams to support explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation angle, hence the whole shape can have no more than two acute angles. Pop. 80°, 80°, 80°, 80°, 80°, 80°, 80°, 80°,	18 a	True. In a parallelogram opposite sides are parallel.	B1	3	B1 for true	М
In a square all sides are the same length. So a rhombus with right angles must be a square.  True. A rhombus must be a parallelogram does not all sides the same length so it does not have to be a rhombus.  True. Using the diagram of a trapezium above, you see each pair of angles between the parallel sides are allied angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have no more than two acute angles, e.g. 80°, 80°, 80°, 80° and 120°.  B1  B1 b1 for true B1 for clear explanation M1 for clear use of diagrams to support explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation supported by a clear diagram for clear use of a correct diagram: a diagram is essential		In a rhombus, opposite sides are parallel and all sides are the same length. So a rhombus is a type of	B1		B1 for clear explanation	
a parallelogram (part a) but a parallelogram does not all sides the same length so it does not have to be a rhombus.  M1  True. Using the diagram of a trapezium above, you see each pair of angles between the parallel sides are allied angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have no more than two acute angles, e.g. 80°, 80°, 80° and 120°.  B1 for clear explanation  M1 for clear use of diagrams to support explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation support the explanation and the parallel sides are allied angles, e.g. 80°, 80° and 120°.  B1 for true B1 for true B1 for true B1 for true B1 for clear use of diagrams to support the explanation supported by a clear diagram of a correct diagram is essential		In a square all sides are the same length. So a rhombus with right angles must be	B1		B1 for clear explanation	
True. Using the diagram of a trapezium above, you see each pair of angles between the parallel sides are allied angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have no more than two acute angles.  True. Vaquadrilateral can have three acute angles, e.g. 80°, 80°, 80° and 120°.  80°  80°  80°  80°  M1  B1 B1 for true B1 for clear use of diagrams to support explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation M1 for clear use of diagrams to support the explanation		parallelogram (part a) but a parallelogram does not all sides the same length so it				
above, you see each pair of angles between the parallel sides are allied angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have no more than two acute angles.  True. A quadrilateral can have three acute angles, e.g. 80°, 80°, 80° and 120°.  B1 for clear explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support the explanation  M1 for clear use of diagrams to support devaluation  M1 for clear use of diagrams to support devaluation  M1 for clear use of diagrams to support devaluation  M1 for clear use of diagrams are diagram of the explanation	c		M1		M1 for clear use of diagrams to support explanation	
angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have no more than two acute angles.  True. A quadrilateral can have three acute angles, e.g. 80°, 80°, 80° and 120°.  B1 B1 for true B1 for clear use of diagrams to support the explanation  B1 B1 for true B1 for clear explanation supported by a clear diagram M1 for clear use of a correct diagram: a diagram is essential						
True. A quadrilateral can have three acute angles, e.g. 80°, 80°, 80° and 120°.  B1 B1 For true B1 for clear explanation supported by a clear diagram M1 for clear use of a correct diagram: a diagram is essential		between the parallel sides are allied angles, adding up to 180°, so each pair can only have a maximum of one acute angle, hence the whole shape can have	M1		·	
12	d	acute angles, e.g. 80°, 80°, 80° and 120°.	B1		B1 for clear explanation supported by a clear diagram M1 for clear use of a correct diagram: a diagram is	
			12			

19	Look at the sides and/or angles you have been given and what you need to calculate.  When the triangle has a right angle, use Pythagoras' theorem when you need to work out one side length and you know the other two side lengths.	B1 B1	3	B1 for clear Pythagoras explanation B1 for clear right angled trig explanation	М
	Otherwise, when the triangle does not have a right angle, use sine, cosine or tangent when you need to work out an angle or a side.				
	Use the cosine rule to find angles when all sides of any triangle are known or to find the third side when two sides and the included angle are known.	B1		B1 for clear cosine rule explanation	
	Use the sine rule when two sides and one angle other than the included angle are known, or two angles and one side	B1		B1 for clear sine rule explanation	
	are known.	4			
20 ai	A suitable simple reflection.	B1	2	B1 for a diagram of a simple reflection	М
ii	A suitable reflection with a mirror line that is parallel to one of the sides of the shape.	M1	3	M1 for a clear explanation	
bi	A suitable simple rotation.	B1		B1 for a diagram of a simple rotation	
ii	A suitable rotation with centre not on an extension of one of the sides of the shape.	M1		M1 for a clear explanation	
		4			

21 a		The lengths of the sides change by the scale factor. Angles in the shape stay the same.	B2	2 3	B1 for correct statement about the lengths B1 for correct statement about the angles	М
b		The scale factor and centre of enlargement.	B2		B1 for scale factor B1 for centre of enlargement	
С		Suitable explanation of enlargements with use of diagram to help explanation. For example: Draw lines connecting corresponding vertices on the shape and its enlargement. The centre of	B1		B1 for a clear explanation	
		enlargement is where these lines cross.	B1		B1 for a good accurate diagram to support the explanation	
di	Diagram to help explanation:	Centre of enlargement outside the shape: the shape will move up and down a line that passes through the shape. Centre inside the original shape: the enlargement is either inside or around the shape depending on whether the scale factor is whole or fractional.	B2 M1		B1 for correct explanation of centre outside the shape B1 for correct explanation of centre within the shape M1 for clear diagrams used in both explanations	
	-12 -10 -9 -6 4 -2 0 2 4 6 8 10 12 X	When the centre is on a vertex the shape and enlargement share part of two sides. When the centre is on a side, the shape and enlargement shape part of the side. The image is smaller than the object.	B1		B1 for clear explanation.	
ii	The image is smaller than the object.		B1		B1 for clear explanation.	
			10			

22 a		When a shape has been translated the orientation is the same. When it has been reflected its orientation is different.	B2 M1	2	B1 for comment about orientation staying the same in translation B1 for comment about orientation being different in rotation M1 for a clear diagram to support the explanation	М
b		Rotating a rectangle about its centre: all the vertices move and the image is superimposed over the object.	B1 M1		B1 for clear explanation M1 for good diagram to support explanation	
		Rotating the rectangle about one of its vertices: all the other vertices move and, as the angle increases, the image is no longer superimposed over the object.	B1		B1 for clear explanation	
			M1 7		M1 for use of diagram to illustrate explanation	
23	Cross-sectional area is a quarter of circle		•	2		M
	with radius 1.5 cm and a rectangle 1.5 cm by 6.5 cm. area of quarter circle= $\frac{1}{4} \pi 1.5^2$		M1 A1 B1	3	M1 for method of finding area of the quadrant A1 for any rounding to 4 or more sf B1 for 9.75	
	= 1.767 145 9 cm <sup>2</sup> Area of rectangle 1.5 × 6.5 = 9.75 cm <sup>2</sup> Total area = 1.767 145 9 + 9.75 = 11.517 146 cm <sup>2</sup>		B1		B1 for any rounding to 4 or more sf	
	Total volume of wood is $11.517 \ 146 \times 12000 = 138205.75 \ cm^2$ . Convert this to m <sup>2</sup> by dividing by 1 000 000. Total volume = 0.138 205 75 m <sup>2</sup>	138 000 cm <sup>2</sup> or 0.14 m <sup>2</sup>	M1 A1		M1 for method of finding volume A1 for correct answer rounded to either 2 or 3 sf Accept alternative answer in cubic metres given correctly to 2 or 3 sf	

24	P		3		М
	Area of the poster $\theta$ $\pi^2$	B1		B1 for correct formula of area of sector	
	Area of the sector = $\frac{\theta}{360} \pi r^2$				
	Area of segment = area of sector – area of triangle	B1 M1		B1 for correct formula of area of triangle M1 for correctly stating the combined equation for	
	$=\frac{\theta}{360}\pi r^2 - \frac{1}{2}ab\sin\theta$			segment area	
	As $a$ and $b$ are both equal to $r$ , this becomes:	M1		M1 for correct use of $r$ in triangle formula	
	$\frac{\theta}{360}\pi r^2 - \frac{1}{2}r^2\sin\theta$				
	Factorising gives:				
	$r^2(\frac{\theta}{360}\pi - \frac{1}{2}\sin\theta)$	M1 A1		M1 for factorising A1 for correct factorisation	
	as required.	M1		M1 for clear use of diagram to support explanation	
		7			

25				2		М
	5 10 C					
	Using trigonometry:					
	$\cos \alpha = \frac{5}{6}$					
	$\alpha = \cos^{-1}\frac{5}{6}$		M1		M1 for correct trigonometric statement for angle	
	<i>α</i> = 33.557 31°		A1		A1 for any rounded answer to 2 or more sf	
	Area of segment of one circle					
	$=\frac{\theta}{360}\pi r^2 - \frac{1}{2}r^2\sin\theta$		M1		M1 for correct segment formula	
	$=r^2(\frac{\theta}{360}\pi-\frac{1}{2}\sin\theta)$		M1		M1 for correct factorisation	
	where $\theta = 2 \times 33.6^{\circ} = 67.2^{\circ}$ and $r = 6$ cm.					
	Area = $6^2 (\frac{67.2}{360} \pi - \frac{1}{2} \sin 67.2^\circ)$		A1		A1 for correct substitution of radius and a correct angle	
	$= 36(0.586 431 - \frac{1}{2}\sin 67.2^{\circ})$					
	= 36(0.586 431 – 0.460 931 6)					
	= 4.517 979 cm <sup>2</sup>		A1		A1 for correct answer to 2 or more sf	
	Area of overlap = $2 \times 4.517979 \text{ cm}^2$		M1		M1 for multiplying by 2	
	= 9.035 959 cm <sup>2</sup>	9.0 cm <sup>2</sup>	A1 M1		A1 for correct answer to either 1 or 2 sf M1 for use of mathematical language and diagrams to	
					support solution	
			9			

26 a		14 faces: the same as the number of polygons in the net.	B1 B1	2	B1 for the 14 faces B1 for clear explanation	М
b	Triangle 11 will move round to sit next to face 13, square 4 will move round to be next to face 12, leaving face 2 opposite to face 13.	13	B1		B1 for face 13	
С		I would create the shape first then draw what I see from above as the plan and from the side as the elevation. Once I have created the shape, I can measure the lengths and angles concerned.	B1 M1 B2		B1 for clear explanation M1 for use of diagrams to support the explanation B1 for an explanation of the plan B1 for explanation of elevation	
27	Circumference of wheel = $\pi D$ = $\pi \times 68$ = 213.6283 cm		7 M1 A1	2	M1 for method of calculating circumference of wheel A1 for full unrounded answer	M
	10 km = 10 × 1000 × 100 cm = 1 000 000 cm		B1		B1 for use of 1 000 000 as a conversion factor either way round	
	Number of revolutions in 10 km = 1 000 000 cm ÷ 213.6283 cm = 4681.028	4681 complete rotations	M1 A1		M1 for correct division with common units A1 for cao	
28	5 km C		81 M1	2	B1 for use of a correct diagram M1 for explanation of how and why using Pythagoras	M
	$x^{2} = 5^{2} + 3^{2}$ $x^{2} = 34$		M1 M1		M1 for correct application of Pythagoras' theorem M1 for correct method of finding hypotenuse	
	$x = \sqrt{34} \\ = 5.830 951 9$	x = 5.8  km	A1 <b>5</b>		A1 for correct rounding to 2 or 3 sf	

29			B1	2	B1 for clear correct diagram used	М
	62° 53°					
	Chimney					
	28° 37°					
	30 x					
	Let $c$ = the height of the chimney.		M1		M1 for correct use of trigonometry with $x$ , $c$ and angle 53° or 37°	
	$\frac{x}{c}$ = tan 53°		A1		A1 for correct equation having <i>x</i> as subject	
	$x = c \tan 53^{\circ}$					
	$\frac{(30+x)}{x} = \tan 62^{\circ}$		M1		M4 for correct upo of trigonometry with and angle	
	$c$ 30 + $x = c \tan 62^{\circ}$		IVII		M1 for correct use of trigonometry with $x$ , $c$ and angle 62° or 28°	
	$x = c \tan 62^\circ - 30$		A1		A1 for correct equation in format to combine with equation 1	
	Combining equations 1 and 2 to eliminate $x$ : $c \tan 53^\circ = c \tan 62^\circ - 30$		M1		M1 for correctly eliminating x	
	Rearrange to get $c$ on one side of the		IVII		With to correctly emininating x	
	equation. $30 = c \tan 62^\circ - c \tan 53^\circ$					
	$30 = c(\tan 62^\circ - \tan 53^\circ)$					
	$c = \frac{30}{\left(\tan 62^\circ - \tan 53^\circ\right)}$		M1		M1 for correct equation with $c$ as subject	
	= 54.182 761 m	54.2 m	A1		A1 for correct rounding to 2 or 3 sf	
			8			

20		<u> </u>	MO	1 0	MA for the second illustration become also found to A. J.D.	
30	30° A 330° S 40° A 120° A 15 B		M2	2	M1 for diagram illustrating how angles found at A and B M1 for complete triangle drawn, showing all relevant data	M
	Angle at A is $90^{\circ} + (360^{\circ} - 330^{\circ}) = 120^{\circ}$ Angle at B is $290^{\circ} - 270^{\circ} = 20^{\circ}$ Angle at S is $180^{\circ} - (120^{\circ} + 20^{\circ}) = 40^{\circ}$ Use the sine rule. $\frac{x}{\sin 20^{\circ}} = \frac{15}{\sin 40^{\circ}}$ $x = 15 \times \frac{\sin 20^{\circ}}{\sin 40^{\circ}}$		B1 B1 B1 M1		B1 for 120° B1 for 20° B1 for 40° M1 for use of sine rule	
	sin40° = 7.981 33	8.0 km	A1 <b>7</b>		A1 for correct answer rounded to 1, 2 or 3 sf	
31 a		Sometimes true.	B1	2	B1 for sometimes true	М
b		It is not true if the number of individual cubes has fewer than 3 factors, including 1 and itself, for example, you cannot do it with 7 cubes (factors 1 and 7) You can only make one cuboid if the number of factors, including 1 is equal to 3, for example, with 21 cubes (factors 1, 3 and 7).	B1 B1		B1 for clear explanation for when not true  B1 for clear explanation for when only 1 cuboid could be made	
С		You can make more than one cuboid if the number of cubes has more than 3 factors not including itself, for example, 30 (factors 1, 2, 3 and 5).	B1 B1 <b>5</b>		B1 for clear explanation for when more than 1 cuboid could be made B1 for use of examples to illustrate the explanations	

32 a		Yes.	B1 B1	2	B1 for yes B1 for a clear diagram or explanation	М
b		Yes.	B1 B1		B1 for yes B1 for a clear diagram or explanation	
С		Yes.	B1 B1		B1 for yes B1 for a clear diagram or explanation	
d		Yes.	B1 B1		B1 for yes B1 for a clear diagram or explanation	
33	Assume the cuboid has dimensions $x$ , $y$ and $t$ . The surface area = $2(xy + xt + yt)$ Volume = $xyt$ Doubling the lengths gives dimensions as $2x$ , $2y$ and $2t$ .	False.	B1 M1 M1 M1	2	B1 for false M1 for surface area with either specific lengths or a generalisation M1 for volume with either specific lengths or a generalisation M1 for showing correct follow through of double the lengths	М
	So surface area $= 2(2x \times 2y + 2x \times 2t + 2y \times 2t)$ $= 2(4xy + 4xt + 4yt)$ $= 8(xy + xt + yt)$ which is 4 times the first area. and $V = 2x \times 2y \times 2t$ $= 8xyt$		B1 B1 B1		B1 for a correct statement of SA with their data  B1 for 4 times area  B1 for a correct statement of volume with their data	
	which is 8 times the first volume.		B1 <b>8</b>		B1 for 8 times volume	

34			M1	2	M1 for clear diagram	М
	10					
	22.5 Consider just half the shape, where $x$ is the					
	length of the string. Use Pythagoras' theorem.		M1		M1 for correct Pythagoras statement	
	$x^2 = 10^2 + 22.5^2$ = 606.25		M1		M1 for correct method of applying Pythagoras' theorem	
	$x = \sqrt{606.25}$					
	= 24.622 145 Two lengths of string will be		A1		A1 for full answer	
	49.244 289 cm		A1		A1 for double the initial <i>x</i>	
	Subtract the original 45 cm Gives extension as 4.244 289	4.2 cm	A1		A1 for rounded answer to either 2 or 3 sf	
			6			
35	Let AC = x, the length of the new road. Use Pythagoras' theorem.		M1	2	M1 for use of a diagram to assist the explanation	М
	$x^2 = 4.9^2 + 6.3^2$ = 63.7		M1		M1 for clear statement of Pythagoras	
	$x = \sqrt{63.7}$		M1 A1		M1 for correctly applying Pythagoras' theorem A1 for full answer	
	= 7.981 228 Current distance = 4.9 + 6.3 = 11.2 km					
	Saving = 11.2 – 7.981 228		B1 M1		B1 for 11.2 M1 for subtracting lengths	
	= 3.218 772 km	3.22 km	A1 <b>7</b>		A1 for correct rounding to 2 or 3 sf	
36		Vac a size 12 52.429	B1	2	B1 for yes	М
		Yes. $\theta = \sin^{-1} \frac{12}{15} = 53.13^{\circ}$ = 53° to the nearest degree				
		= 50° to 1 sf	M1		M1 for showing that using trigonometry and rounding can give 50°	
		12 cm has range of 11.5 to 12.5 cm 15 cm has range of 14.5 to 15.5 cm	M1		M1 for showing the ranges of lengths of the sides	
		The smallest value for $\sin \theta$ is $\frac{11.5}{15.5}$			wit for showing the ranges of lengths of the sides	
		which gives $\theta = \sin^{-1} 0.7419$				
		$\theta$ = 47.9° So there are values that round to 12 cm	B1		B1 for showing the least possible value of the angle	
		and 15 cm which will give an angle that rounds to 50°.	B1		given the ranges B1 for final summary explaining that it is possible	
]			5		Drift iniai summary explaining that it is possible	

37		Use Pythagoras' theorem. $AC^2 = 4^2 - (2\sqrt{2})^2$ $= 16 - 8 = 8$ $BC^2 = 8 = (2\sqrt{2})^2$ $= 8$ Hence BC = AC, an isosceles triangle.	M1 A1 M1 A1 A1 5	2	M1 for correct Pythagoras statement A1 for correct value of AC <sup>2</sup> M1 for finding BC <sup>2</sup> A1 for correct value of BC <sup>2</sup> A1 for clear explanation of sides being the same length	M
38	$AB^{2} = 2^{2} - 1^{2}$ $= 4 - 1 = 3$ $AB = \sqrt{3}$	$\sqrt{3}$ cm	M1 A1 M1	2	M1 for correct Pythagoras statement A1 for 3 M1 for a clear communication of the method used	М
39	cos 68° = -cos 112° = -cos 248° = 0.3746 cos 338° = 0.9271	cos 338° is the odd one out. All the others have the same numerical value (ignoring signs).	B1 B1	2	B1 for cos 338° B1 for a clear explanation	М
40 ai	$\sin x + 1 = 2$ $\sin x = 1$ $x = \sin^{-1} 1 = 90^{\circ}$	x = 90°	M1 A1	2	M1 for $\sin x = 1$ A1 for 90°	М
ii b	2 + 3cos $x = 1$ 3cos $x = 1 - 2 = -1$ $\cos x = -\frac{1}{3}$ $x = 109.5^{\circ}$ and 360° - 109.5° = 250.5°	x = 109.5°, 250.5°	M1 A1 A1 A1 M1		M1 for first step of solving equation A1 for correct statement of cos <i>x</i> A1 for correct angle to 1 dp A1 for correct angle to 1dp M1 for method of getting to sin <sup>-1</sup>	
	cos 320° = 0.766 044 4 sin <sup>-1</sup> 0.766 044 4 = 50° and 180° – 50° = 130°	$x = 50^{\circ}$ and 130°	A1 A1 <b>9</b>		A1 for 50° A1 for 130°	

41 a	$\tan x = \sin x \div \cos x$		M1	2	M1 for communicating effectively how the sine and cos	М
b	$\frac{\sqrt{8}}{4} \div \frac{3}{\sqrt{18}}$ $= \frac{\sqrt{8}}{4} \cdot \frac{\sqrt{18}}{3}$ $= \frac{\sqrt{144}}{3}$		M1 M1 A1	2	can be used to find tan (This could be $\tan x = \frac{\sin x}{\cos x}$ )  M1 for correct use of tan A1 for correct combination of surds	IVI
	$12$ $= \frac{12}{12} = 1$ $\tan^{-1} 1 = 45^{\circ}$ Alternatively, use Pythagoras' theorem to work out the length of the third side, e.g. (side) <sup>2</sup> = 16 - 8 = 8 $\sin \theta = \sqrt{8}$	$\tan x = 1$	A1		A1 for $\tan x = 1$	
	side = $\sqrt{8}$ $\tan x = \frac{\sqrt{8}}{\sqrt{8}} = 1$ $\tan^{-1} 1 = 45^{\circ}$	45°	M1 A1 <b>6</b>		M1 for use of inverse tan or recognising an isosceles triangle A1 for 45°	
42		Using Pythagoras' theorem, the hypotenuse = $\sqrt{6+10} = \sqrt{16} = 4$	M1 A1	2	M1 for correct Pythagoras statement A1 for 4	М
		Then $\sin x = \frac{\sqrt{6}}{4}$	B1		B1 for correct sin x	
		and $\cos x = \frac{\sqrt{10}}{4}$	B1		B1 for correct cos x	
		Hence $(\sin x)^2 + (\cos x)^2 =$ $\frac{6}{16} + \frac{10}{16} = \frac{16}{16} = 1$	A1		A1 for correct explanation	
			5			

43	A  3  C $60^{\circ}$ B  Use the cosine rule. $c^2 = a^2 + b^2 - 2ab \cos C$ $= 9 + 16 - 2 \times 3 \times 4 \times \cos 60^{\circ}$ $= 25 - 24 \times \frac{1}{2}$ $= 13$		M1 M1 A1 B1	2	M1 for clear use of diagram  M1 for correct cosine rule statement A1 for correct substitution B1 for $\cos 60^\circ = \frac{1}{2}$	М
	$c = \sqrt{13}$	√13 cm	A1 6		M1 for taking square root A1 for correct surd form	
44	B	$\binom{6}{2}$	B1 B1	2	B1 for correct diagram B1 for correct vector	М
45		No. To work out the return vector, multiply each component by $-1$ .  The return vector is $\begin{pmatrix} 3 \\ -2 \end{pmatrix}$ .	B1 B1 B1 3	2	B1 for No  B1 for correct vector B1 for a clear explanation of what Joel should have done	M

46 a	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\		M2 A1	2	M1 for showing construction of 60° M1 for showing bisection of 60° A1 for showing bisection of 30° to show 15°	Н
b	75°		M2 A1		M1 for showing construction of 90° M1 for showing construction of 60° to leave a 30° angle A1 for bisecting that 30° angle to leave 75°	
47		Each angle bisector is the locus of points equidistant from the two arms or sides of the angle.  Hence, where they all meet will be the only point that is equidistant from each of the three sides.	M2	2	M1 for explanation referring to the bisector being equidistant  M1 for the interpretation of the intersections	Н
		Hence a circle can be drawn inside the triangle, with this centre, that just touches each side of the triangle.	A1 3		A1 for the use of a diagram to help interpret the explanation	

48 a-d	A E A Z	M1 A1 M1 A1 A1 M1 A1	2	M1 for method of constructing any midpoint A1 for all three midpoints correct and labelled  M1 for constructing any perpendicular from a vertex to opposite face A1 for all three correct A1 all 3 feet correctly labelled M1 for constructing a midpoint of AO or BO or CO A1 for all midpoints correct and labelled	Н
e	D D D M M A Z	M1 A1		M1 for constructing a bisector of LM or LN or MN A1 for all three bisectors correct and point of intersection labelled P	
f	A circle, centre P, should pass through each of the nine labelled points.	A1		A1 for correct explanation	
49	AB = CD (given) $\angle ABD = \angle CDB \text{ (alternate angles)}$ $\angle BAC = \angle DCA \text{ (alternate angles)}$ so $\triangle ABX \equiv \triangle CDX \text{ (ASA)}$	B3 B1 4	2	B1 for correct statement with justification B1 for correct statement with justification B1 for correct statement with justification B1 for stating ASA within correct explanation	Н
50	AB and PQ are the corresponding sides opposite the 50° angle but they are not equal in length.	B2 <b>2</b>	2	B1 for stating the corresponding side link B1 for complete clear statement	Н

51 a		Joining adjacent midpoints forms a right-angled isosceles triangle, with the perpendicular sides each half the length of the side of the square. All four triangles are congruent. At each midpoint, there are two angles of 45°, leaving the vertex of the new shape being 90°. Since all the sides are equal and all the angles are 90°< the new shape is a square.	B2 M1	2	B1 for explaining all sides are the same length B1 for explaining how all angles are 90°  M1 for communicating a given original side length and finding the length of a side of the inscribed square	Н
b	Area of original rectangle = $x^2$ If the length of the side of the inscribed square is $h$ , then: $h^2 = \left(\frac{x}{2}\right)^2 + \left(\frac{x}{2}\right)^2$		M1 A1		M1 for correctly using Pythagoras' theorem to find the length of the side of the new square  A1 for correct expression of $h^2$	
	$h^{2} = \frac{2x^{2}}{4}$ $h^{2} = \frac{x^{2}}{2}$ Area of inscribed square is $h^{2}$	The area of the inscribed square is half the area of the original square.	A1 A1 <b>7</b>		A1 for correctly stating area A1 for clear communication of complete solution	
52	$=\frac{x^2}{2}$	Each internal angle of an octagon is 135°. Each internal angle of a hexagon is 120°. The sum of these two angles is 255°. The sum of the angles in a quadrilateral	B2 B1	2	B1 for explanation of 135° B1 for explanation of 120° B1 for 255°	Н
		is 360° so the sum of the remaining angles is: 360° – 255° = 105°.  The two remaining angles are equal, as the line joining through the vertices C, J, G and L (and thus through the obtuse angles) is a line of symmetry.	M1 A1 B2		M1 for subtraction from 360° A1 for 105° B1 for explaining two angles are equal B1 for clear reasons given as to why	
		JFG = 52.5°	B1 <b>8</b>		B1 for correct 52.5°	

53	Use the sine rule in both triangles.	M1	2	M1 for use of sine rule	Н
	$\frac{\sin P}{b} = \frac{\sin C}{p}$	A1		A1 for correct equation	
	$\frac{\sin A}{a} = \frac{\sin C}{c}$	A1		A1 for correct equation	
	$\sin A = \frac{a \sin C}{c}$				
	As $A = P$ , then $\sin P = \sin A$	M1		M1 for equating both known angles	
	So $\frac{b\sin c}{p} = \frac{a\sin C}{c}$				
	Hence $\frac{b}{p} = \frac{a}{c}$	B1		B1 for correct statement linking $p$ , $a$ , $b$ and $c$	
	Hence $\frac{p}{b} = \frac{c}{a}$	A1		A1 for clear communication of the full solution	
	So $p = \frac{bc}{a}$				
		6			

54	Use Pythagoras' theorem to write expressions for $z^2$ .		2		Н
	Triangle ABC: $z^2 = r^2 + (s + y)^2$				
	Triangle ABD: $z^2 = w^2 + (x + t)^2$				
	So $r^2 + (s + y)^2 = w^2 + (x + t)^2$	M1		M1 for combining expressions	
	Now $r^2 = x^2 - s^2$				
	and $w^2 = y^2 - t^2$				
	Substitute for $r^2$ and $w^2$ in the equation:				
	$x^2 - s^2 + (s + y)^2 = y^2 - t^2 + (x + t)^2$	M1		M1 for substitution	
	Multiply out the brackets:				
	$x^{2} - s^{2} + s^{2} + 2sy + y^{2}$ $= y^{2} - t^{2} + x^{2} + 2xt + t^{2}$	M1		M1 for multiplying out to get individual terms	
	$= y^2 - t^2 + x^2 + 2xt + t^2$ Simplify:	IVII		Wit for multiplying out to get individual terms	
	$x^2 + 2sy + y^2 = y^2 + x^2 + 2xt$	M1		M1 for simplifying	
	2sy = 2xt			With the camping	
	sy = xt				
	Alternatively:				
	Assume T is the intersection of AD and				
	BC. ACT is similar to BDT as both	B1		B1 for clear explanation	
	contain the same angles. (Angles ATC				
	and BTD are vertically opposite and so				
	are equal.)				
	Hence by similarity $\frac{x}{y} = \frac{s}{t}$	B1		B1 for $\frac{x}{}=\frac{s}{}$	
	, in the second	-		y t	
	So $xt = sy$	B1		B1 for clear communication of proof	
		7			

55 a	SC SC	ake the smallest two sides, quare each of them, add the quares together then find the quare root of the sum.	M1	2	M1 for correct Pythagoras statement	Н
	th	this root is equal to the length of ne longest side, then the triangle s right angled.	B1		B1 for clear explanation	
	of	the root is smaller than the length of the longest side, then the angle of greater than 90°.	B1		B1 for clear explanation	
	of	the root is larger than the length of the longest side then there is no ongle greater than 90°.	B1		B1 for clear explanation	
b	is	the first triangle the hypotenuse is $\sqrt{5^2 + 12^2} = \sqrt{139} = 13$	B1		B1 for 13	
	hy	the second triangle, the spotenuse is 12 with the unknown ide $\sqrt{12^2 - 5^2} = \sqrt{119}$ , which is				
		etween 10 and 11 cm.	B1		B1 for side length between 10 and 11 or more accurate.	
		So they both have a short side of cm.	B1		B1 for explanation of what is the same	
	si	But the lengths of the other short ide and the hypotenuse are lifferent.	B1		B1 for clear explanation of what is different	
	- Carl	inicioni.	8			
56	A 3 M		M1	3	M1 for clear diagram	Н
	(n	the top triangle ABM: $m + t + n)^2 = (2x)^2 + x^2 = 5x^2$	M1 A1		M1 for using a large triangle to identify parts A1 for correct equation	
	Si P	So $m + t + n = x\sqrt{5}$ Putting together shape P and Q:	M1 A1		M1 for method of adding P and Q	

area = (m+n)t		A1 for $(m+n)t$	
So the area, $A$ , of the whole shape is: top triangle ABM + bottom triangle DCN + $(P + Q) + t^2$	M1	M1 for adding all separate components	
Area of ABM = $\frac{1}{2} \times 2x \times x = x^2$ Area of DCN = $\frac{1}{2} \times 2x \times x = x^2$ So total area = $x^2 + x^2 + (m+n)t + t^2$ = $2x^2 + t(m+n+t)$ But $m + n + t = x\sqrt{5}$	A1 M1	A1 for correct statement of $A$ M1 for substituting $(m + n + t)$	
So $A = 2x^2 + tx\sqrt{5}$ But the sides are of length $2x$ , so $A = 4x^2$ Then $2x^2 + tx\sqrt{5} = 4x^2$	B1 M1	B1 for whole area $4x^2$ M1 for equating the two equations	
and $tx^{\sqrt{5}} = 2x^2$ $t\sqrt{5} = 2x$ Squaring each side gives: $5t^2 = 4x^2$	A1 M1	A1 for equation enabling <i>t</i> to be identified M1 for squaring A1 for correct expression for <i>t</i> <sup>2</sup>	
$t^2 = \frac{4x^2}{5}$ Whole area $A = 4x^2$	A1 A1	A1 for clear explanation showing $\frac{1}{5}$ idea	
Hence the middle square, $t^2$ , is $\frac{1}{5}$ of $A$ .	A1 15	A1 for complete clear solution	

	T	T		1		
57 a		Not true. For example these are both right-angled triangles but their sides are not in proportion.	B1 B1	2	B1 for not true B1 for clear explanation with an example drawn to illustrate	Н
b		True. With an enlargement the final shape will be in the same <i>proportion</i> as the original so it will be similar.	B1 B1		B1 for true B1 for clear explanation	
С		True. All circles are in proportion to each other and so will be similar.	B1 B1		B1 for true B1 for clear explanation	
58 a		Any two regular polygons with the same number of sides will have the same angles so the ratio of lengths of the sides will be the same. This means the shapes will be similar.	B1 B1	2	B1 for clear example B1 for use of diagrams to support the explanation	Н
b		A B B B C D D D As the corresponding sides of triangle A and triangle B are the same, the two triangles are congruent, SSS. Therefore equivalent angles are the same. This demonstrates the corresponding angles between parallel lines are the same.	B1 B1		B1 for clear explanation B1 for use of diagram to clarify explanation	
		between parallel lilles are the same.	4			

59 a	7 + 6 - 6 - 5 - 4 - 3 - 2 - 1 0 1 2 3 4 5 * * * * * * * * * * * * * * * * * *	B1	2	B1 for accurate image B drawn	Н
b	-9 -8 -7 -8 -3 -4 -3 -2 -1 1	B2		B1 for enlargement of scale factor –2 B1 for correct enlargement to image C	
С	-6- -7-	B2		B1 for enlargement scale factor $-\frac{1}{2}$ B1 for centre of enlargement (-6, 2)	
	Enlargement with scale factor $-\frac{1}{2}$ about				
	(-6, 2).				
		5			
60	Enlargement with sf –3 about (1, 2). Drawing lines from the two vertices at the base of triangle A to their image points in B. The intersection shows the centre of enlargement. The base of A is 2 squares wide, the base of B is 6 squares wide, and 6 is 3	B1 B1 B1	2	B1 for correct statement  B1 for explanation of how centre of enlargement is found B1 for explanation how sf is found	Н
	times 2, so the sf is 3.	3			

61 a	Examine the four possible starting points for the stamp. These are at the top right and bottom left of each side, allowing for 180° rotation of each side. Four rotations mean that each of these points is covered once.	B1	2	B1 for clear explanation	Н
b	No, the machine would not detect the stamp placed on the top left-hand corner because none of the rotations will put the stamp in the top right-hand corner.	B1		B1 for No	
С	Four corners on each side could possibly be the 'top right'.	B1		B1 for clear explanation	
d	One way is to rotate about H and then rotate about one of the diagonals (call it	B1		B1 for clear explanation	
	D). Keep repeating the sequence H, D, H, D, to check all eight corners.	4			
62	A B		2		Н
	The hypotenuses (OA and OB) are the same, as each is a radius of the circle. OM is common to both triangles. OMA and OMB are both right angles. Triangles OAM and OBM are congruent, therefore AM = MB. Therefore, M is the midpoint of AB and the chord has been bisected, as	B4 B2		B1 for hypotenuse same B1 for OM common B1 for right angles B1 for congruency B1 for clear explanation and good use of mathematical language. B1 for use of diagram to support proof	
	required.	6			

63	Circle Theorem 1 states that the angle at the centre of a circle is twice the angle at the circumference when they are both subtended by the same arc.	M2	2	M1 for stating Theorem 1 M1 for extending this to this proof	Н
	Theorem 1 tells you that any angle subtended from arc AB at a point C on the circumference is always half the angle subtended from arc AB at the	A1		A1 for clear overall explanation and clarity	
	centre.	B1		B1 for use of diagram and mathematical language	
	$C_3$ $X$ $C_4$ $X$				
	Therefore, every possible angle subtended from arc AB at the circumference will correspond to the same angle at the centre.	4			

64		A	M1	2	M1 for clear use of diagram	Н
		Draw triangle BCP, where P is on the circumference in the opposite segment . Then angle BPC is $180^{\circ} - x$ as BAC and BPC are opposite angles in a cyclic quadrilateral. Angle BOC is double BPC, which is $360^{\circ} - 2x$ . Angle BCO will also be $y$ , as BCO is an isosceles triangle. Angles in triangle OBC sum to $180^{\circ}$ , so $2y + 360^{\circ} - 2x = 180^{\circ}$ and $2y = 2x - 180^{\circ}$ Divide both sides by 2 to give: $y = x - 90^{\circ}$ .	M1 A1 B1 M1 A1 A1 A1 A1 A1		M1 for using point P A1 for 180 – x  A1 for identifying 360° – 2x B1 for identifying BCO  M1 for adding known angles together A1 for simplifying A1 for a clear, well presented solution	
65	As ABCD is a cyclic quadrilateral, the opposite angles will sum to $180^{\circ}$ . So $2x - 5^{\circ} + 5y - 20^{\circ} = 180^{\circ}$ . $2x + 5y = 205^{\circ}$ (1) And $3y + 5 + 2x + 20^{\circ} = 180^{\circ}$ . $2x + 3y = 155^{\circ}$ (2) Subtract (2) from (1): $2y = 50^{\circ}$ . $y = 25^{\circ}$ Substitute $y$ into (2): $2x + 75^{\circ} = 155^{\circ}$ . $2x = 80^{\circ}$ . $x = 40^{\circ}$ .	$y = 25^{\circ}$ $x = 40^{\circ}$	M1 M1 A1 A1 M1 A1 M1	2	M1 for explanation of cyclic quadrilateral M1 for adding opposite angles A1 for first correct equation A1 for second correct equation M1 for method of eliminating one variable A1 for 25° M1 for method of substitution A1 for 40°	Н

66	A 3 B 3 Y Z Z		B1	3	B1 for good clear diagram showing perpendiculars to Y and Z  B1 for clear diagram of ABT	Н
	Drop perpendiculars down to Y and X and complete the trapezium, with the top triangle being ABT, as shown. Length TB will be the same as YZ. Use Pythagoras' theorem on triangle ABT. $TB^2 = 9^2 - 3^2 = 81 - 9 = 72$ $TB = \sqrt{72} = 8.485 281 4$	8.49 cm	M1 A1 A1		B1 for clear explanation of how the triangle ABT has been formed  M1 for use of Pythagoras' theorem A1 for correct statement  A1 for correct answer to 2 or 3 sf	
67	Circle Theorem 1 states The angle at the centre of a circle is twice the angle at the circumference when they are both subtended by the same arc. Theorem 1 tells you that any angle subtended from arc AB at a point C on the circumference is always half the angle subtended from arc AB at the centre.		P2 C1	3	P1 for stating Theorem 1 P1 for extending this to this proof C1 for clear overall explanation and clarity  C1 for use of diagram and mathematical language.	Н
	Therefore, every possible angle subtended from arc AB at the circumference will correspond to the same angle at the centre.  Hence angles subtended at the circumference are equal.		4			

68 a	The angle PQS is the same as PRS, $3x$ , as they are angles in the same quadrant		M1	2	M1 for clear explanation	Н
	(subtended by the same arc). The angle sum of triangle PQT is 180°. Hence $2x + 3x + 5x = 180^{\circ}$		M1		M1 for using angles in a triangle	
b	$10x = 180^{\circ}$ $x = 18^{\circ}$	<i>x</i> = 18	A1		A1 for 18	
	Complete the diagram with all the known					
	angles.		B1		B1 for clear use of a diagram marked with all the angles	
	54° 18° P					
	72° K		B1		B1 for clear explanation	
	36° 36° 18° 72°		B1		B1 for finding all the angles and showing them clearly	
	P s					
	You can now see that: angle $P = 54^\circ$ , angle					
	$Q = 72^{\circ}$ , angle $R = 126^{\circ}$ , angle $S = 108^{\circ}$ and angle $STP = 90^{\circ}$ .		B1		B1 for clear explanation of the number sequence found	
	The numbers 54, 72, 90, 108 and 126 form a sequence with a difference of 18.		7			

69	1.2 m 40 cm		3		Н
	As it is shown in the diagram, the proportion of the height of the container	M1		M1 for method of finding proportion of height	
	that is filled is $\frac{80}{120} = \frac{2}{3}$ . The current volume of water is $90 \times 40 \times 80 = 288\ 000\ \text{cm}^3$ .	A1 B1		A1 for $\frac{2}{3}$ B1 for 288 000	
	Assume you move the container so that the base is $40 \times 120$ . The volume of water must stay the same and take its height as $C$ cm. Then: $40 \times 120 \times C = 288000$ so $4800 \times C = 288000$ $C = 60$ Comparing this with the height, 90 cm: $60  2$	A2		A1 for clear explanation of changing to a different base A1 for structure and clarity of explanation	
	$\frac{60}{90} = \frac{2}{3}$ Now assume you move the container so the base is $90 \times 120$ then $90 \times 120 \times C = 288000$ $10800C = 288000$ $C = \frac{80}{3}$ Comparing this with the height, $40 \text{ cm}$ : $\frac{80/3}{40} = \frac{80}{3 \times 40} = \frac{80}{120} = \frac{2}{3}$ So the proportion of the height of the	B2		B1 for clear explanation of changing to a different base B1 for structure and clarity of explanation	
	container that is filled with water remains constant.	A1 <b>8</b>		A1 for clear explanation	

70 a		The end face or cross-section of a right prism is a polygon and is perpendicular to the vertical sides all through its length. The end faces (polygons) are the same shape and size. The volume is equal to the area of cross-section x the height of the prism. So if you know the height and the volume you know the area of the cross-section but not the dimensions or the shape of the base of the prism.	В3	2	B1 for perpendicular sides B1 for same base as top B1 for statement about base area	Н
b	Assume the sides all have integer values. The formula for the volume of the prism will be: $a \times b \times 10 = 160 \text{ cm}^3$	Only 1	B1		B1 for answer 1	
	but if the base is a square, then $a = b$ . $a^2 = 16 \text{ cm}^3$ This has only one solution: $a = 4$ .	4 × 4 × 10	B1 B1 <b>6</b>		B1 for identifying the 4 × 4 × 10  B1 for clarity and detail of explanation	
71 a		The formula for the circumference of circle is $2\pi r$ . This is just a length, $r$ , multiplied by a number, so the answer will still be a length.  The formula for the area of a circle is $\pi r^2$ . This is a number multiplied by a length squared so this will be an area.	B2	2	B1 for explanation about circumference B1 for explanation about area	Н
b		A formula for a surface area will include the product of two lengths, but a formula for a volume will include the product of three lengths.	B1		B1 for clear of explanation	
С		$\frac{1}{3}b^2h$ includes the produce of three lengths, $b \times b \times h$ and so must be the volume. $4\pi r^2$ includes the product of two lengths, $r \times r$ , and so must be the area.	B1 B1 B1		B1 for clear explanation B1 for clear explanation B1 for demonstrating an understanding of how to help other people to understand this concept.	

	T		1		1
72	Identify the third arrangement.		2		H
	The single row of 8 cubes shows the	B1		B1 for volume being 8 cubes	
	cuboid must have a volume of 8 cubes.				
	The missing arrangement is a $1 \times 2 \times 4$	B1		B1 for missing dimensions	
	cuboid.			3	
		M1		M1 for clearly showing how to find the missing	
		1411		arrangement	
				arrangement	
	Find the amount of string for each of the				
	arrangements.				
	For the cuboid above, $1 \times 2 \times 4$ :				
	$L = 4 \times 15$ , $W = 2 \times 15$ , $H = 1 \times 15$ and	M1		M1 for correct method of using formula	
	$S = 2 \times 60 + 2 \times 30 + 4 \times 15 + 20$				
	= 260 cm	A1		A1 for 260	
	For the 1 × 1 × 8 cuboid:				
	$L = 8 \times 15$ , $W = 1 \times 15$ , $H = 1 \times 15$ and				
	$S = 2 \times 120 + 2 \times 15 + 4 \times 15 + 20$				
	= 350 cm	A1		A1 for 350	
	= 350 cm				
	For the 2 2 2 subside				
	For the $2 \times 2 \times 2$ cuboid:				
	$L = 2 \times 15, W = 2 \times 15, H = 2 \times 15 \text{ and}$				
	$S = 2 \times 30 + 2 \times 30 + 4 \times 30 + 20$	۸.4		A4 for 260	
	= 260 cm	A1		A1 for 260	
	So the least amount of string is used in	B1		B1 for identifying which uses least string	
	the $1 \times 2 \times 4$ and the $2 \times 2 \times 2$	A1		A1 for clear complete solution.	
	arrangements.				
		9			
1					1

73	Surface area of end = 1000 ÷ 20 = 50 cm <sup>2</sup>	B1	3	B1 for 50	Н
	Consider a cuboid with a square end. Side length of square = $\sqrt{50}$ = 7.0711 Surface area (SA) = 50 + 50 + 4 × 7.0711 × 20 = 665.6 cm <sup>2</sup> Consider a triangular prism with a triangular end.	B1 B1		B1 for 7.07 any rounding B1 for 665.6 any rounding 2sf or more	
	Area of triangular end = $\frac{1}{4}\sqrt{3}a^2 = 50$	M1		M1 for use of given formula	
	So $a^2 = \frac{200}{\sqrt{3}} = 115.470\ 054$			A47, 40.75	
	<i>a</i> = 10.745 70 cm	A1		A1 for 10.75 any rounding 2sf or more	
	$SA = 50 + 50 + 3 \times 10.745 \ 70 \times 20$ $= 745 \ cm^2$ Consider a cylinder with a circular end.	A1		A1 for 745 any rounding 2sf or more	
	Then $\pi r^2 = 50$ $r = \sqrt{\frac{50}{\pi}} = 3.989 42$	M1		M1 for use of formula	
	$\sqrt{\pi}$ SA = 50 + 50 + $\pi$ × 2 × 3.989 42 × 20	A1		A1 for correct answer to any rounding	
	$SA = 50 + 50 + \pi \times 2 \times 3.969 42 \times 20$ = 601.4 cm <sup>2</sup>	A1		A1 for 601.4 any rounding	
	Differences between the three surface areas:	B1		B1 for clear explanation	
	<ul> <li>surface area of the triangular prism is 79.4 cm<sup>2</sup> larger than the cuboid and 143.6 cm<sup>2</sup> larger than the cylinder</li> </ul>	B1		B1 for clear explanation	
	<ul> <li>surface area of cuboid is 64.2 cm<sup>2</sup> larger than the cylinder.</li> </ul>	B1		B1 for clear explanation	
	The larger the surface area, the more packaging material is required therefore the higher the production	B1		B1 for a clear complete solution	
	costs.	13			

74	Use the cosine rule. $AB^2 = 2.1^2 + 1.8^2 - 2 \times 2.1 \times 1.8 \times \cos 70^\circ$ = 5.064 328 $AB = \sqrt{5.06} = 2.250 406$ Extra distance = $(2.1 + 1.8) - 2.25$ km	1.65 km	M1 A1 A1 A1	3	M1 for use of cosine rule A1 for correct substitution into cosine rule A1 for 5.06 rounded to 3 or more sf A1 for 2.25 rounded to 2 or 3 sf A1 1.65 rounded to 2 or 3 sf	Н
75	X Y 3 km 2 km		<b>5</b>	3	M1 for clear diagram showing all data	Н
	Use Pythagoras' theorem to find BY.  BY = $\sqrt{9+4}$ = 3.605 551 3  Use the right-angled triangle XYB to find XY. $\frac{XY}{BY} = \tan 6^{\circ}$ XY = BY × tan 6° $\frac{370.050.7}{100}$		M1 A1 M1		M1 for use of Pythagoras' theorem  A1 for BY unrounded  M1 for use of tangent	
	= 0.378 958 7 km = 378.9587 m	379 m	A1 A1 6		A1 for XY unrounded A1 for 379 in metres and rounded to 2 or 3 sf	
76 a	8 P R		M1	3	M1 for use of clear diagram	Н
b	$PM = \sqrt{8^2 + 4^2} = \sqrt{80}$ $PM = 8.944 \ 271 \ 9 \ cm$	8.9 cm	M1 A1 M1		M1 for use of Pythagoras' theorem A1 for 8.9 rounded to 2 or 3 sf M1 for clear diagram	

С	$Q = \frac{10}{4 \text{ M}} = \frac{10}{10^2 + 4^2} = \sqrt{116}$ $VM = \sqrt{10^2 + 4^2} = \sqrt{116}$ $VM = 10.770 33$	10.8 cm	M1 A1 M1		M1 for use of Pythagoras' theorem A1 for 10.8 rounded to 2 or 3 sf M1 for use of clear diagram	
d	P T $\cos P = \frac{\frac{1}{2}\sqrt{80}}{\sqrt{116}}$ = 0.415 227 4  Angle VPM = 65.466 362°  Vertical height of V above face PRQ is given by VT in diagram above.	65.5°	M1 A1 A1 M1		M1 for use of correct cosine  A1 for 65.5 rounded to 2 or 3 sf  A1 for explanation of how the height is to be found  M1 for use of Pythagoras' theorem	
	VT = $\sqrt{\text{VM}^2 + \left(\frac{1}{2}\text{PM}\right)^2} = \sqrt{116 + \frac{1}{4} \cdot 80}$ = $\sqrt{136}$ = 11.661 904 Add the 15 cm of the base to give 26.661 904 cm.	26.7 cm	A1 A1 13		A1 for 11.619 04 and any rounding 3 or more sf A1 for 26.7 rounded to 2 or 3 sf	
77	He needs to find half of AC (not AC) to make a right-angled triangle. i.e. $\cos x = \frac{1}{2} \sqrt{208} = 0.721 \ 110$ $= \cos^{-1} 0.721 \ 110$		B1 M1	2	B1 for clear explanation  M1 for correct cosine method	Н
	= cos <sup>-1</sup> 0.721 110 = 43.853 779°	43.9	A1 3		A1 for 43.9 rounded to either 2 or 3 sf	

78	d e c		3		Н
	A $32^{\circ}$ B $C$ Using angles on a straight line.				
	$\theta$ = 180° – 58° = 122° Angle ADB = $\alpha$ = 180° – (32° + 122°)	M1		M1 for method for finding angle ABD	
	$= 180^{\circ} - 154^{\circ} = 26^{\circ}$ Use the sine rule.	B1		B1 for 26°	
	$\frac{e}{\sin 32^\circ} = \frac{28}{\sin 26^\circ}$	M1		M1 for use of sine rule	
	$e = \sin 32^{\circ} \times \frac{28}{\sin 26^{\circ}}$ $e = \sin 32^{\circ} \times 63.8728169$ = 63.847436	B1		B1 for $e$ and any rounding	
	c 58°				
	B C Using trigonometry:	M1		M1 for correct use of trigonometry	
	$\sin 58^{\circ} = \frac{c}{}$				
	$c = e \sin 58^{\circ}$ = 28.704 253 7	M1		M1 for correct expression for c	
	So the height of the tower is 29 m to the nearest metre.	A1 A1		A1 for 29 answer rounded to 2 or 3 sf A1 for complete accurate solution well laid out.	
		•			

79	$\sin 24^\circ = \frac{t}{}$			3		Н
	$\sin 24^\circ = \frac{t}{4.7}$					
	H 128° e		M1		M1 for a clear diagram with all relevant lengths and angles marked	
	$\frac{d}{180 - 128}$ $s = 52^{\circ}$ B					
	8.6 m 4.7 m 66° 90 – 66 = 24°					
	$y$ C $x$ $t = 4.7 \sin 24^\circ$				MA for mostly and of finality and	
			M1 A1		M1 for method of finding <i>t</i> A1 for correct expression of <i>t</i>	
	$\cos 24^\circ = \frac{x}{4.7}$		M1		M1 for method of finding <i>x</i>	
	$x = 4.7 \cos 24^{\circ}$		A1		A1 for correct expression of x	
	$\sin 52^\circ = \frac{y}{8.6}$		M1		M1 for method of finding y	
			A1		A1 for correct expression of <i>y</i>	
	$y = 8.6 \sin 52^{\circ}$				M. C	
	$\cos 52^\circ = \frac{s}{8.6}$		M1		M1 for method of finding s	
	s = 8.6 cos 52°		A1		A1 for correct expression of s	
	$e = x + y = 4.7\cos 24^{\circ} + 8.6\sin 52^{\circ}$		M1		M1 for method of finding <i>e</i>	
	= 11.070 556 km		A1		A1 for correct e, rounded to 4 or more sf	
	$f = s - t = 8.6 \cos 52^{\circ} - 4.7 \sin 24^{\circ}$		M1		M1 for method of finding <i>f</i>	
	= 3.383 0264 km		A1		A1 for correct <i>f</i> rounded to 4 or more sf	
		Use Pythagoras' theorem to find $d$ . $d = \sqrt{e^2 + f^2}$	M1		M1 for using Pythagoras' theorem	
		· ·				
		$= \sqrt{134.002}$ = 11.575 93 km	A1		A1 for correct d any value 3 sf or more	
		= 11.575 93 km = 11.6 km	A1		A1 for correct d rounded to 3sf	
		Use trigonometry to find $\beta$ .				
		$\tan \beta = \frac{e}{f} = \frac{11.070556}{3.3830264}$	M1		M1 for method of finding $\beta$	
		= 3.272382				
		$\beta = \tan^{-1} 3.272 \ 382 = 73.007 \ 489^{\circ}$ The required bearing = $360^{\circ} - \beta$	A1		A1 for $\beta$ to 4 or more sf	

		= 286.992 510 8° = 287°	A1 A1		A1 for final three-figure bearing A1 for effective use of diagrams and good use of mathematical language	
80	Use the sine rule to work out angle B.		<b>20</b> M1	3	M1 for use of sine rule	Н
	$\frac{\sin B}{10} = \frac{\sin 32^{\circ}}{6}$ $\sin B = \frac{10\sin 32^{\circ}}{6}$					
	$B = \sin^{-1} \frac{10\sin 32^{\circ}}{6} = 62^{\circ}$		A1		A1 for 62°, accept any rounding to 2sf or more	
	But we know ABC is obtuse, so: $B = 180^{\circ} - 62^{\circ} = 118^{\circ}$ Then $C = 180^{\circ} - (118^{\circ} + 32^{\circ}) = 30^{\circ}$ Use the sine area rule.		A1 B1		A1 for 118° and any rounding to 3sf or more B1 for 30° with any rounding to 2sf or more	
	Area = $\frac{1}{2}ab\sin C$		M1		M1 for use of area sine rule	
	= $\frac{1}{2}$ × 10 × 6 × sin 30° = 15 cm <sup>2</sup>	15 cm <sup>2</sup>	M1 A1 A1		M1 for correct substitution A1 for 15 rounded to 2 or 3 sf A1 for a complete solution clearly set out with correct mathematical language and symbols	
81 a	20 m		<b>8</b> M1	3	M1 for use of clear diagram	Н
	A 23 m					
	B 24 m C Use Pythagoras' theorem to work out <i>H</i> .		M1		M1 for use of Pythagoras' theorem	
	$H = \sqrt{10^2 + 24^2}$		A1		A1 for 26 cao	
	= 26 Use the cosine rule to work out angle D.		M1		M1 for use of cosine rule	
	$\cos D = \frac{20^2 + 23^2 - 26^2}{2 \cdot 20 \cdot 23} = 0.275$ $D = 74.037 986^{\circ}$		A1		A1 for <i>D</i> and any rounding to 2 or more sf	
	Use the area sine rule to work out the area of triangle ADC.		M1		M1 for use of area sine rule	

b	Area = $\frac{1}{2}$ × 20 × 23 × sin 74.037 986° = 221.13217 m <sup>2</sup> Area of triangle ABC = $\frac{1}{2}$ × 24 × 10 = 120 m <sup>2</sup> Total area = 341.132 17 m <sup>2</sup> 341.1321 ÷ 5 = 68.226 434	341 m <sup>2</sup> 68 trees	M1 A1 A1 M1 A1 A1 A1		A1 for area correct to 3 or more sf  M1 for triangle area rule A1 for 120 cao A1 for 341 correct to 2 or 3 sf  M1 for dividing by 5 A1 for 68 cao A1 for complete clear solution with correct mathematical notation.	
82		A  B  B  B  C  Let the vertical height of the parallelogram be $H$ . $\frac{H}{a} = \sin \theta$ $H = a \sin \theta$ Area of parallelogram = base × height $= b \times a \sin \theta$ $= ab \sin \theta$	M1 A1 A1 A1 A1	2	M1 for clear diagram showing vertical height.  M1 for correct use of trigonometry to find the height A1 for correct height expression M1 for correct method of finding area of a parallelogram A1 for correct expression that will simplify to $ab \sin \theta$ A1 for complete, clear explanation with good mathematical notation	Н

83	Use Pythagoras' theorem to work out DB. $DB = \sqrt{6^2 + 8^2}$		M1	3	M1 for use of Pythagoras' theorem	Н
	= 10 cm		A1		A1 for 10 cao	
	Use the cosine rule to work out angle A. $\cos A = \frac{9^2 + 14^2 - 10^2}{10^2} = 0.7023809$		M1		M1 for use of cosine rule	
	$\cos A = \frac{1}{2} = 0.7023809$ $A = 45.381658^{\circ}$		A1		A1 for A with any rounding to 2 or more sf	
	Use the area sine rule to work out the area of triangle ADB.		M1		M1 for use of area sine rule	
	Area = $\frac{1}{2}$ x 9 x 14 x sin 45.381 658° = 44.843 478 cm <sup>2</sup>		A1		A1 for area correct to 3 or more sf	
	Area of triangle BDC = $\frac{1}{2}$ x 6 x 8 = 24 cm <sup>2</sup> Total area = 68.843 478 cm <sup>2</sup>		M1 A1		M1 for triangle area rule A1 for 24 cao	
		69 cm <sup>2</sup>	A1 A1		A1 for 69 correct to 2 or 3 sf A1 for clear, complete solution with mathematical language	
			10			

84 a	A possible triangle is one with sides 3, 4 and 5 (check, using Pythagoras' theorem).		B2	2 3	B1 for showing an example that works B1 for clarity of explanation to support the example	Н
	Then $s = 6$ and the area is $\sqrt{6 \cdot 3 \cdot 2 \cdot 1}$					
	$=\sqrt{36}=6$					
	Also, area = $\frac{1}{2}$ × base × height					
	$=\frac{1}{2} \times 3 \times 4 = 6$					
	which gives the same answer.					
b	Suppose the triangle has a side of 10 cm (you could use any number you like).  The formula gives:		B2		B1 for showing an example that works B1 for clarity of explanation to support the example	
	$\sqrt{15} \cdot 5 \cdot 5 \cdot 5 = \sqrt{1875} = 43.3 \text{ cm}^2$					
	You could also use the area sine rule:					
	$area = \frac{1}{2}ab\sin C$					
	$=\frac{1}{2} \times 10 \times 10 \times \sin 60^{\circ}$					
	= 43.3 cm <sup>2</sup> which gives the same answer.					
С	The sides of the triangle are 18 metres, 22 metres and 24 metres. So:					
	s = 32		B1		B1 for 32	
	area = $\sqrt{32^{14}10^{8}}$					
	$=\sqrt{35480}$		M1		M1 for correct substitution	
	= 189.314 55	189 m²	A1		A1 for 189 to 2 or 3 sf	
d	A diagonal will divide the field into two triangles. Measure the four sides and a diagonal. Use the formula to find the area		B1		B1 for clear explanation	
	of each triangle separately and then add the answers together.		8			

85	One example is: Start at coordinates (1, 1), then move through translation $\begin{pmatrix} 1 \\ 3 \end{pmatrix}$ then through translation $\begin{pmatrix} 3 \\ -3 \end{pmatrix}$ and finish with $\begin{pmatrix} -4 \\ 1 \end{pmatrix}$ to get back to (1, 1).		M1 B3	3	Note there are a few different correct answers. Check all vectors sum to $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ M1 for having just 3 translations B1 for the describing first translation B1 for the describing second translation B1 for the describing final translation	H
86 ai ii iii iv b		b – a –2a 2b – a 2b – a Parallel and equal in length.	B1 B1 B1 B1 B1 B1	2	B1 cao B1 cao B1 cao B1 cao B1 cao B1 for parallel B1 for equal in length	Н
87 a		They lie in a straight line, $AC = 1\frac{1}{2} \times \overline{AB}$ $\overline{BC} = \overline{AC} - \overline{AB}$ $9\mathbf{a} + 6\mathbf{b} - (6\mathbf{a} + 4\mathbf{b})$ $= 3\mathbf{a} + 2\mathbf{b}$ $\overline{AB}$ is $2 \times \overline{BC}$ So $AB : BC = 2 : 1$	B1 B1 M1 A1 B1	2	B1 for clearly stating they lie in a straight line B1 for explaining one is a multiple of the other  M1 for finding BC A1 for BC cao  B1 for correct ratio	Н

88 ai	$\overrightarrow{BC} = \mathbf{c} - \mathbf{b}$	B1	2	B1 cao	Н
ii	$\overrightarrow{NQ} = \frac{1}{2}\mathbf{b} + \frac{1}{2}(\mathbf{c} - \mathbf{b})$ $= \frac{1}{2}\mathbf{c}$	M1 A1	3	M1 method of finding NQ A1 cao	
iii	$\overline{MP} = \frac{1}{2}\mathbf{a} + \frac{1}{2}AC$ $\overline{AC} = \mathbf{c} - \mathbf{a}$ $\overline{MP} = \frac{1}{2}\mathbf{a} + \frac{1}{2}(\mathbf{c} - \mathbf{a})$ $= \frac{1}{2}\mathbf{c}$	M1 B1		M1 method of finding MP B1 cao	
b	It is a parallelogram, because $\overline{NQ} = MP = \frac{1}{2}\mathbf{c}$ and hence they are parallel and equal in length.	B1 B2 <b>9</b>		B1 for parallelogram  B1 for stating vectors are parallel B1 for stating vectors will be same length	
89	$\overline{AB} = \mathbf{b} - \mathbf{a},$ $\overline{AC} = \overline{AO} + \overline{OC}$ $= -\mathbf{a} + 3\mathbf{b} - 2\mathbf{a}$ $= 3\mathbf{b} - 3\mathbf{a}$ so $\overline{AC} = 3 \overline{AB}$ and hence ABC is a straight line.	B1 M1 A1 A1 5	2	B1 cao M1 for adding vectors  A1 cao A1 for explaining the two vectors are multiples of each other A1 for explaining this gives a straight line	Н

90	The knight can get to all the squares shown.	M1	3	M1 is for a clear diagram to support the explanation, showing all the possible places the knight can move to	Н
	Do not forget that you can use -a and -b as well as a and b.				
	The starting position must match the question (bottom left white square).				
	The lines show all the possible paths of the Knight, using <b>a</b> , <b>b</b> , <b>–a</b> and <b>–b</b> .				
	There are many ways to reach the king. However, there are three ways to get to the king in the minimum of five moves.	В4		B1 for explaining there are numerous ways to get to the king B1 for explaining there is a minimum of five moves to get to the king B1 for explaining there are only three ways to get to the king with these 5 minimum moves B1 for a clear cohesive explanation	
		5			